

# Sensitivity of JEM-EUSO to Ensemble Variations in the Ultra-High Energy Cosmic Ray Flux

M. Ahlers, L. Anchordoqui, A. Olinto, T. Paul, A. Taylor

IceCube Particle Astrophysics Symposium, Madison, May 13, 2013

# Outline

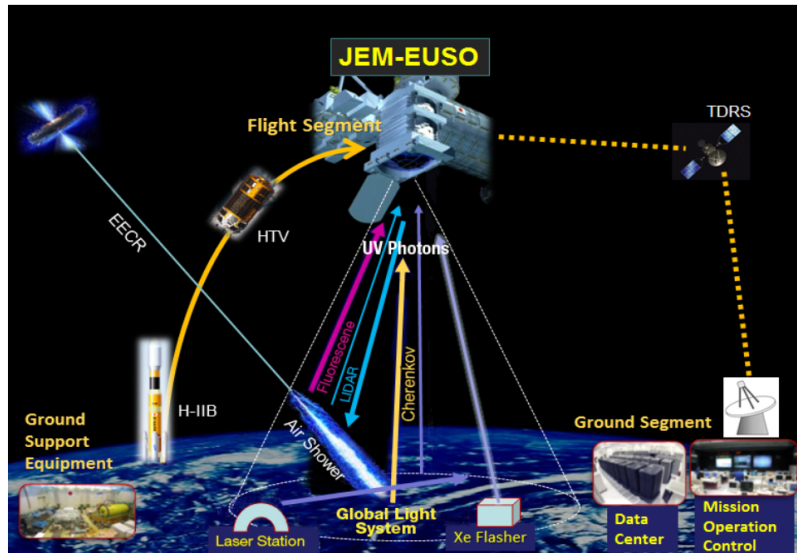
- What are ensemble variations ?
- Dependence of on source density, proximity, composition, energy, ...
- Some examples compared to current data
- Sensitivity of JEM-EUSO to ensemble variations

---

M. Ahlers, L. Anchordoqui, and A. Taylor, PRD87 (2013)  
[arXiv:1209.5427]

M. Ahlers, L. Anchordoqui, A. Olinto, T. Paul, and A. Taylor, in preparation

# JEM-EUSO Mission (reminder)



## Ensemble Variation : Introduction

- Common approach : make a prediction of UHECR spectrum assuming some composition and CR emission rate density (in units of  $\text{eV}^{-1} \text{cm}^{-3} \text{s}^{-1}$ )
  - ... assuming spatially homogenous and isotropic emission

## Ensemble Variation : Introduction

- Common approach : make a prediction of UHECR spectrum assuming some composition and CR emission rate density (in units of  $\text{eV}^{-1} \text{cm}^{-3} \text{s}^{-1}$ )
  - ... assuming spatially homogenous and isotropic emission
- Real life : at highest energies, emission is from an ensemble of  $N$  (local) sources with different emission rates (cosmic variance)

## Ensemble Variation : Introduction

- Common approach : make a prediction of UHECR spectrum assuming some composition and CR emission rate density (in units of  $\text{eV}^{-1} \text{cm}^{-3} \text{s}^{-1}$ )
  - ... assuming spatially homogenous and isotropic emission
- Real life : at highest energies, emission is from an ensemble of  $N$  (local) sources with different emission rates (cosmic variance)
- We don't know (or have only partial understanding of) :  
source locations, density, composition

## Ensemble Variation : Introduction

- Common approach : make a prediction of UHECR spectrum assuming some composition and CR emission rate density (in units of  $\text{eV}^{-1} \text{cm}^{-3} \text{s}^{-1}$ )
  - ... assuming spatially homogenous and isotropic emission
- Real life : at highest energies, emission is from an ensemble of  $N$  (local) sources with different emission rates (cosmic variance)
- We don't know (or have only partial understanding of) :  
source locations, density, composition
- First order approximation : mean spectrum assuming spatially homogeneous emission & isotropic sources (and some composition).

## Ensemble Variation : Introduction

- Common approach : make a prediction of UHECR spectrum assuming some composition and CR emission rate density (in units of  $\text{eV}^{-1} \text{cm}^{-3} \text{s}^{-1}$ )
  - ... assuming spatially homogenous and isotropic emission
- Real life : at highest energies, emission is from an ensemble of  $N$  (local) sources with different emission rates (cosmic variance)
- We don't know (or have only partial understanding of) :  
source locations, density, composition
- First order approximation : mean spectrum assuming spatially homogeneous emission & isotropic sources (and some composition).
- Next step : quantify possible deviations from the mean prediction. *i.e.* estimate next statistical moment of the distribution.  
This is the ensemble variation .



# Ensemble Variations

- **Ensemble variations** are variations in the energy spectrum relative to a mean prediction.

# Ensemble Variations

- **Ensemble variations** are variations in the energy spectrum relative to a mean prediction.
- Influenced by UHECR source and propagation characteristics
  - Distribution of *discrete* local sources
  - Composition
  - Energy losses during propagation

# Ensemble Variations

- **Ensemble variations** are variations in the energy spectrum relative to a mean prediction.
- Influenced by UHECR source and propagation characteristics
  - Distribution of *discrete* local sources
  - Composition
  - Energy losses during propagation
- At the highest energies, flux variation could be “large” : relatively few local sources (in GZK region) can contribute

# Ensemble Variations

- **Ensemble variations** are variations in the energy spectrum relative to a mean prediction.
- Influenced by UHECR source and propagation characteristics
  - Distribution of *discrete* local sources
  - Composition
  - Energy losses during propagation
- At the highest energies, flux variation could be “large” : relatively few local sources (in GZK region) can contribute
- These variations are one manifestation of the “cosmic variance”. (Anisotropy is another one)

# Ensemble Variations

- **Ensemble variations** are variations in the energy spectrum relative to a mean prediction.
- Influenced by UHECR source and propagation characteristics
  - Distribution of *discrete* local sources
  - Composition
  - Energy losses during propagation
- At the highest energies, flux variation could be “large” : relatively few local sources (in GZK region) can contribute
- These variations are one manifestation of the “cosmic variance”. (Anisotropy is another one)
- Analytical approaches have been pursued to quantify the variation  
[M. Ahlers, L. Anchordoqui and A. Taylor, PRD87 \(2013\)](#)

# Ensemble Variations

- **Ensemble variations** are variations in the energy spectrum relative to a mean prediction.
- Influenced by UHECR source and propagation characteristics
  - Distribution of *discrete* local sources
  - Composition
  - Energy losses during propagation
- At the highest energies, flux variation could be “large” : relatively few local sources (in GZK region) can contribute
- These variations are one manifestation of the “cosmic variance”. (Anisotropy is another one)
- Analytical approaches have been pursued to quantify the variation  
[M. Ahlers, L. Anchordoqui and A. Taylor, PRD87 \(2013\)](#)
- **Will JEM-EUSO be able to discern this variation from statistical fluctuations?**

## Flux Variation

Defining residual  $\delta X \equiv X - \langle X \rangle$ , the covariance between relative flux of two particle species  $A, B$  populating energy bins  $i, j$  :

$$\langle \delta N_{A,i} \delta N_{B,j} \rangle \equiv \langle N_{A,i} N_{B,j} \rangle - \langle N_{A,i} \rangle \langle N_{B,j} \rangle$$

Relative variation of total flux described by two-point density perturbations :

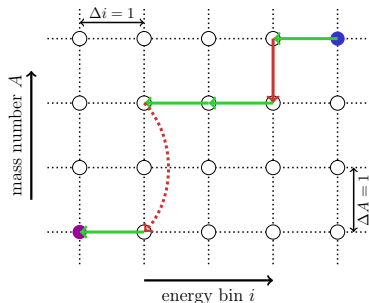
$$\sigma_{\text{loc}}^2 = \sum_{A,B} \frac{\langle \delta N_A(E/A) \delta N_B(E/B) \rangle}{\langle N_{\text{tot}}(E) \rangle^2}$$

M. Ahlers, L. Anchordoqui and A. Taylor, PRD87 (2013)

# Flux Variation

Analytical estimate of ensemble variations including :

- Density of sources
- Source emission parameters  
 $\gamma$  and  $E_{\max}$
- Propagation effects  
[ M. Ahlers and A. Taylor, PRD82 (2010) ]
- Energy losses  $\rightarrow$  migration in energy bin
- Photodisintegration  $\rightarrow$  migration in mass



$\mathcal{H}_0 \sim 10^{-6} - 10^{-5} \text{ Mpc}^{-3}$  consistent with absence of clustering

Pierre Auger Collaboration JCAP 2013 (accepted)

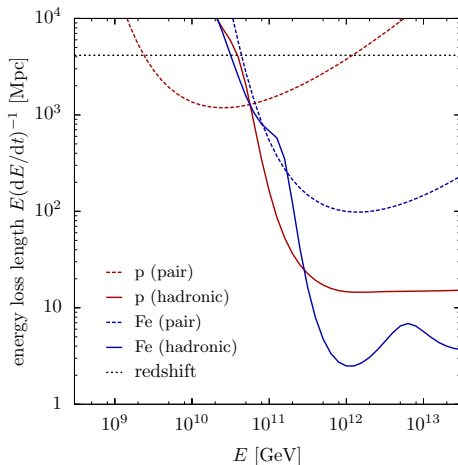
E. Waxman, K. B. Fisher, T. Piran ApJ 483 (1997)

T. Kashti and E. Waxman, JCAP 05 (2008)

H. Takami, S. Inoue, and T. Yamamoto, Astropart. Phys 35 (2012)

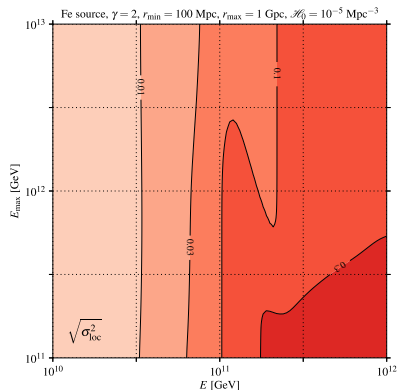
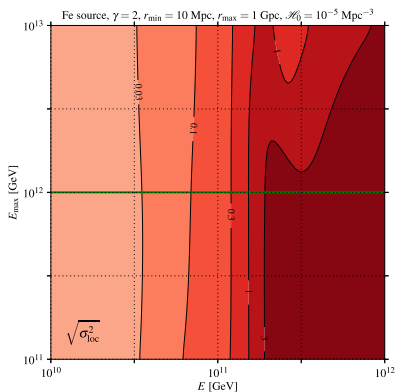


# Energy Loss Lengths



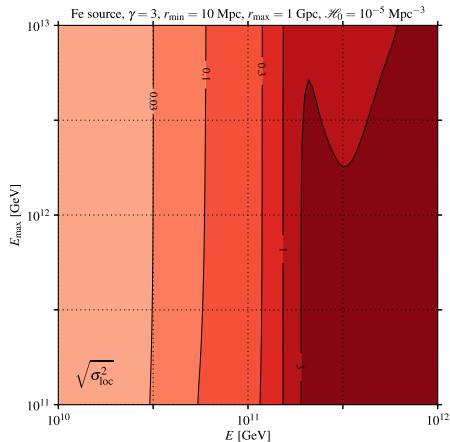
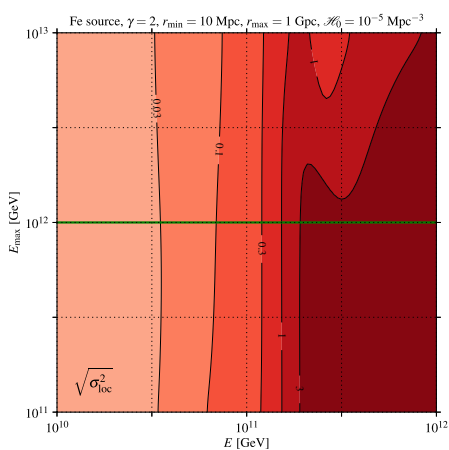
- Energy losses carve the average energy spectrum and modulate the ensemble variation

# Relative Ensemble Variation (Fe sources)



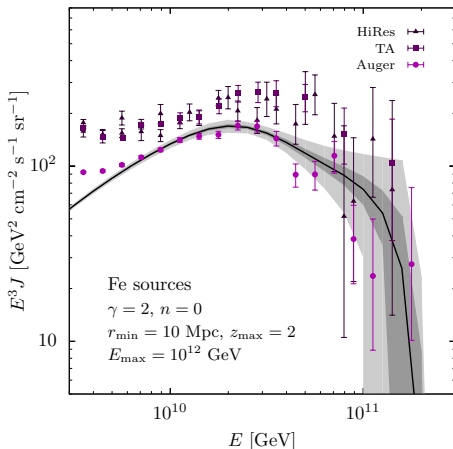
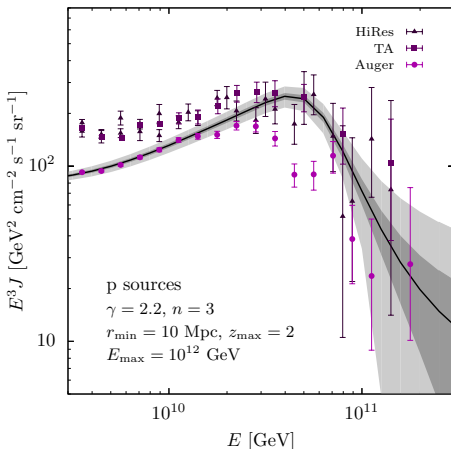
- Different minimal distances ( $r_{\min}$ ) to source populations, with the same source density assumption
- $r_{\min} = 10$  Mpc : relative ensemble fluctuation increases with  $E$  (above the level of 10% at about  $10^{10.8}$  GeV)
- $r_{\min} = 100$  Mpc : ensemble variations smaller by factor  $\sim 3$

# Relative Ensemble Variation (Fe sources)



Results do not strongly depend on the spectral index

$$r_{\min} = 10 \text{ Mpc}$$

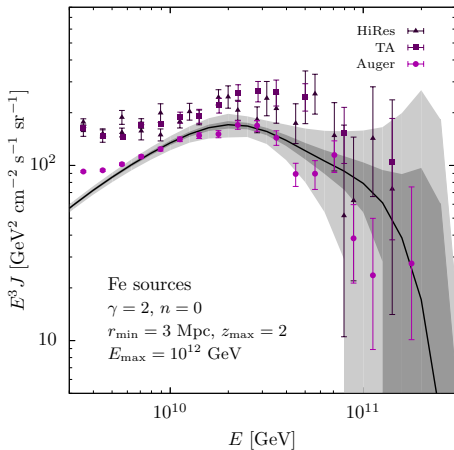
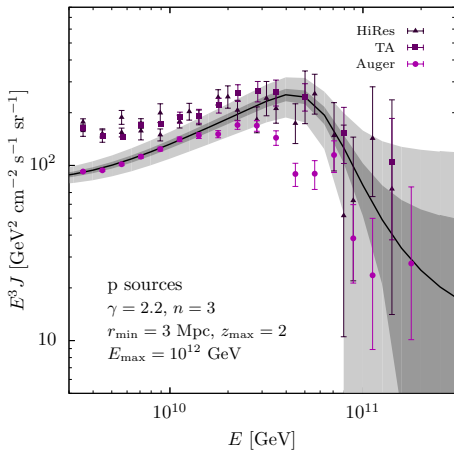


Approximate variation of the flux assuming a local source distribution:

$\mathcal{H}_0 = 10^{-5} \text{ Mpc}^{-3}$  (dark gray band)

$\mathcal{H}_0 = 10^{-6} \text{ Mpc}^{-3}$  (light gray band)

$$r_{\min} = 3 \text{ Mpc}$$

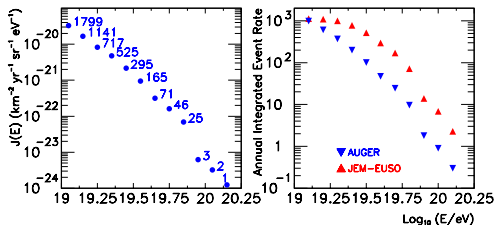
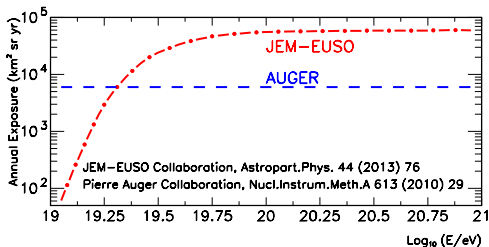


Approximate variation of the flux assuming a local source distribution:

$H_0 = 10^{-5} \text{ Mpc}^{-3}$  (dark gray band)

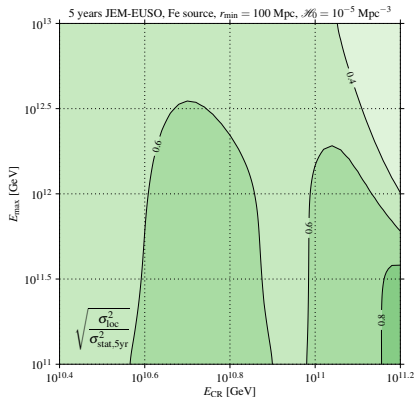
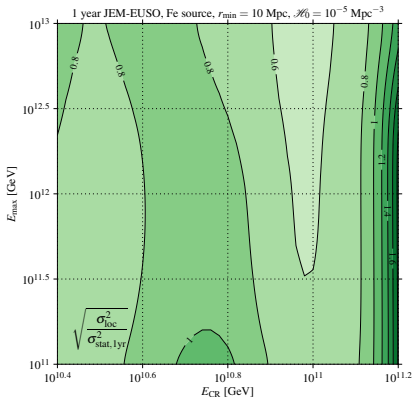
$H_0 = 10^{-6} \text{ Mpc}^{-3}$  (light gray band)

# JEM-EUSO Potential : Annual Exposure



Estimate of JEM-EUSO sample size  $\Rightarrow$  scale Auger spectrum according to Auger vs. JEM-EUSO aperture.

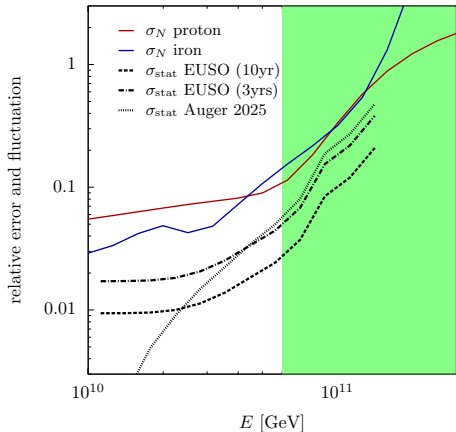
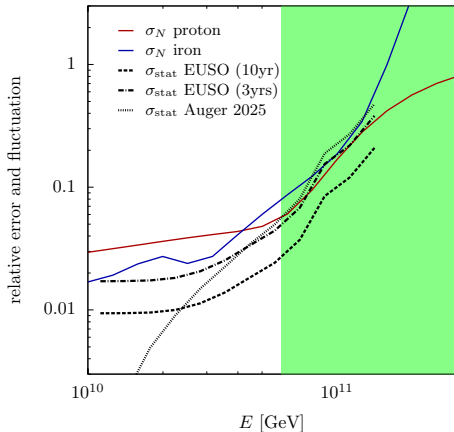
# Ensemble Variations vs. Statistics, JEM-EUSO



Uncovering hints if  $r_{\min} = 10$  Mpc is possible

$r_{\min} = 100$  Mpc probably out of range

# Ensemble fluctuation compared to statistical errors





## Take-Home Message

- “Ensemble variations” are deviations from mean prediction due to cosmic variance
- These variations persist in limit of large statistics

## Take-Home Message

- “Ensemble variations” are deviations from mean prediction due to cosmic variance
- These variations persist in limit of large statistics
- Details of ensemble variations depend on (and hence provide information on)
  - source density
  - distribution of local sources (eg. proximity of closest source(s))
  - nuclear composition
  - injection parameters

## Take-Home Message

- “Ensemble variations” are deviations from mean prediction due to cosmic variance
- These variations persist in limit of large statistics
- Details of ensemble variations depend on (and hence provide information on)
  - source density
  - distribution of local sources (eg. proximity of closest source(s))
  - nuclear composition
  - injection parameters
- Complementary to information on cosmic variance from anisotropy searches
- Example : could compare energy spectra for northern “universe” vs. southern “universe”

## Take-Home Message

- “Ensemble variations” are deviations from mean prediction due to cosmic variance
- These variations persist in limit of large statistics
- Details of ensemble variations depend on (and hence provide information on)
  - source density
  - distribution of local sources (eg. proximity of closest source(s))
  - nuclear composition
  - injection parameters
- Complementary to information on cosmic variance from anisotropy searches
- Example : could compare energy spectra for northern “universe” vs. southern “universe”
- JEM-EUSO has potential to discern the ensemble variation relative to mean prediction for a power-law, potentially shedding light on source density, distance to the closest sources, composition

## Take-Home Message

- “Ensemble variations” are deviations from mean prediction due to cosmic variance
- These variations persist in limit of large statistics
- Details of ensemble variations depend on (and hence provide information on)
  - source density
  - distribution of local sources (eg. proximity of closest source(s))
  - nuclear composition
  - injection parameters
- Complementary to information on cosmic variance from anisotropy searches
- Example : could compare energy spectra for northern “universe” vs. southern “universe”
- JEM-EUSO has potential to discern the ensemble variation relative to mean prediction for a power-law, potentially shedding light on source density, distance to the closest sources, composition