

Cosmic Ray Streaming in Galaxy Clusters



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Acknowledgements



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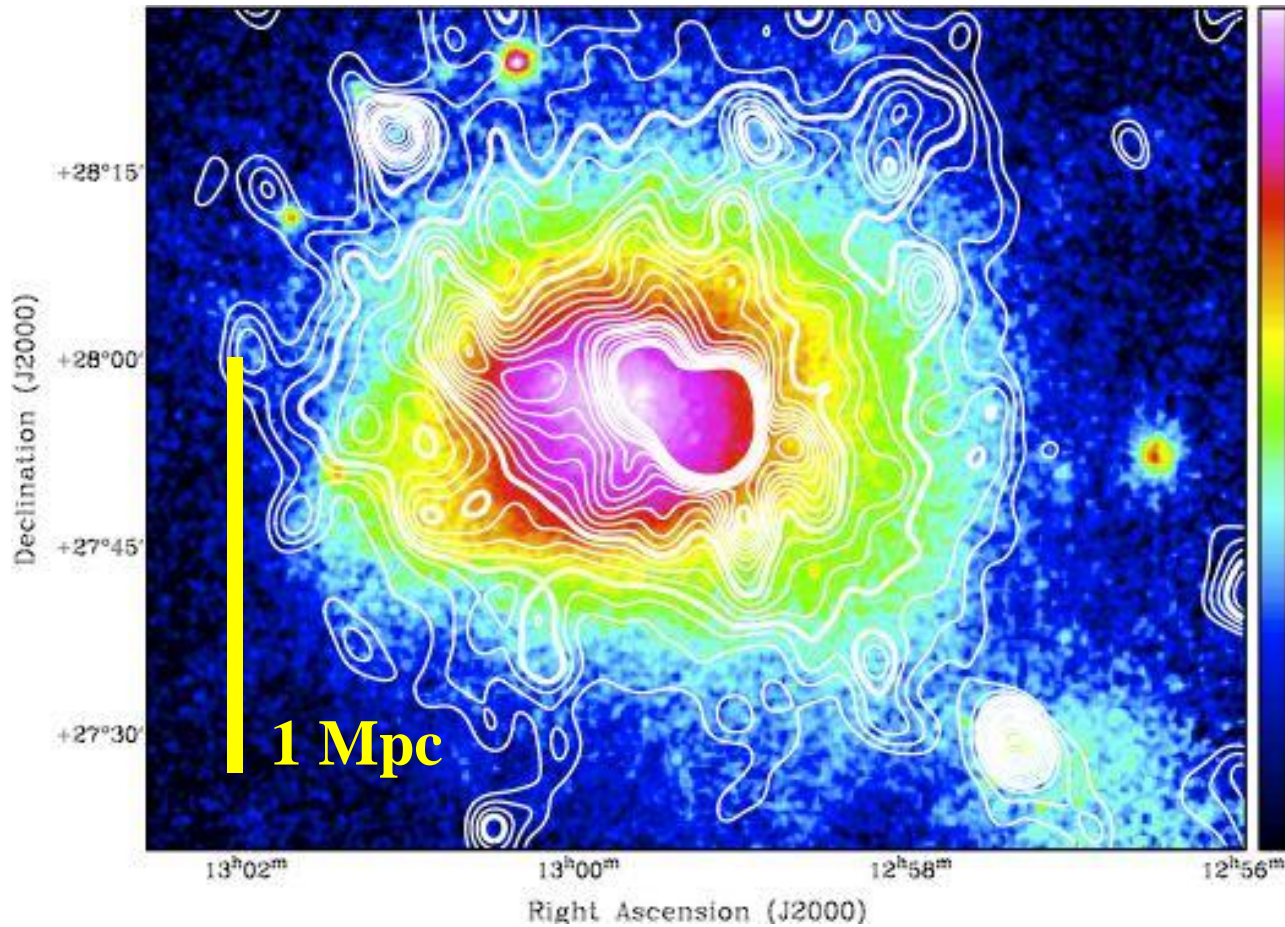
Fulai Guo
Shanghai Astronomical
Observatory

Galaxy Clusters

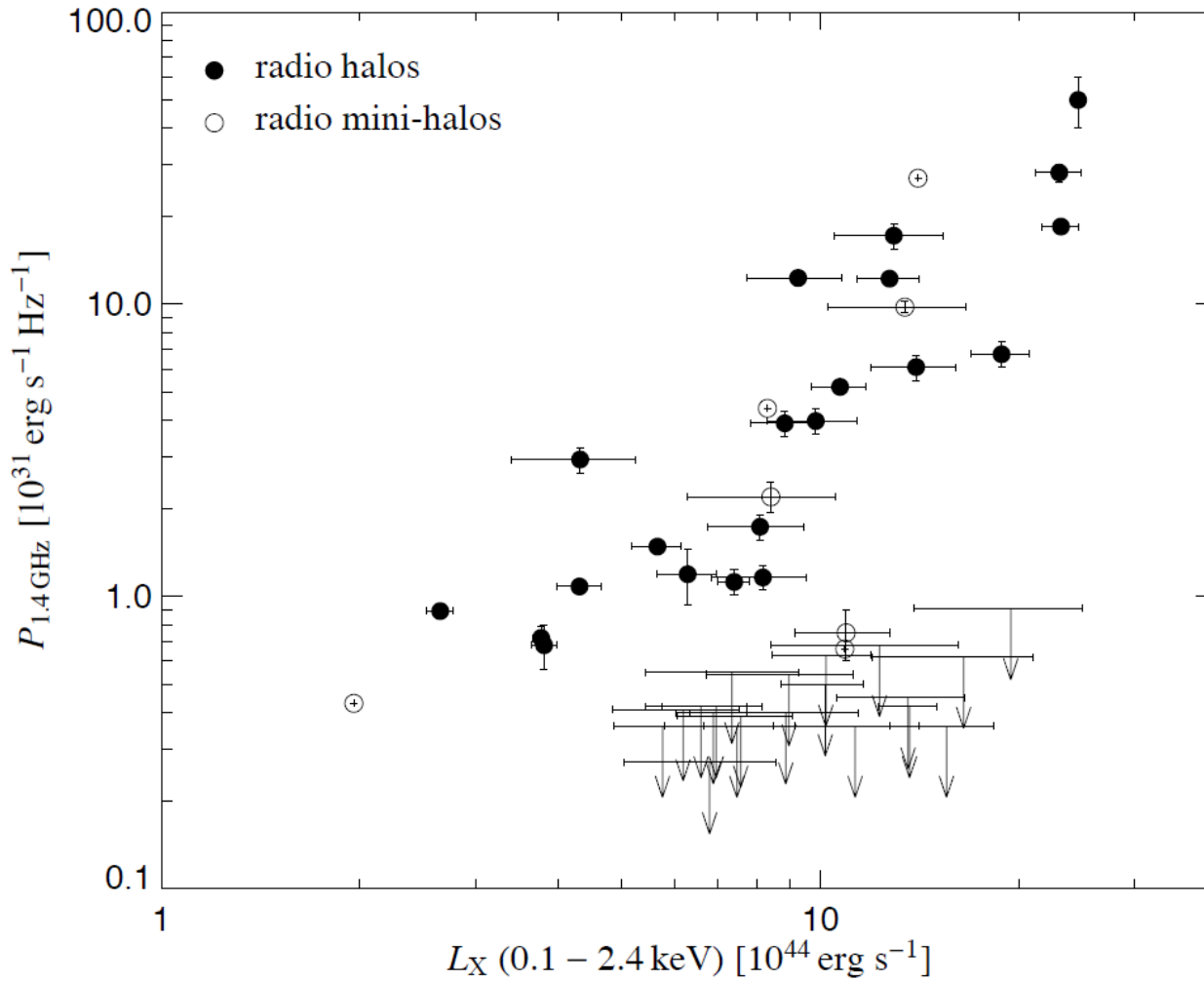


1 Mpc

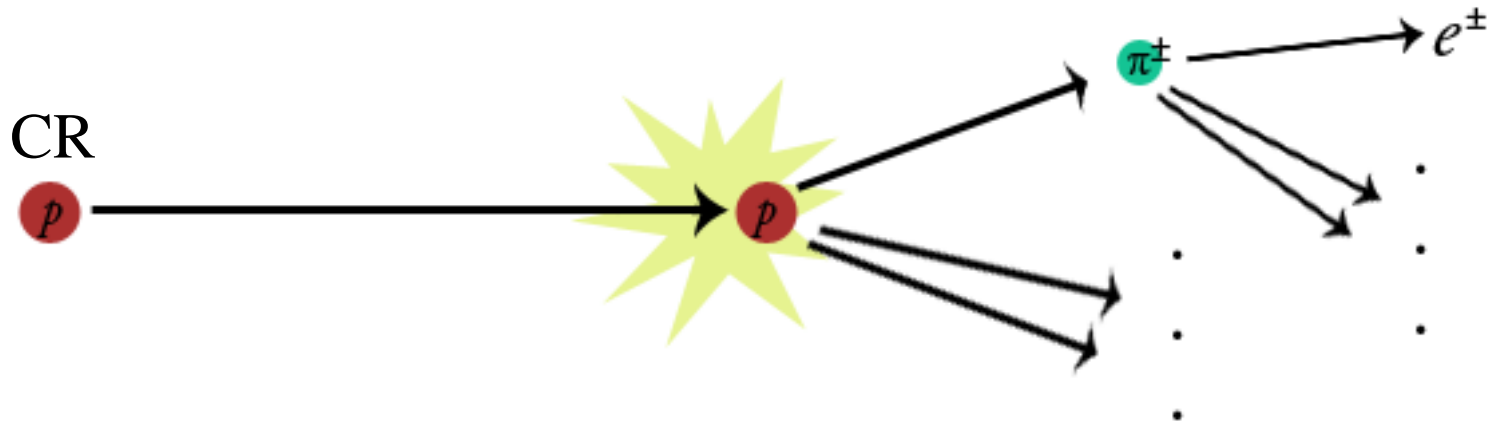
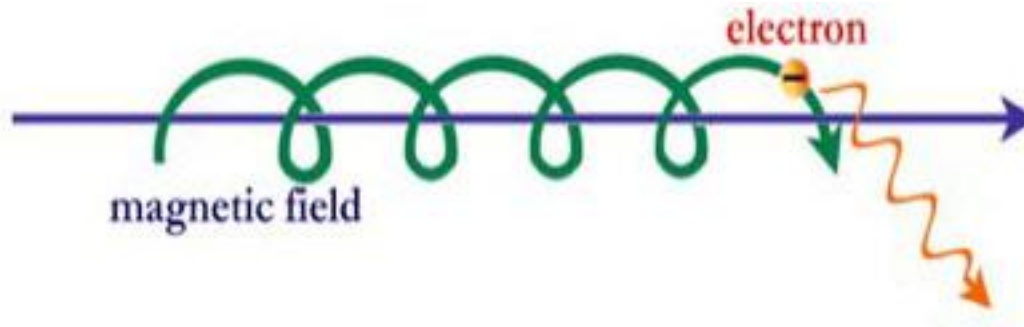
Radio Haloes



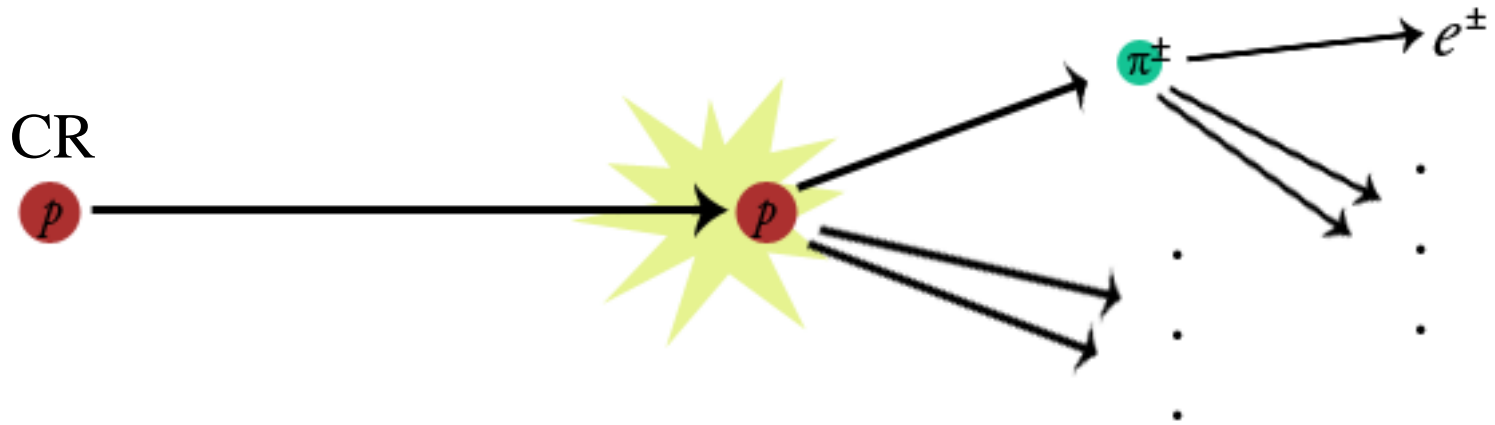
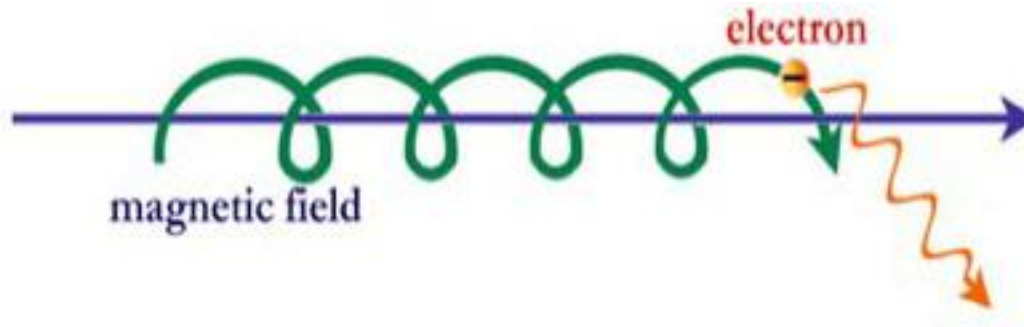
Radio Haloes



Hadronic Model

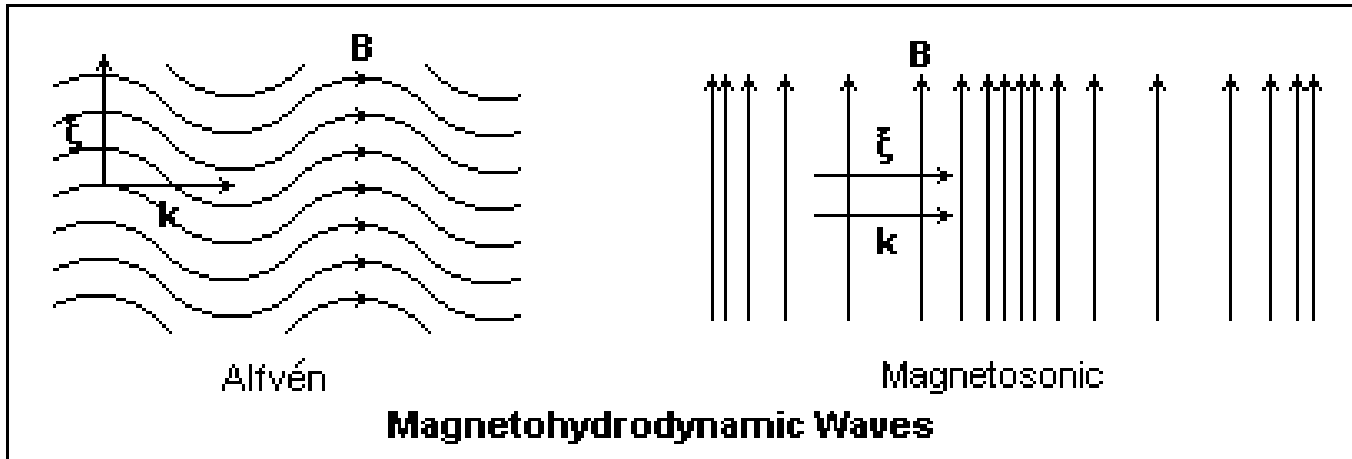


Hadronic Model

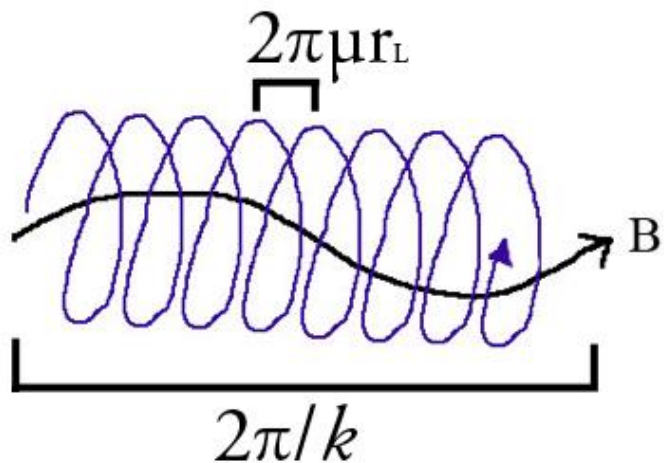
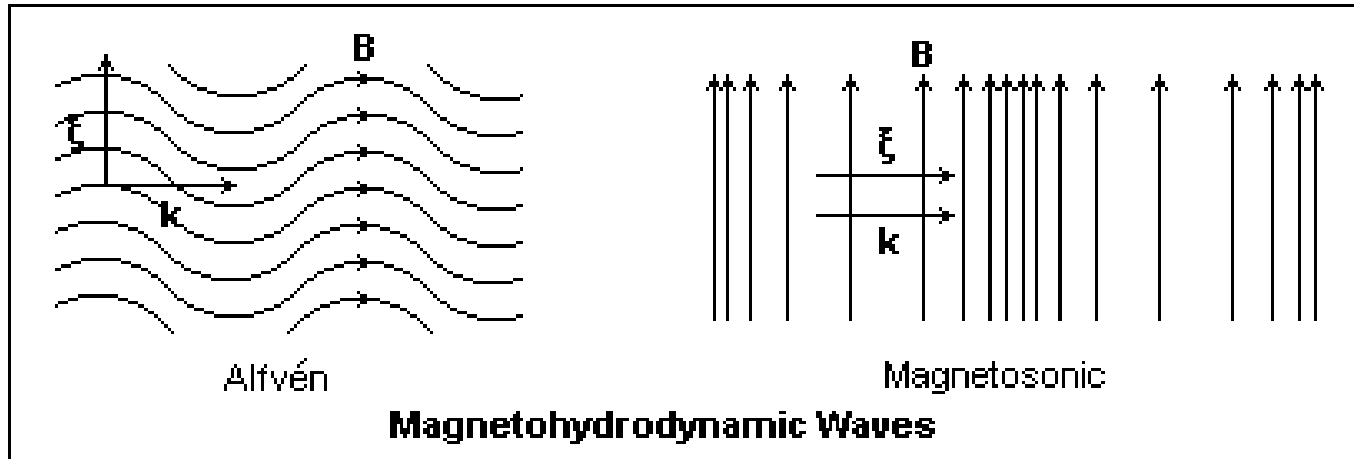


Possibly detectable in gamma rays and neutrinos

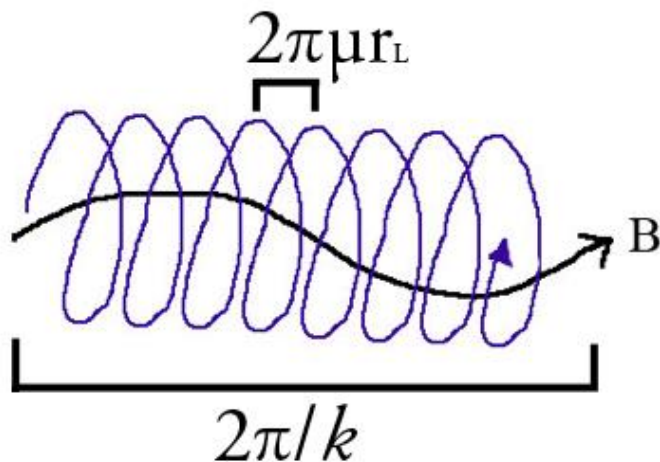
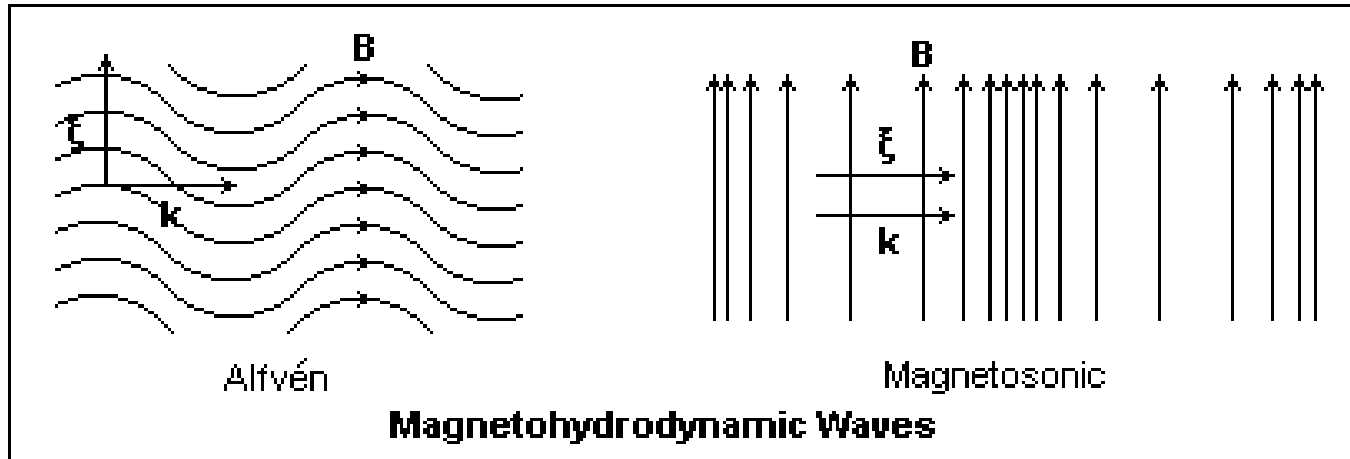
CR Transport - Alfvén Waves



CR Transport - Alfvén Waves



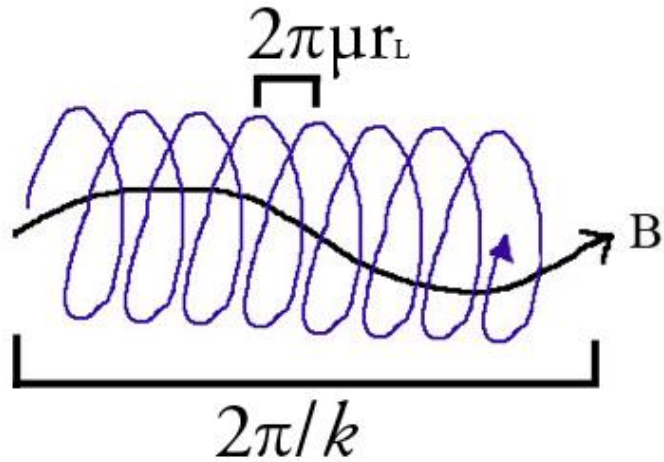
CR Transport - Alfvén Waves



Resonance condition

$$k_{\parallel} = \frac{1}{\mu r_L}, \quad r_L = \gamma r_0$$

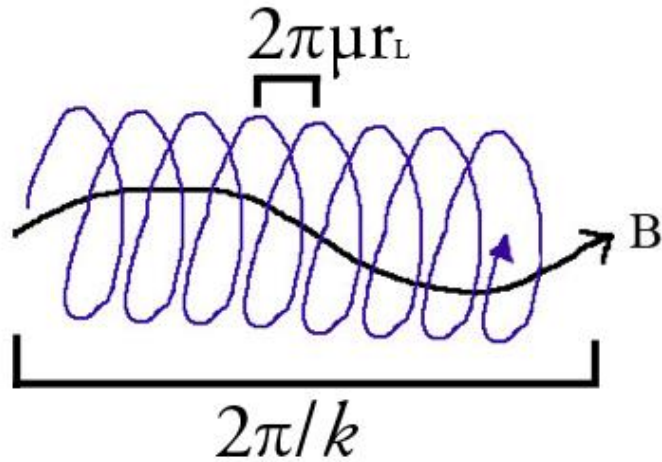
Streaming Instability



Resonance condition

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Streaming Instability



Resonance condition

$$k_{\parallel} = \frac{1}{\mu r_L}, \quad r_L = \gamma r_0$$

Compare bulk CR drift speed v_D with Alfvén speed v_A :

$$\vec{v}_D P_c \equiv \vec{F}_c$$

$$v_D > v_A$$

waves generated

$$v_D < v_A$$

waves damped

$$v_A = \frac{B}{\sqrt{4\pi\rho}}$$

$$v_D = v_A$$

isotropy (no CR flux in wave frame)

Self Confinement

no waves, no scattering $\rightarrow v_D = c$

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but CRs generate waves via streaming instability, so

waves, scattering $\rightarrow v_D = v_A$

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More accurately, the bulk motion of CRs is determined
by

$$\Gamma_{\text{growth}}(v_D) = \Gamma_{\text{damping}}$$

Evolution Equations

Mass:
$$\frac{\partial \rho}{\partial t} + \nabla \cdot (\rho \mathbf{v}) = 0$$

Momentum:
$$\frac{\partial(\rho \mathbf{v})}{\partial t} + \nabla \cdot (\rho \mathbf{v} \mathbf{v}) = -\nabla P_g - \nabla P_c - \rho \nabla \Phi$$

Energy:
$$\frac{\partial E_g}{\partial t} + \nabla \cdot (E_g \mathbf{v}) = -P_g \nabla \cdot \mathbf{v} - \mathbf{v}_A \cdot \nabla P_c - n_e^2 \Lambda(T)$$

CR Energy:
$$\begin{aligned} \frac{\partial E_c}{\partial t} + \nabla \cdot [E_c(\mathbf{v} + \mathbf{v}_A)] &= -P_c \nabla \cdot (\mathbf{v} + \mathbf{v}_A) + \mathbf{v}_A \cdot \nabla P_c \\ &\quad + \nabla \cdot (\kappa \nabla P_c) \end{aligned}$$

B Field:
$$\frac{\partial \mathbf{B}}{\partial t} = \nabla \times (\mathbf{v} \times \mathbf{B})$$

Evolution Equations

~~Mass: $\frac{\partial \rho}{\partial t} + \nabla \cdot (\rho \mathbf{v}) = 0$~~

~~Momentum: $\frac{\partial(\rho \mathbf{v})}{\partial t} + \nabla \cdot (\rho \mathbf{v} \mathbf{v}) = -\nabla P_g - \nabla P_c - \rho \nabla \Phi$~~

~~Energy: $\frac{\partial E_g}{\partial t} + \nabla \cdot (E_g \mathbf{v}) = -P_g \nabla \cdot \mathbf{v} - \mathbf{v}_A \cdot \nabla P_c - n_e^2 \Lambda(T)$~~

CR Energy: $\frac{\partial E_c}{\partial t} + \nabla \cdot [E_c(\mathbf{v} + \mathbf{v}_A)] = -P_c \nabla \cdot (\mathbf{v} + \mathbf{v}_A) + \mathbf{v}_A \cdot \nabla P_c$
 $+ \nabla \cdot (\kappa \nabla P_c)$

~~B Field: $\frac{\partial \mathbf{B}}{\partial t} = \nabla \times (\mathbf{v} \times \mathbf{B})$~~

Evolution Equation

$$\begin{aligned} \frac{\partial f_p}{\partial t} + (\mathbf{u} + \mathbf{v}_A) \cdot \nabla f_p = & \\ & \frac{1}{3} p \frac{\partial f_p}{\partial p} \nabla \cdot (\mathbf{u} + \mathbf{v}_A) \\ & + \frac{1}{p^3} \nabla \cdot \left(\frac{\Gamma_{\text{damp}} B^2 \mathbf{n}}{4\pi^3 m_p \Omega_0 v_A} \frac{\mathbf{n} \cdot \nabla f_p}{|\mathbf{n} \cdot \nabla f_p|} \right) \\ & - \nabla \cdot \left[\frac{v_A L_{\text{MHD}}}{3} \rho^{1.5} \nabla \left(\frac{f_p}{\rho^{1.5}} \right) \right] \end{aligned}$$

Evolution Equation

$$\begin{aligned} & \text{advection} \\ \frac{\partial f_p}{\partial t} + (\mathbf{u} + \mathbf{v}_A) \cdot \nabla f_p = & \\ & \text{compression/} \\ & \text{expansion} \\ & \frac{1}{3} p \frac{\partial f_p}{\partial p} \nabla \cdot (\mathbf{u} + \mathbf{v}_A) \\ & \text{streaming} \\ & + \frac{1}{p^3} \nabla \cdot \left(\frac{\Gamma_{\text{damp}} B^2 \mathbf{n}}{4\pi^3 m_p \Omega_0 v_A} \frac{\mathbf{n} \cdot \nabla f_p}{|\mathbf{n} \cdot \nabla f_p|} \right) \\ & \text{turbulent} \\ & \text{mixing} \\ & - \nabla \cdot \left[\frac{v_A L_{\text{MHD}}}{3} \rho^{1.5} \nabla \left(\frac{f_p}{\rho^{1.5}} \right) \right] \end{aligned}$$

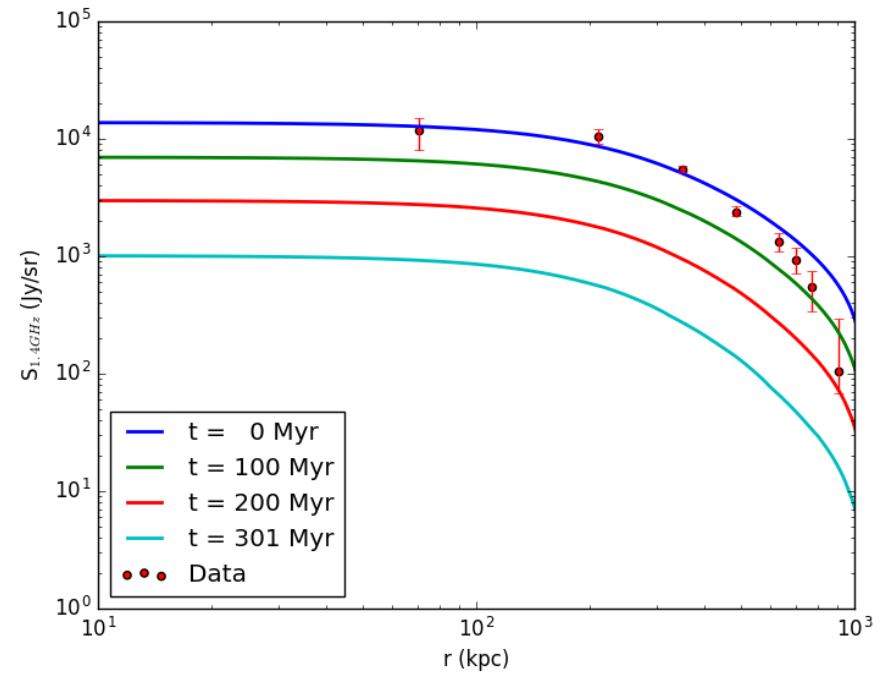
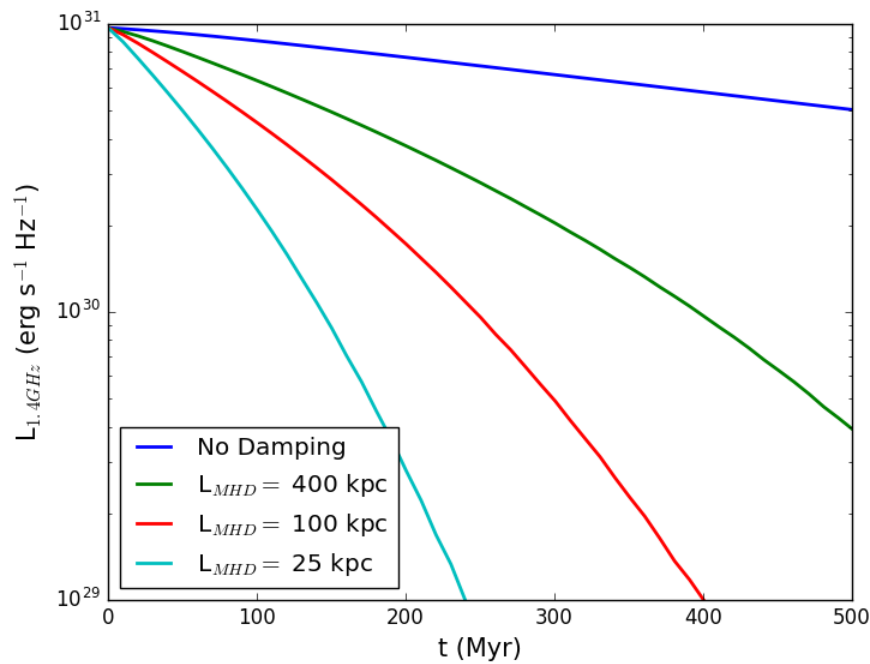
Goal:

With the above simple physics, what happens to radio and gamma emission in galaxy clusters over time?

Method:

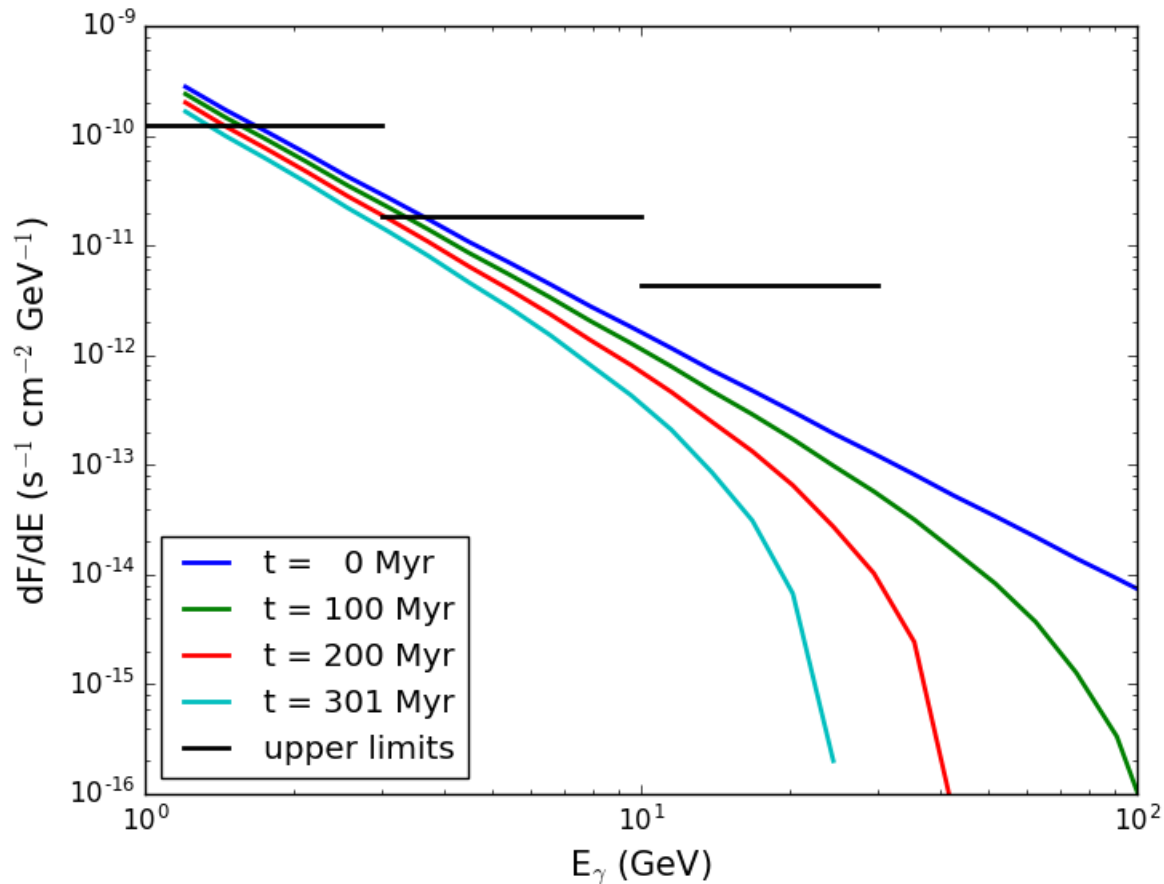
Spherically symmetric 1D simulations of CR streaming in individual galaxy clusters using ZEUS

Coma Cluster Radio Emission



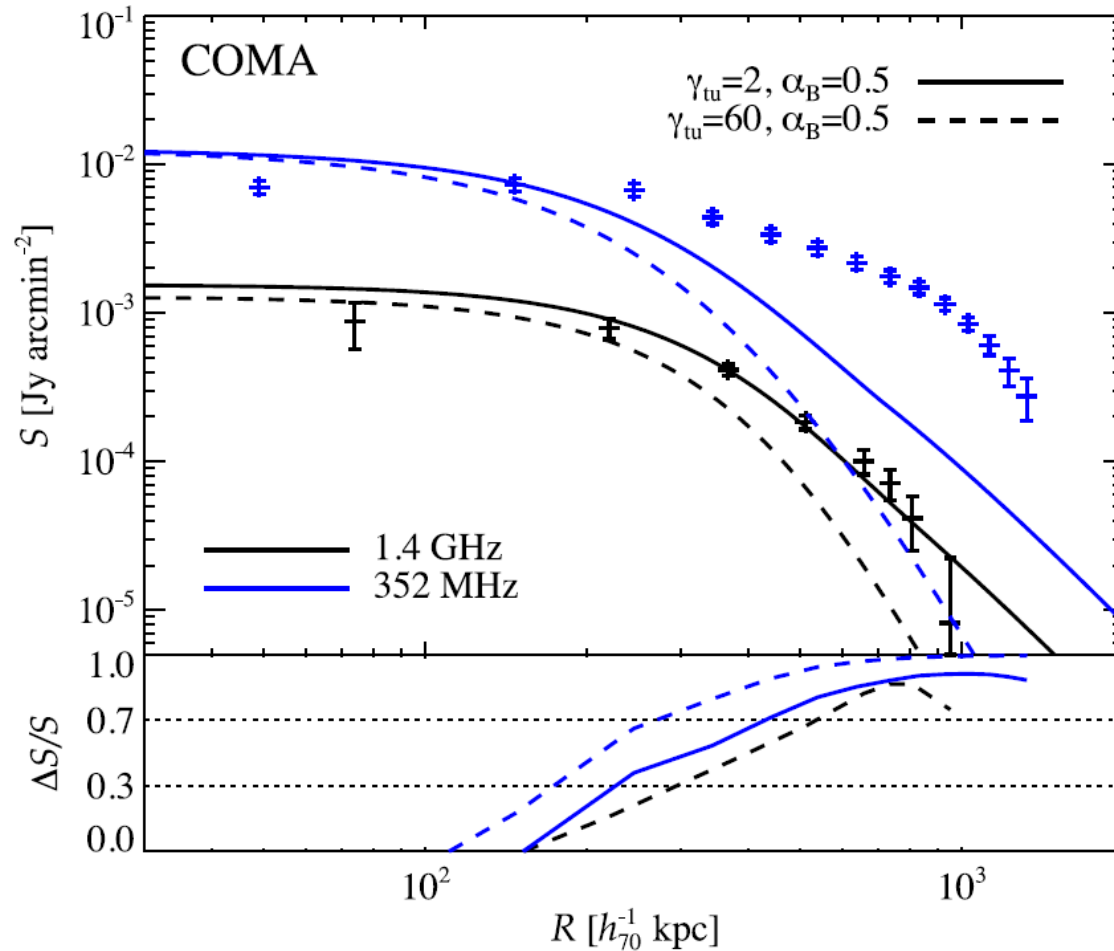
*Observations from Deiss et al 1997
(Effelsberg 100-m telescope)

Coma Cluster γ -ray Emission



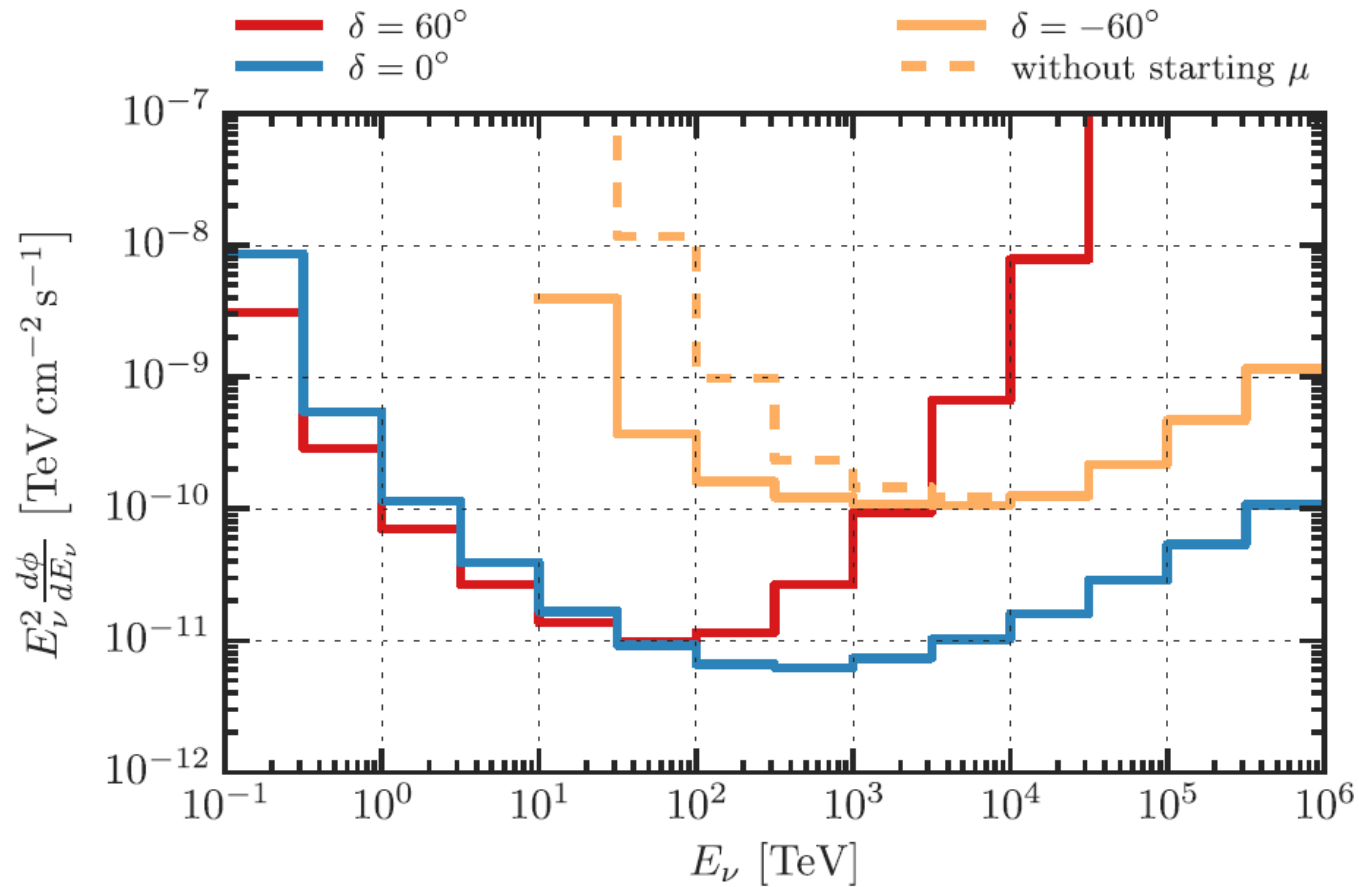
*Upper limits from Arlen et al 2012 (*Fermi* and VERITAS)

Problem: Lower Frequencies



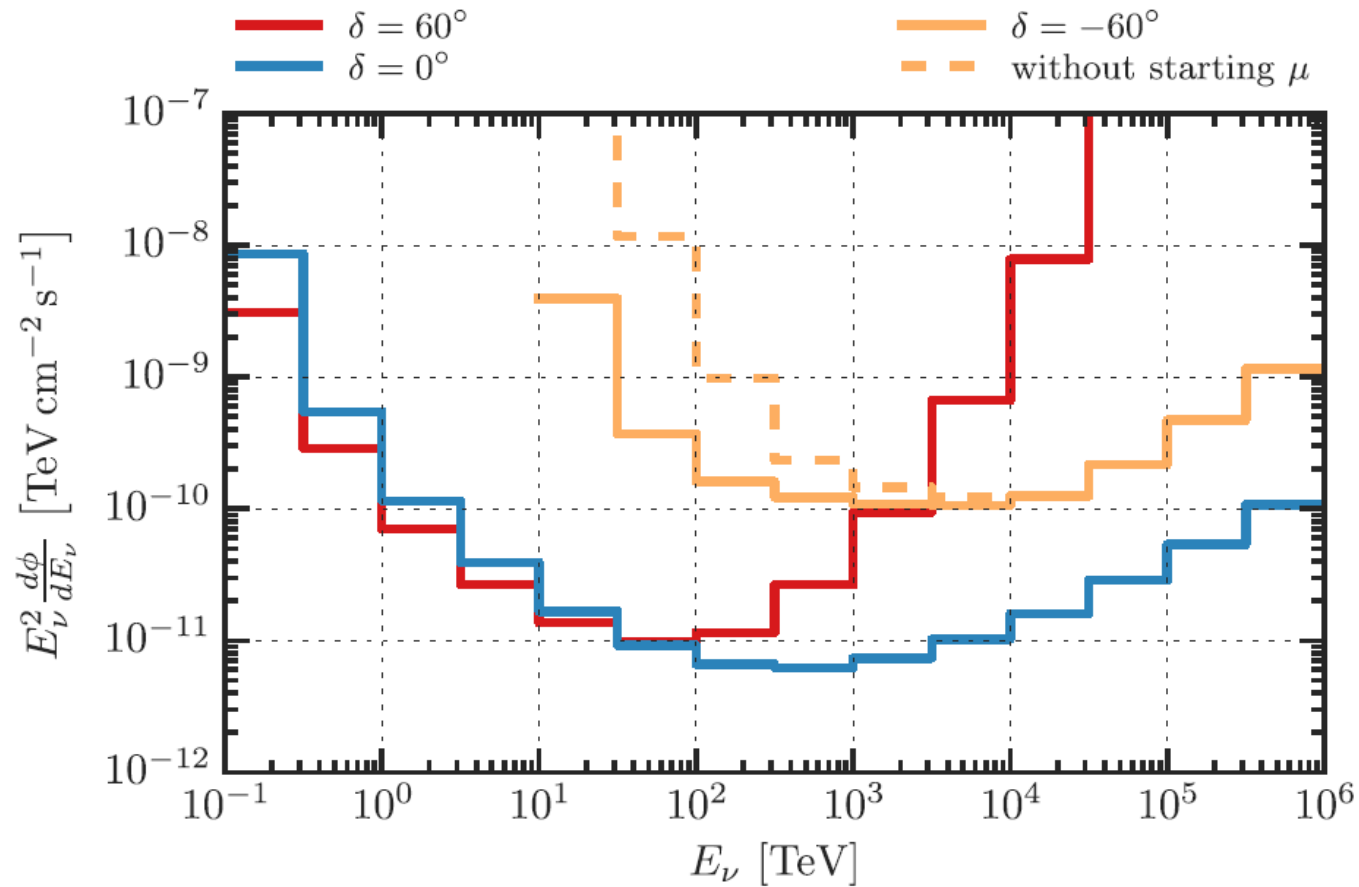
*352 MHz: Brown and Rudnick 2011 (WSRT)

Coma Cluster Neutrino Emission?



*Aartsen et al 2017

Coma Cluster Neutrino Emission?



*Aartsen et al 2017

Preliminary Coma prediction

Conclusions

1. CR distribution in Coma cluster is spatially very flat
2. Reasonable levels of wave damping can dim Coma's radio halo on time scales of 100s of Myr

Limitations

1. Assumptions made about B -field strength and topology affect results
2. Low frequency data cannot be explained
3. Gamma ray non-detections are getting more and more restrictive