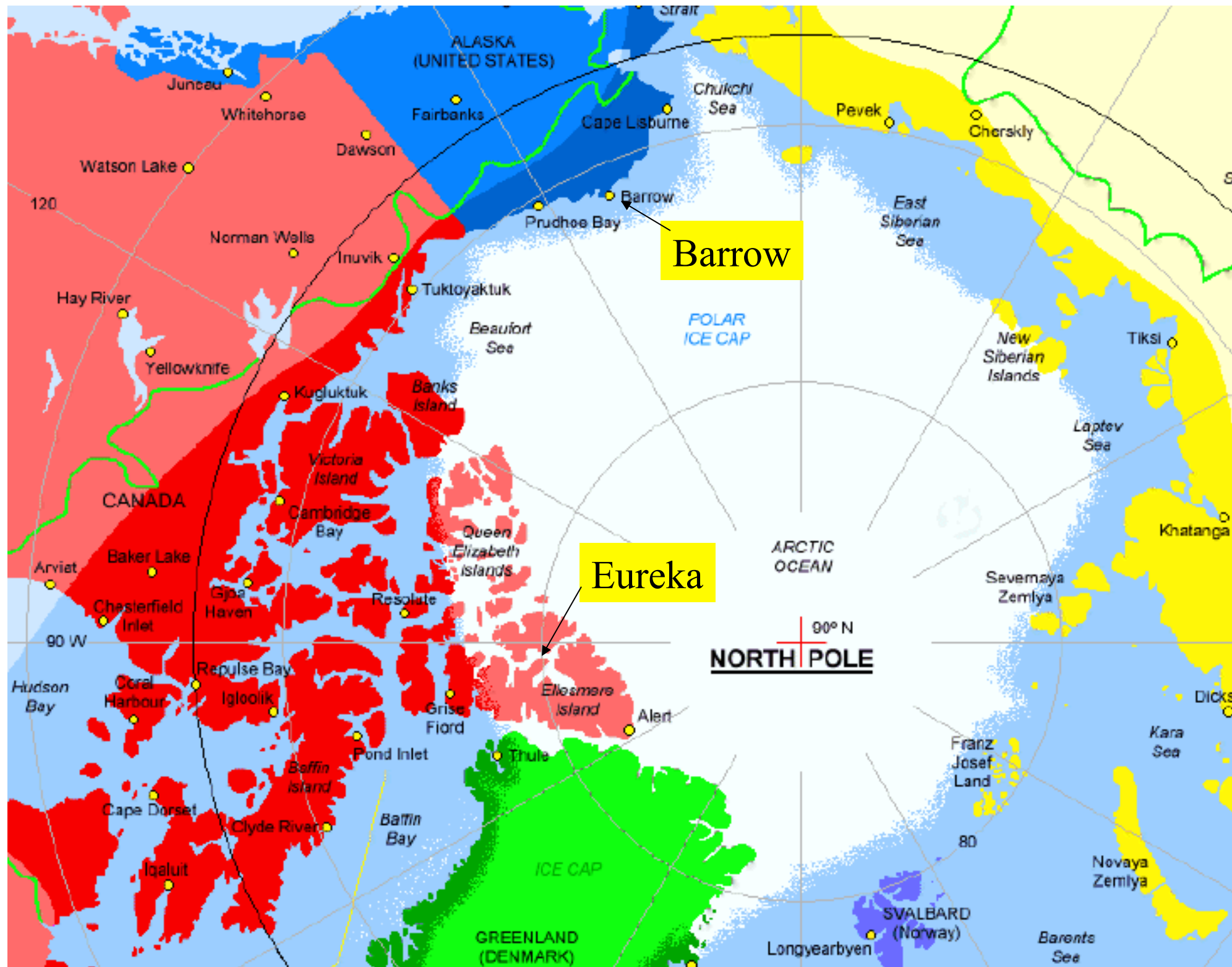


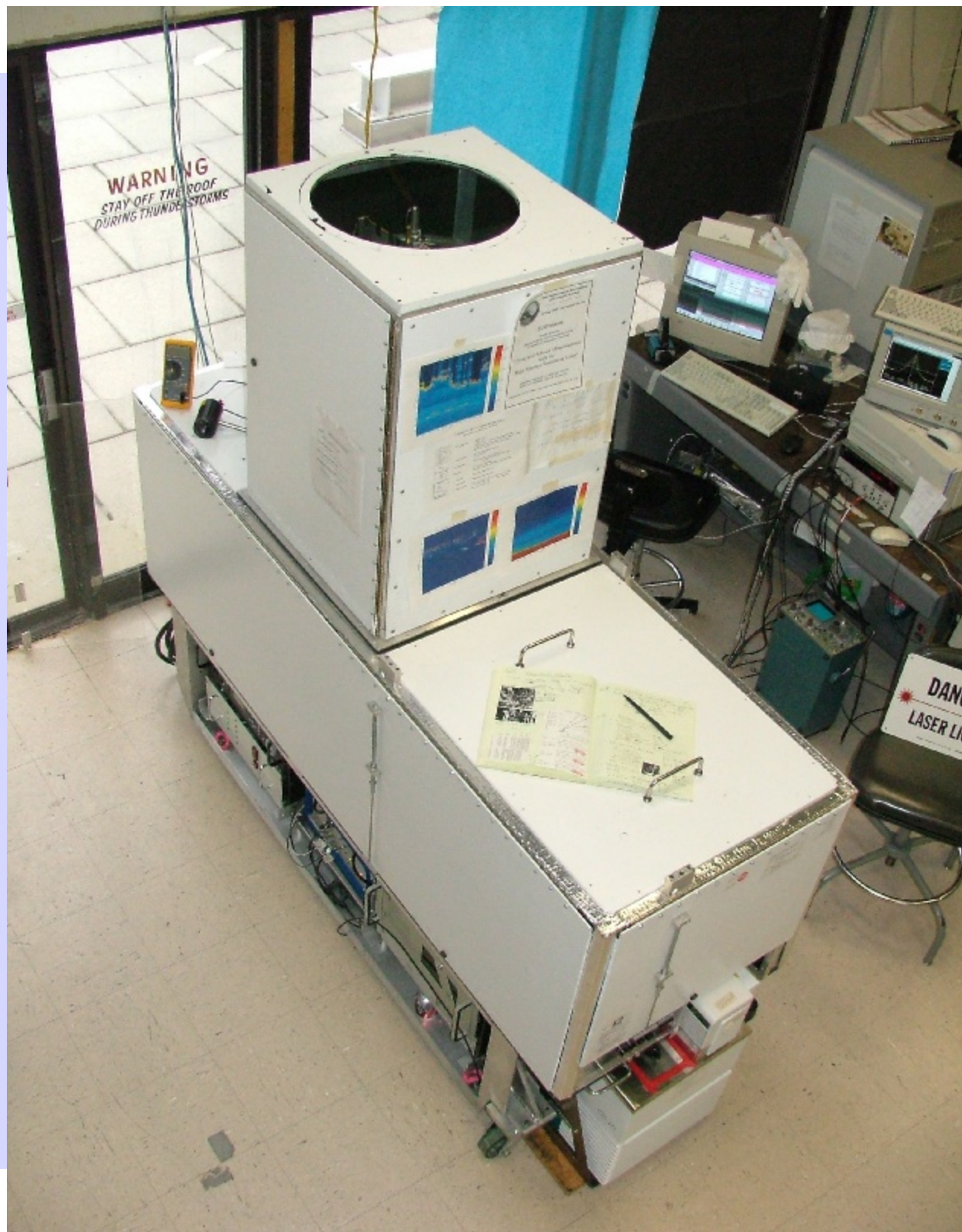
# High Spectral Resolution Lidar

Ed Eloranta

<http://lidar.ssec.wisc.edu>



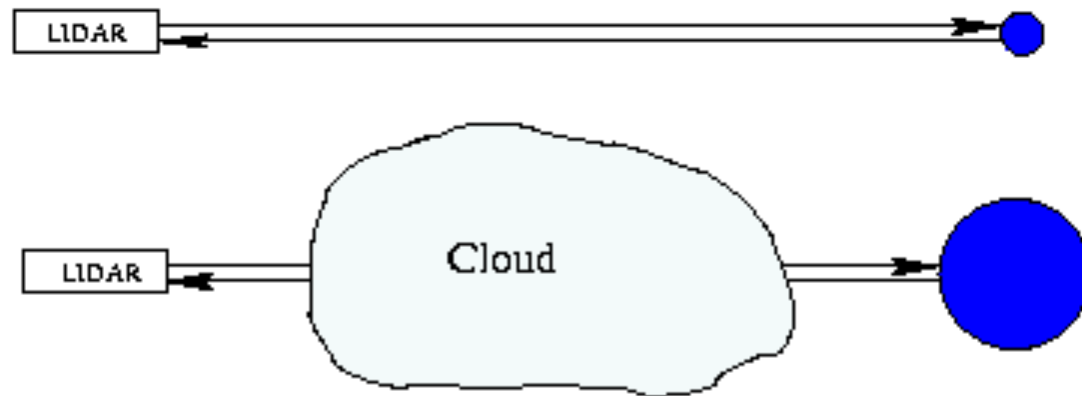








$$P(r) \sim \beta_s(r) \frac{\mathcal{P}(180, r)}{4\pi} \exp(-2 \int_0^r \beta_e(r) dr)$$



Traditional aerosol lidar can not distinguish between changes in target reflectivity and attenuation between the lidar and the target

The power,  $p_c(r)$ , received by a standard aerosol lidar where the scattering cross sections of aerosols,  $\beta_a(r)$ , and molecules,  $\beta_m(r)$ , both contribute:

$$p_c(r) \sim \frac{1}{r^2} \cdot \left( \frac{P(180,r)}{4\pi} \beta_a(r) + \frac{3}{8\pi} \beta_m(r) \right) \cdot \exp(-2 \int (\beta_a(r) + \beta_m(r)) \cdot dr)$$

If we can separate returns from aerosols,  $p_a(r)$ , and molecules,  $p_m(r)$ :

$$p_a(r) \sim \frac{1}{r^2} \cdot \frac{P(180,r)}{4\pi} \beta_a(r) \cdot \exp(-2 \int (\beta_a(r) + \beta_m(r)) \cdot dr) - \text{aerosol return,}$$

$$p_m(r) \sim \frac{1}{r^2} \cdot \frac{3}{8\pi} \beta_m(r) \cdot \exp(-2 \int (\beta_a(r) + \beta_m(r)) \cdot dr) - \text{molecular return}$$

where  $\frac{P(180,r)}{4\pi}$  is the backscatter phase function.

The backscatter ratio can be obtained from the ratio of these returns:

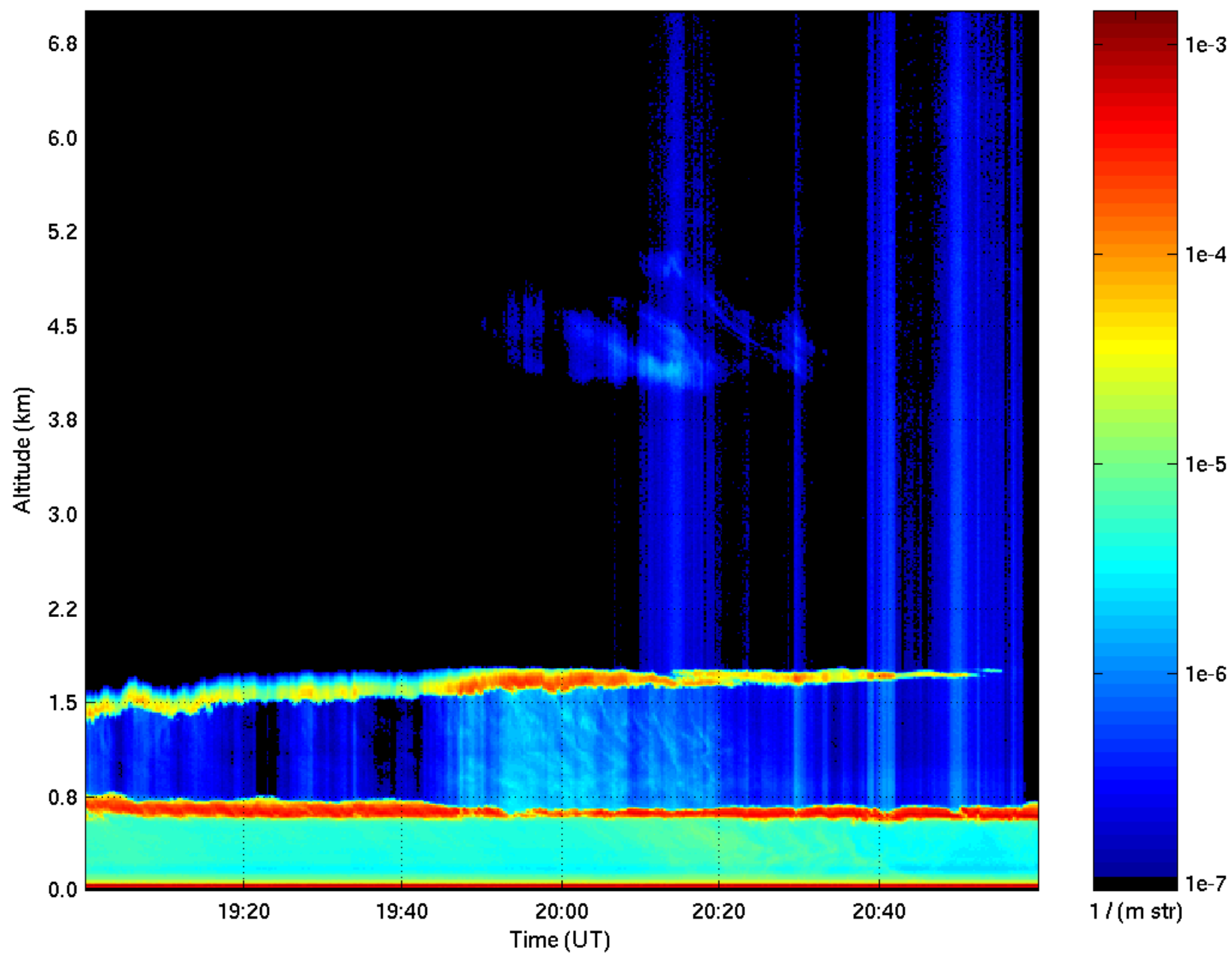
$$R(r) = \frac{p_a(r)}{p_m(r)} = \frac{\frac{P(180,r)}{4\pi} \cdot \beta_a(r)}{\frac{3}{8\pi} \cdot \beta_m(r)} \text{ where } \beta_m(r) \sim \text{atmospheric density profile, } \rho(r).$$

$$\beta'_a(r) = \frac{P(180,r)}{4\pi} \cdot \beta_a(r) = \frac{3}{8\pi} \cdot \beta_m(r) \cdot \frac{p_a(r)}{p_m(r)}$$

The optical depth between  $r_1$  and  $r_2$  is derived by comparing the molecular return to that expected from a purely molecular atmosphere:

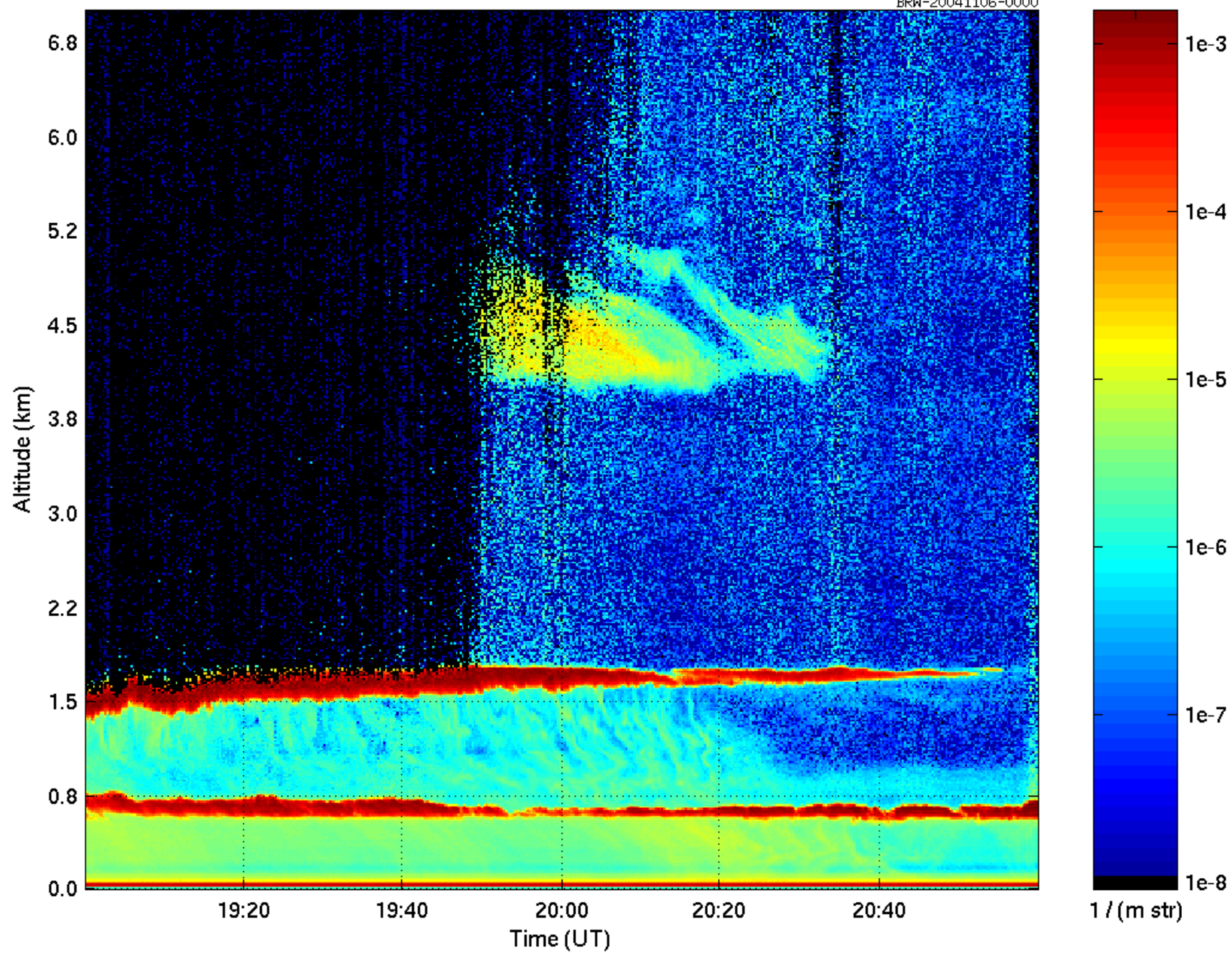
$$\tau(r_1, r_2) = \frac{1}{2} \cdot \log\left(\frac{r_1^2 \rho(r_2) \cdot p_m(r_1)}{r_2^2 \rho(r_1) \cdot p_m(r_2)}\right)$$

Attenuated backscatter ( $\text{m}^{-1}\text{str}^{-1}$ ) 05-Nov-2004

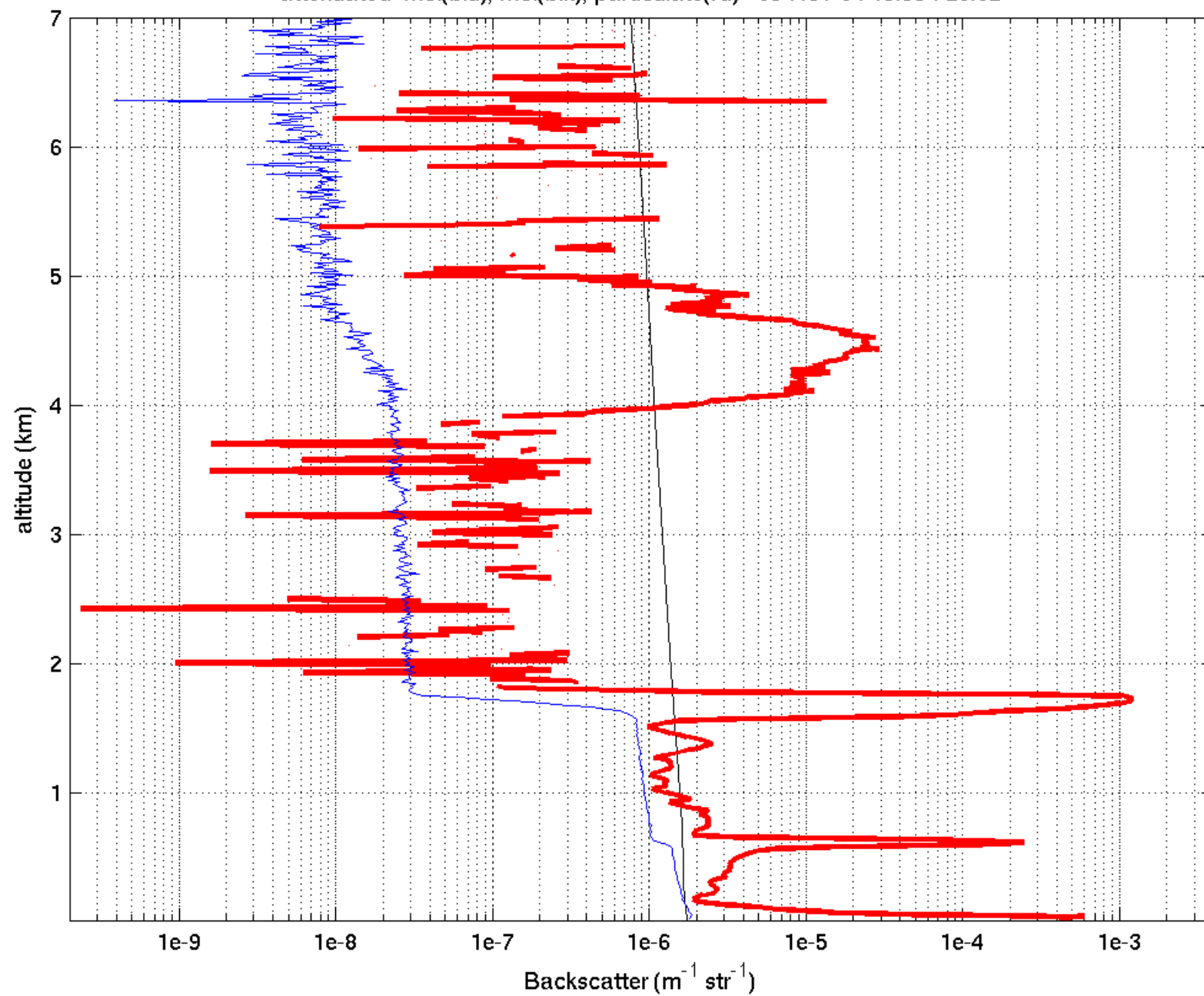


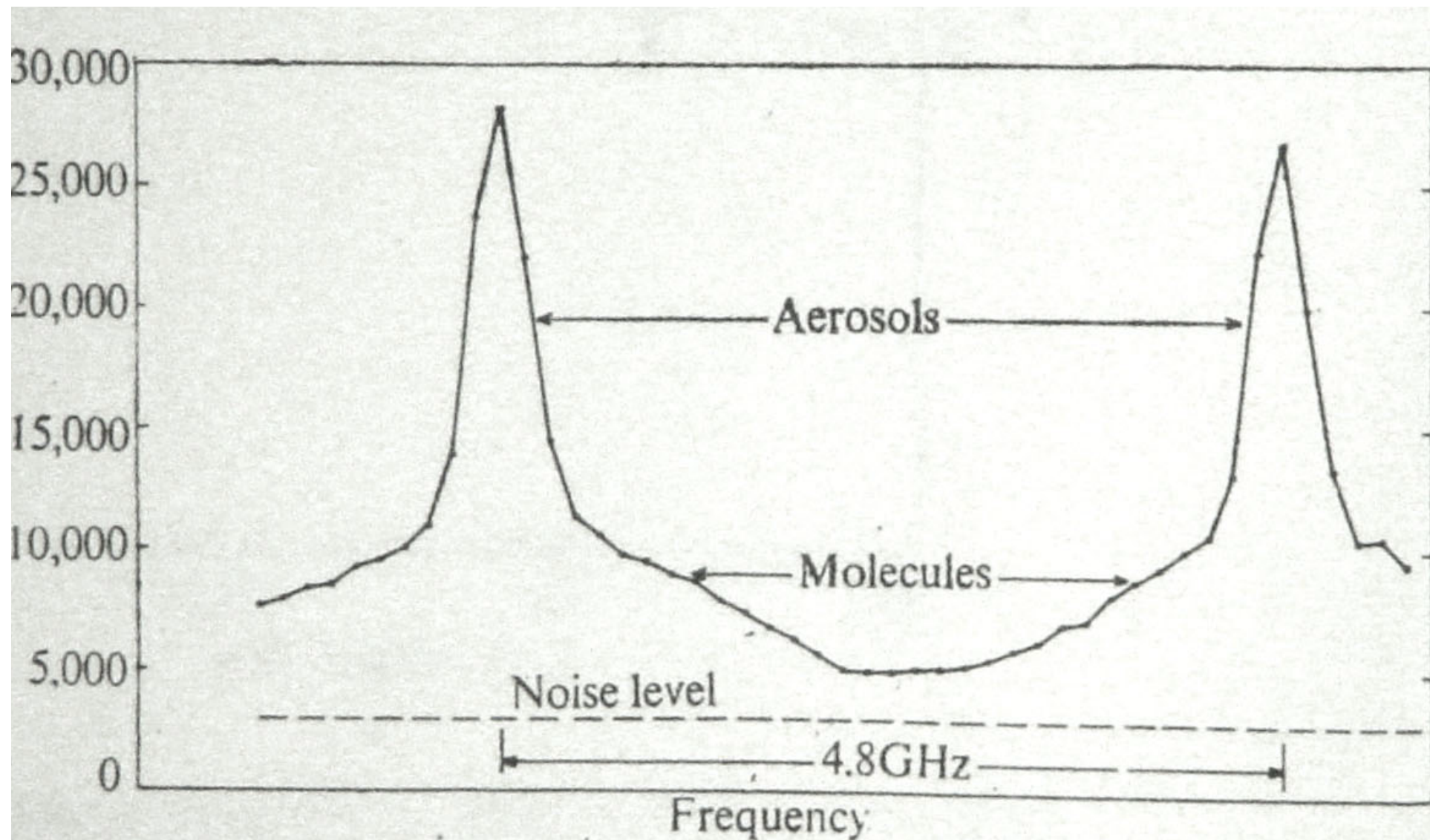
Aerosol backscatter cross section  $\text{m}^{-1} \text{str}^{-1}$  05-Nov-2004

BRW-20041106-0000



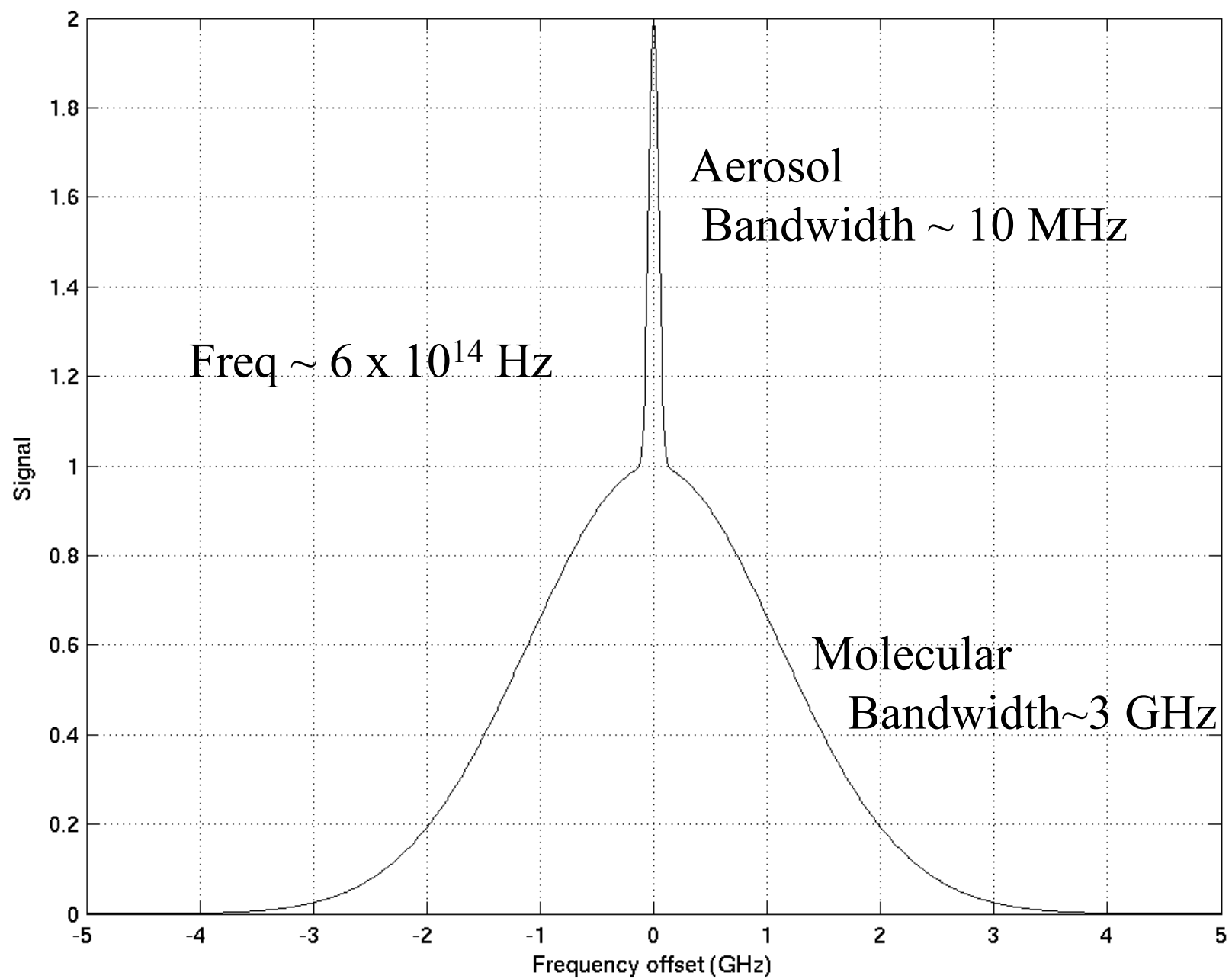
attenuated mol(blu), mol(blk), particulate(rd) 05-Nov-04 19:59->20:02

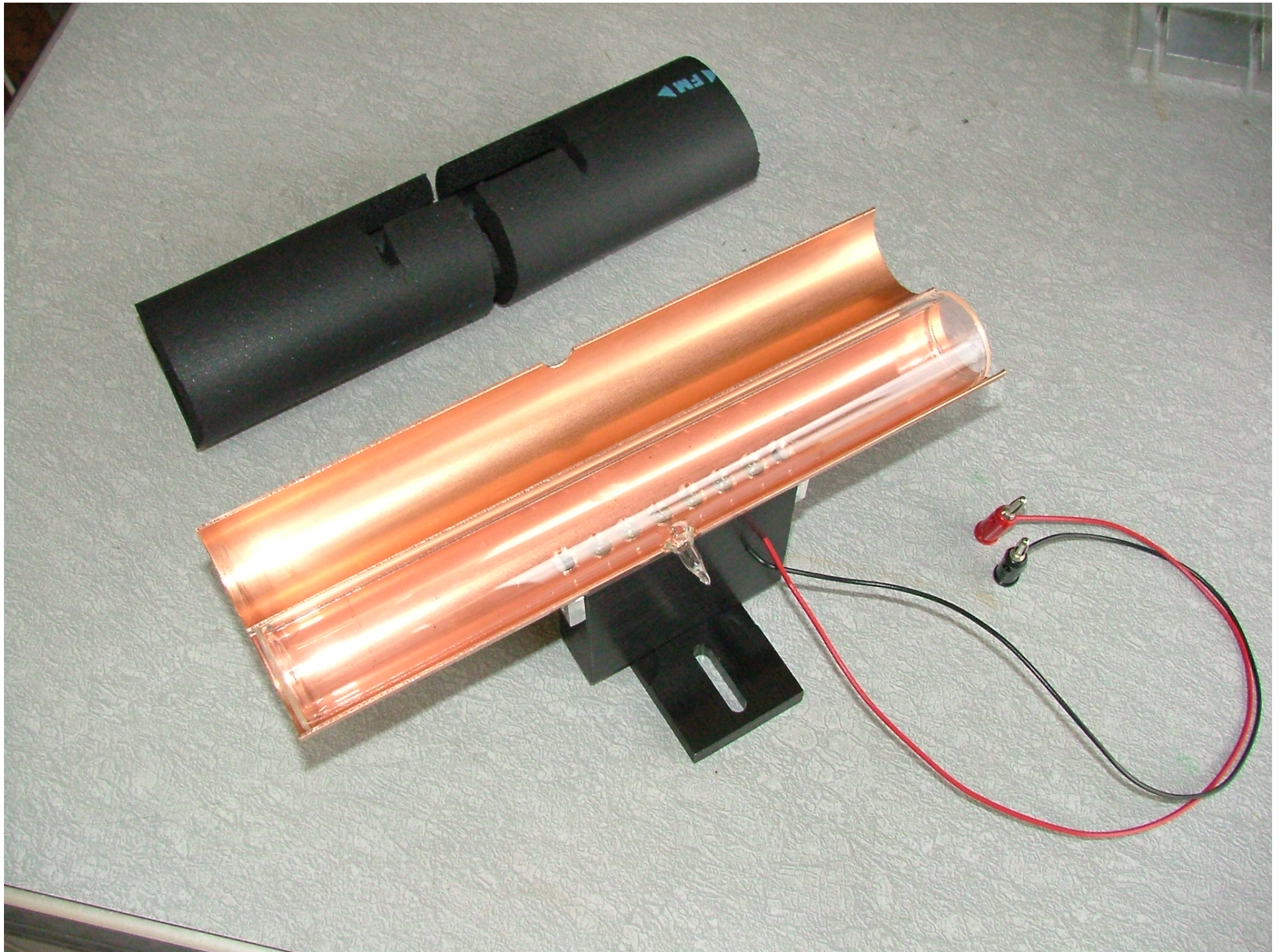




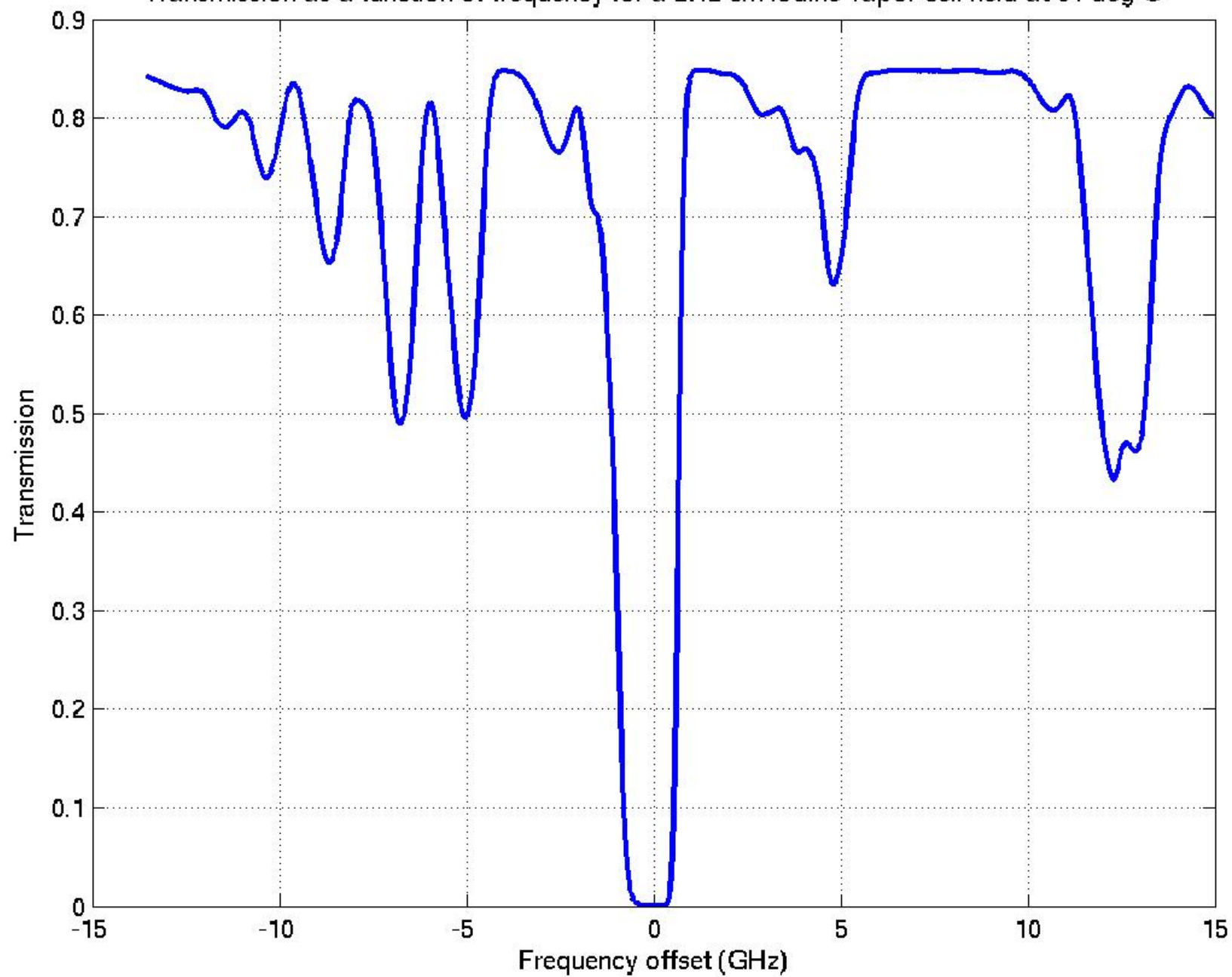
**Fig. 1** Spectrum of echoes from air. Contributions of molecules from aerosols can be separated.

Fiocco et al., Nature Physical Science, Vol. 229, Jan 18, 1971, pp 78-79.

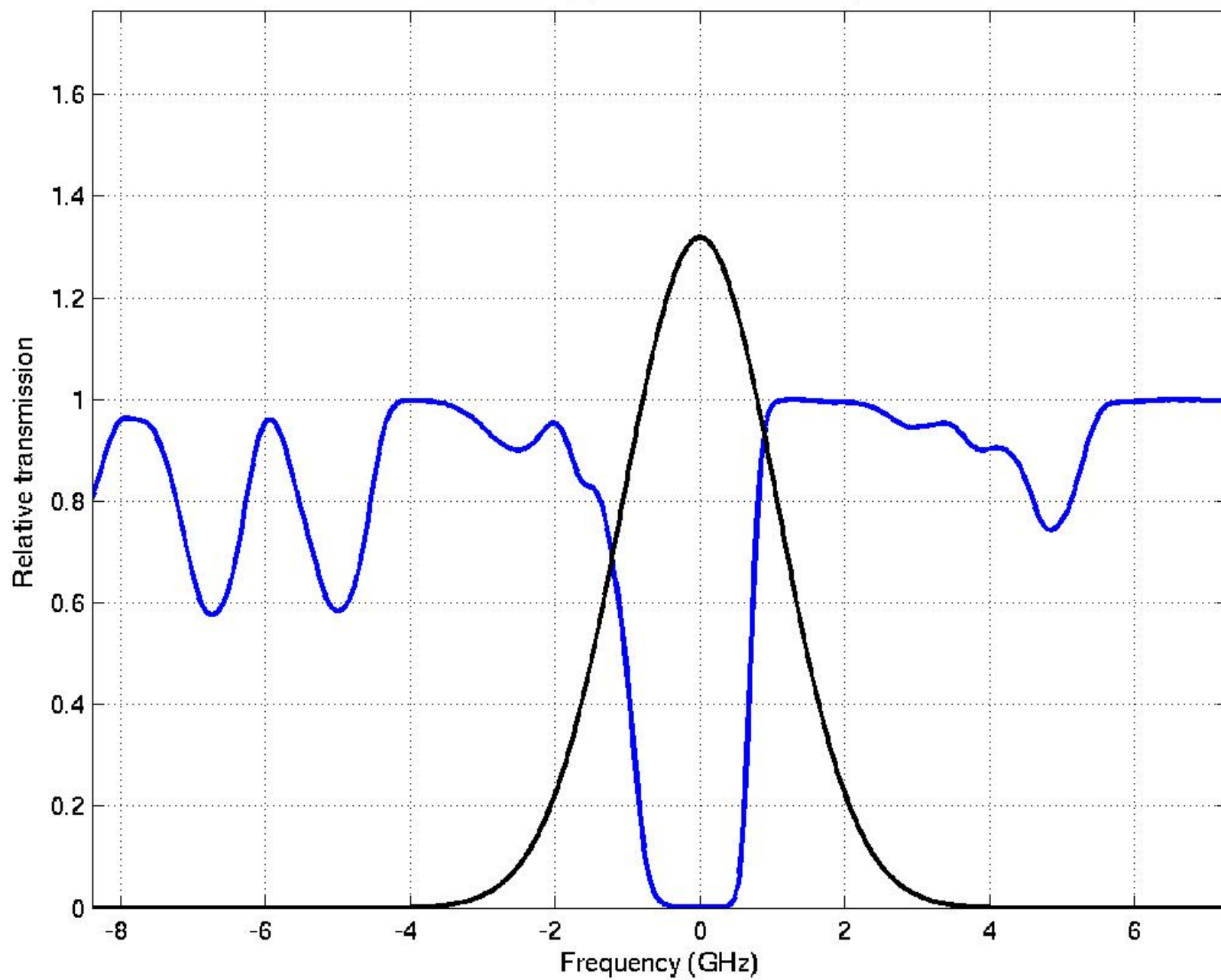


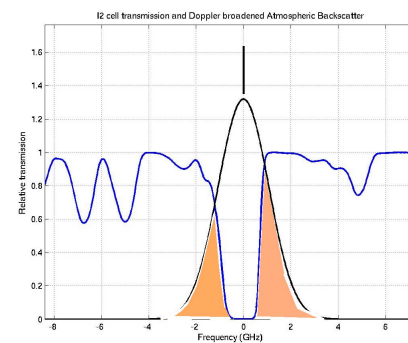
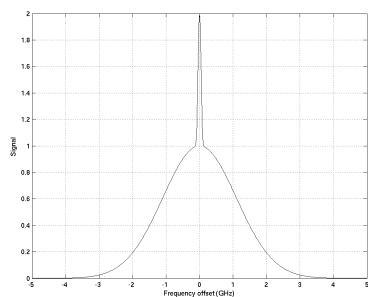
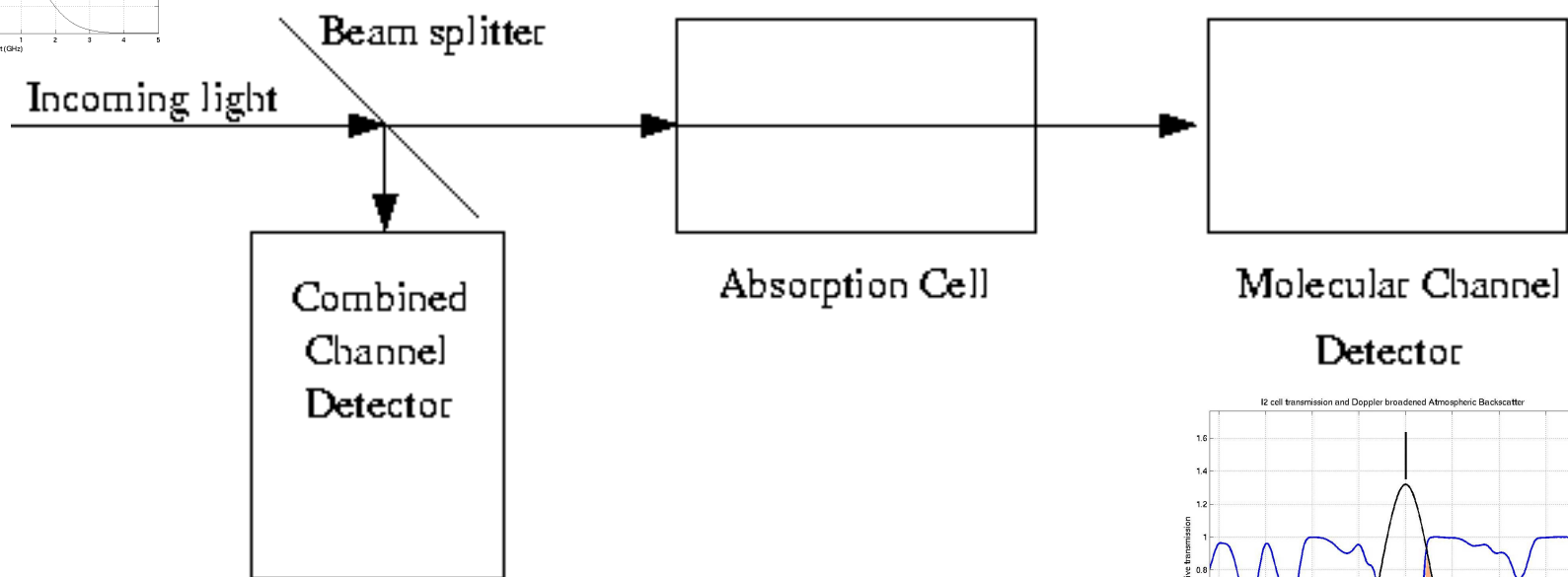
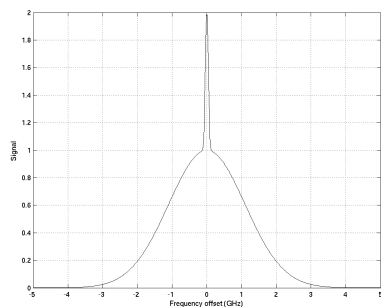


Transmission as a function of frequency for a 27.2 cm iodine vapor cell held at 31 deg C



12 cell transmission and Doppler broadened Atmospheric Backscatter





# Basic HSRL Equations

$S_c = G_{ac}N_a + G_{mc}N_m$  ; eq 1—Signal in the combined channel

$S_m = G_{am}N_a + G_{mm}N_m$ ; eq 2—Signal in the molecular channel

Where  $G_{ik}$  are gains of the two channels when exposed to  $N_a$  aerosol and  $N_m$  molecular photons.

Solving for  $N_m$  and  $N_a$  yields:

$N_m = \frac{S_m/G_{am} - S_c/G_{ac}}{(G_{mm}/G_{am}) - (G_{mc}/G_{ac})}$ ; eq 3—Number of molecular photons incident as function of signals

$N_a = \frac{S_c/G_{mc} - S_m/G_{mm}}{(G_{ac}/G_{mc}) - (G_{am}/G_{mm})}$ ; eq 4—Number of aerosol photons incident as function of signals

With  $G_{ac}$  =gain of the combined channel when exposed to aerosol photons

Define other gains relative to  $G_{ac}$ :

$$G_{mc} = C_{mc} \cdot G_{ac}, G_{am} = C_{am} \cdot G_{ac}, G_{mm} = C_{mm} \cdot G_{ac}$$

$$N_m = (1/G_{ac}) \cdot \frac{S_m/C_{am} - S_c}{(C_{mm}/C_{am}) - C_{mc}} = (1/G_{ac}) \cdot \frac{S_m - C_{am}S_c}{C_{mm} - C_{mc}C_{am}}$$

$$N_a = (1/G_{ac}) \cdot \frac{S_c/C_{mc} - S_m/C_{mm}}{(1/C_{mc}) - (C_{am}/C_{mm})} = (1/G_{ac}) \cdot \frac{C_{mm}S_c - C_{mc}S_m}{C_{mm} - C_{mc}C_{am}}$$

The scattering ratio is then:

$$\frac{N_a}{N_m} = \frac{C_{mm}S_c - C_{mc}S_m}{S_m - C_{am}S_c}$$

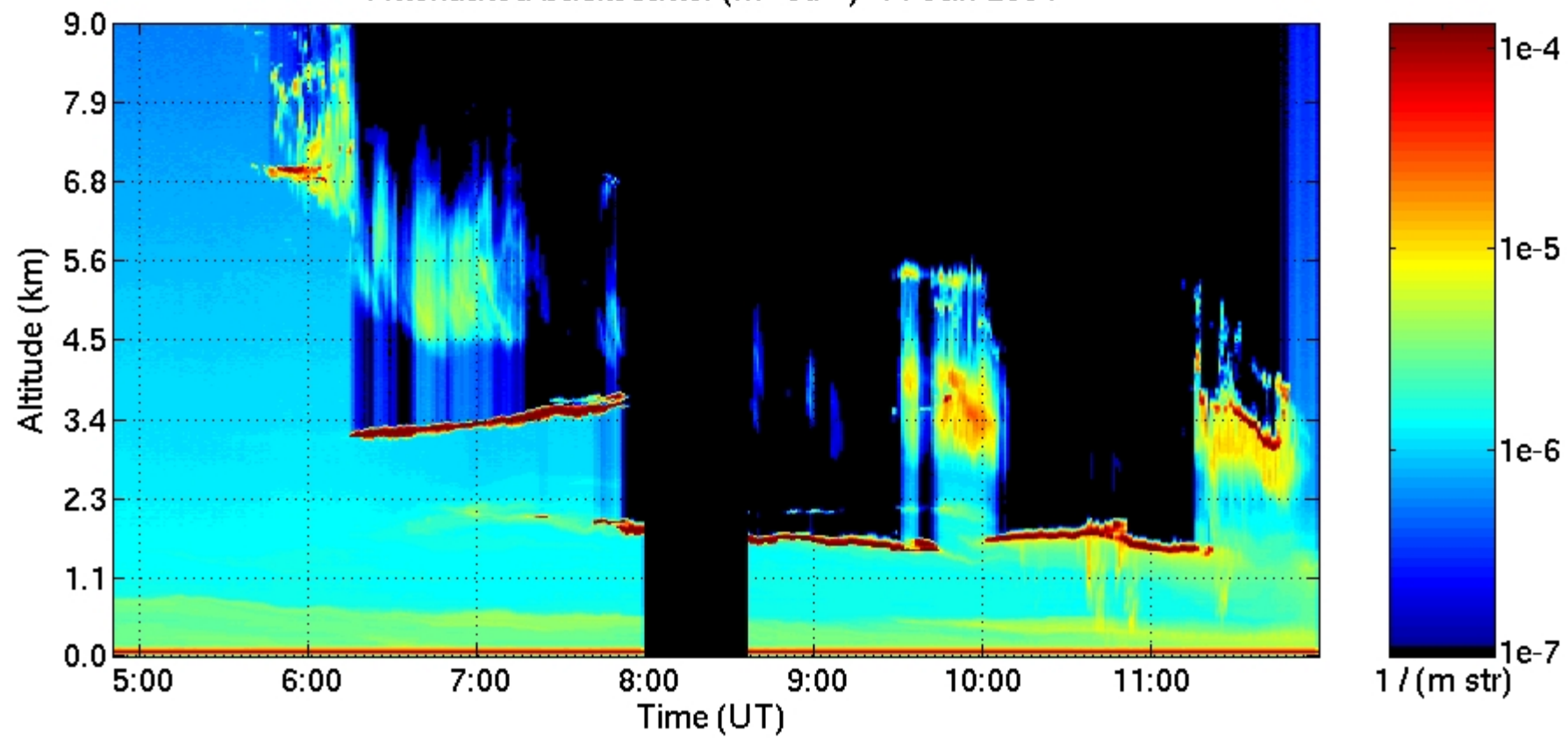
The backscatter cross section,  $\beta'_a$ , is:

$$\beta'_a(r) = \beta_a(r) \cdot \frac{P(180,r)}{4\pi} = \frac{N_a(r)}{N_m(r)} \cdot \beta_m(r), \text{ where } \beta_a = \text{scattering cross section, } \frac{P(180,r)}{4\pi} = \text{backscatter phase function.}$$

the optical depth,  $\tau$ , between two points  $r_1$  and  $r_2$  is:

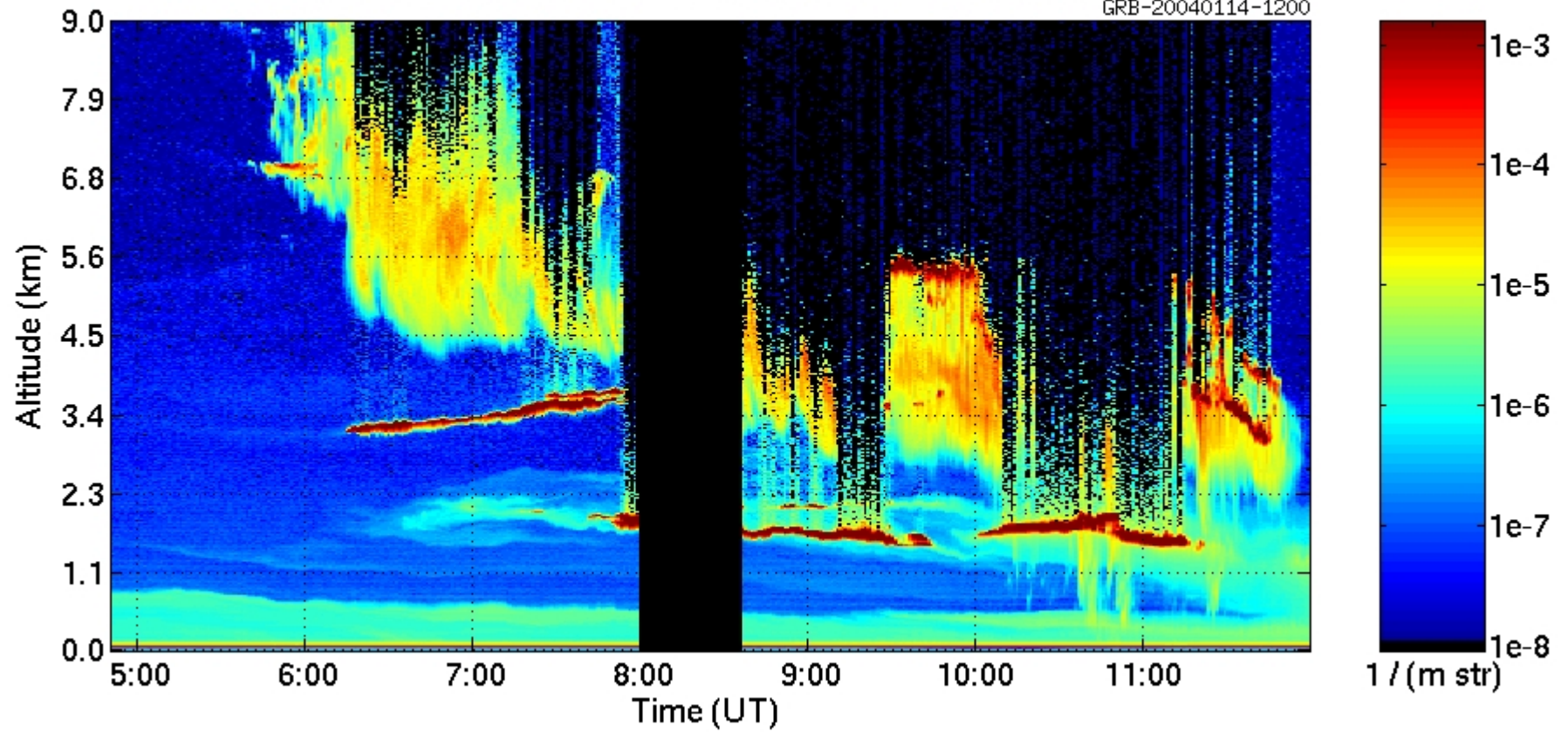
$$\tau(r_2 - r_1) = \frac{1}{2} \cdot \log\left(\frac{r_1^2 \rho(r_2) \cdot N_m(r_1)}{r_2^2 \rho(r_1) \cdot N_m(r_2)}\right), \text{ where } \rho(r) = \text{the atmospheric density profile}$$

Attenuated backscatter ( $\text{m}^{-1} \text{str}^{-1}$ ) 14-Jan-2004

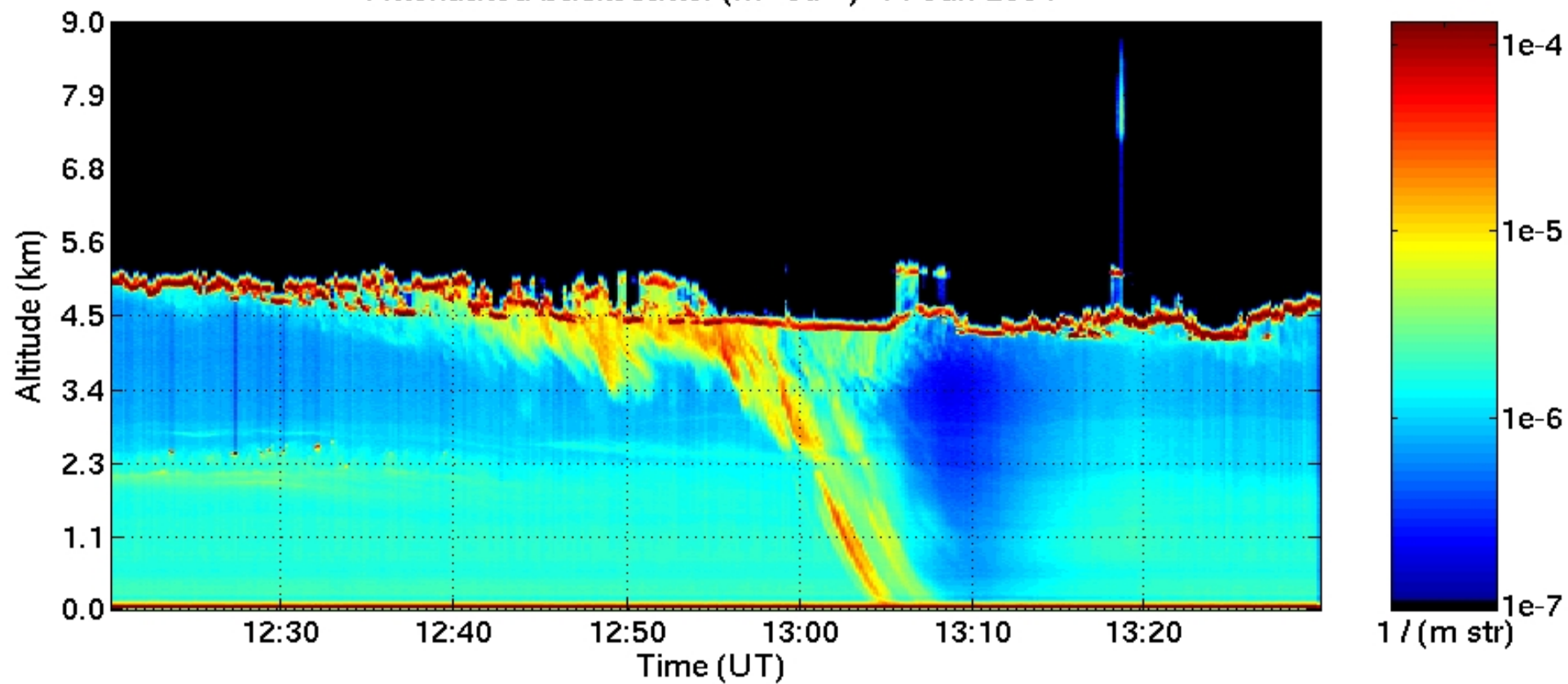


Aerosol backscatter cross section  $\text{m}^{-1}\text{str}^{-1}$  14-Jan-2004

GRB-20040114-1200

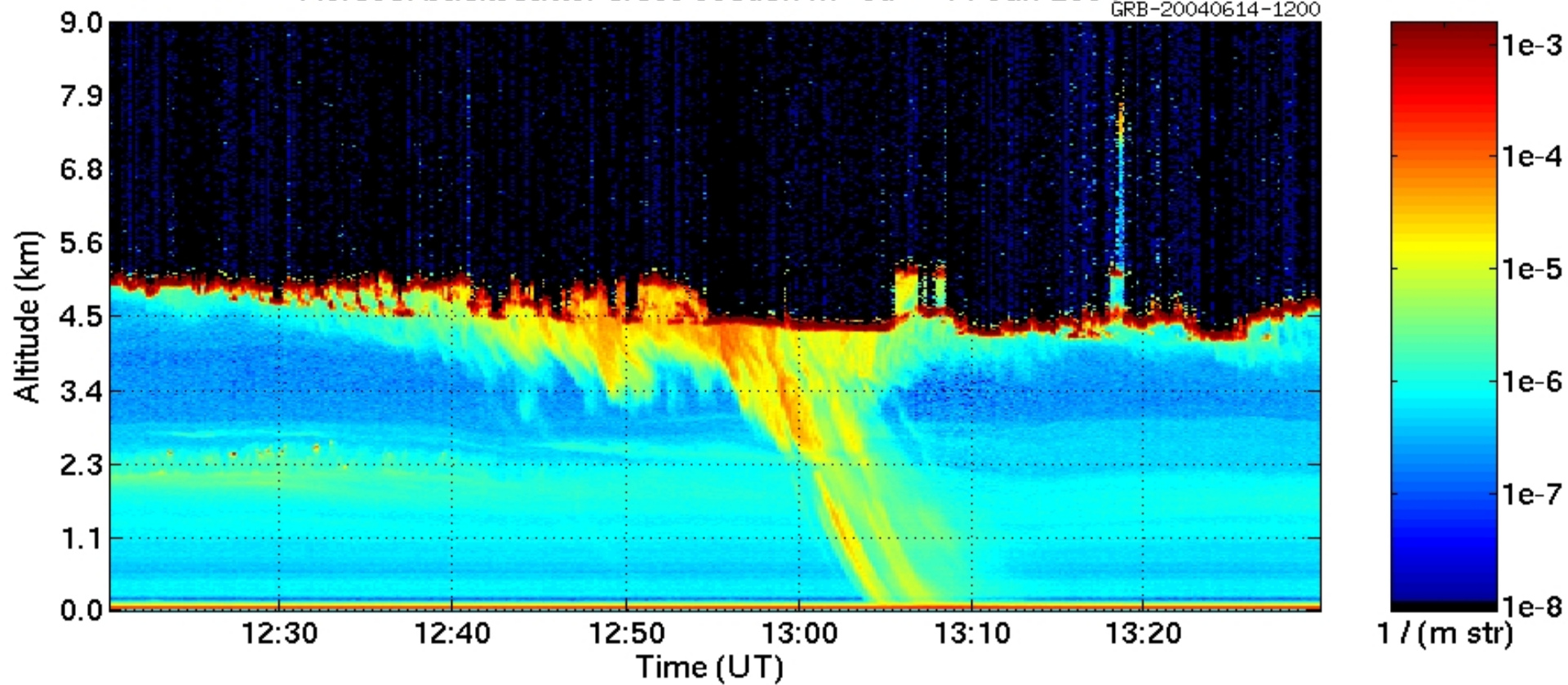


Attenuated backscatter ( $\text{m}^{-1} \text{str}^{-1}$ ) 14-Jun-2004



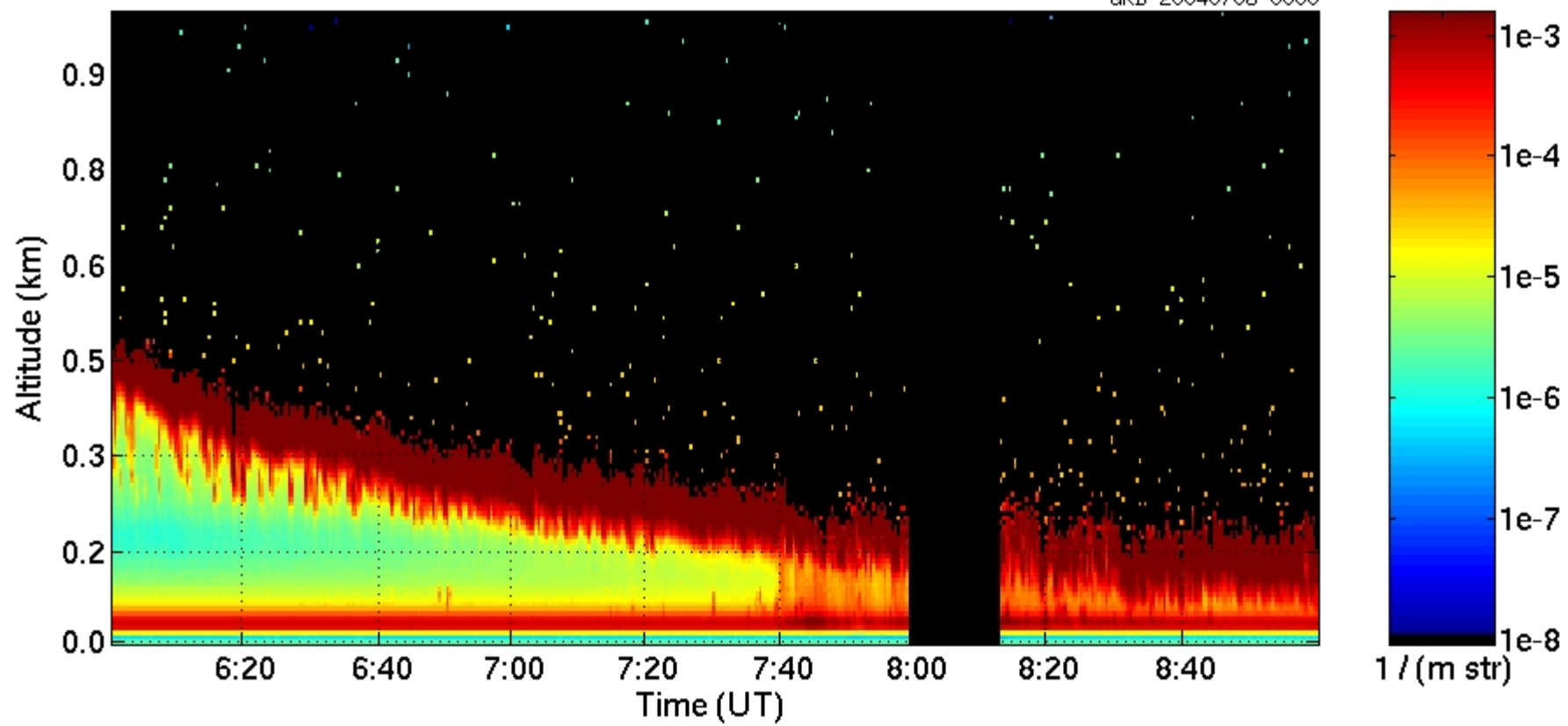
Aerosol backscatter cross section  $\text{m}^{-1} \text{str}^{-1}$  14-Jun-2004

GRB-20040614-1200

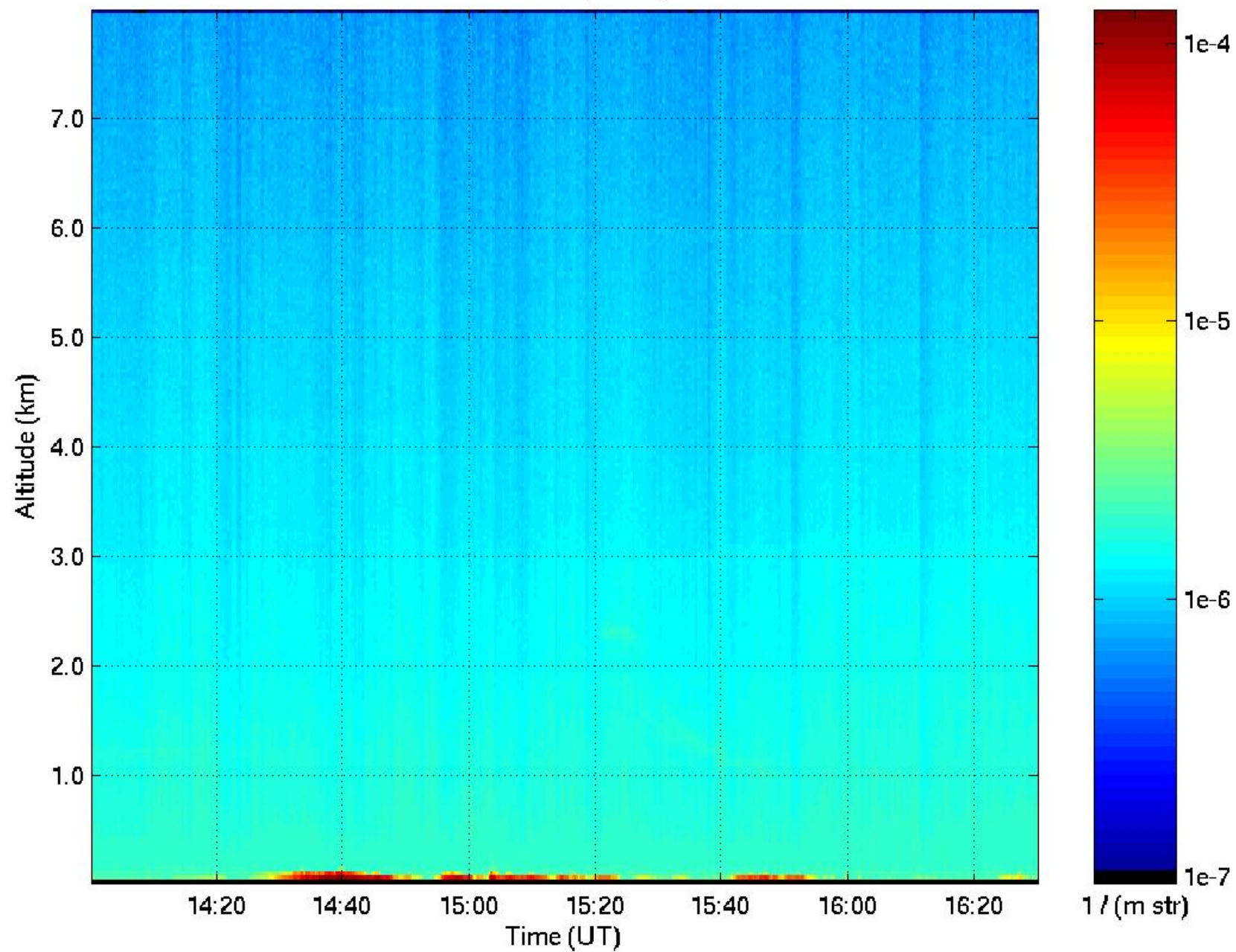


Aerosol backscatter cross section  $\text{m}^{-1} \text{str}^{-1}$  06-Jul-2004

GRB-20040706-0000

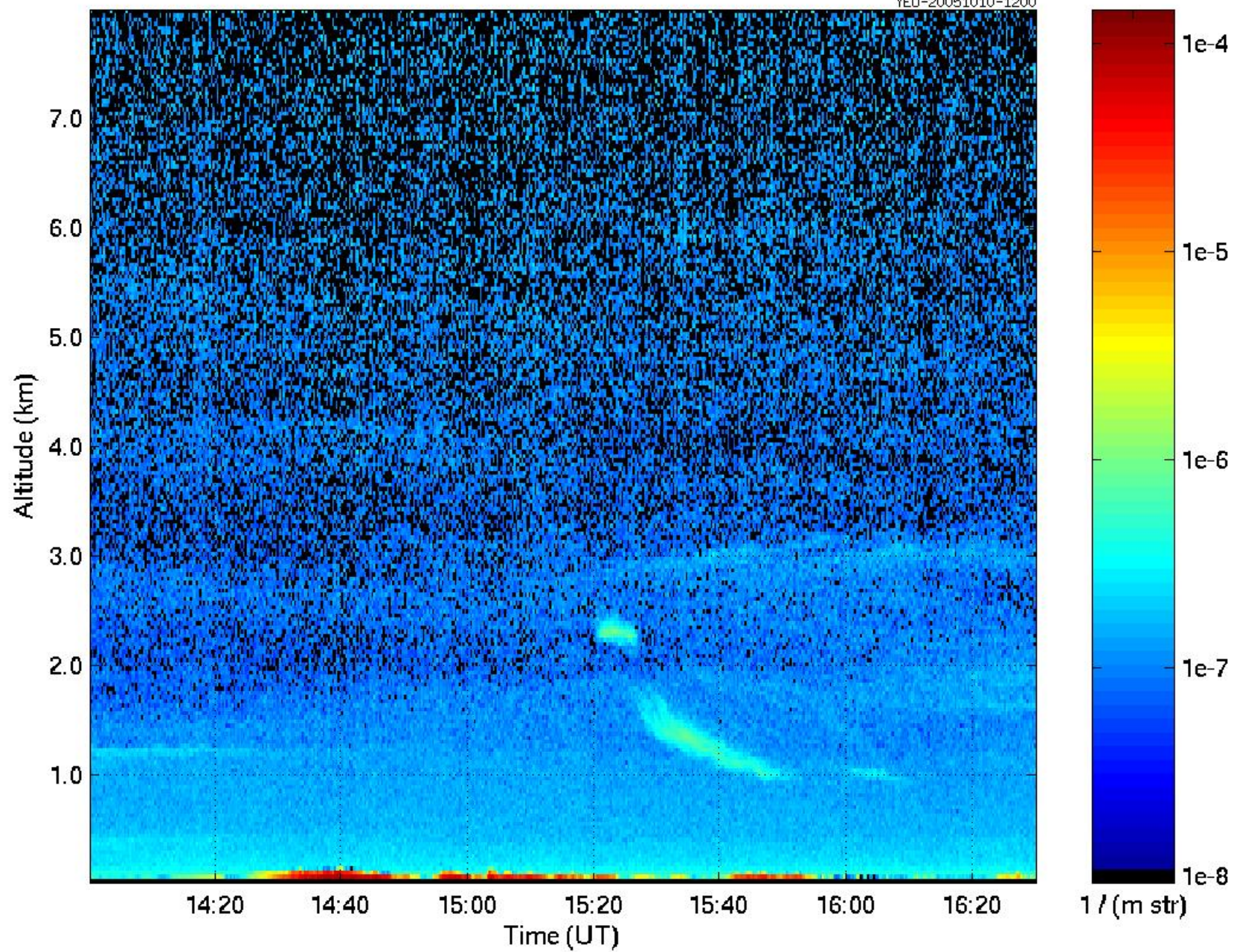


Attenuated backscatter ( $\text{m}^{-1}\text{str}^{-1}$ ) 10-Oct-2005

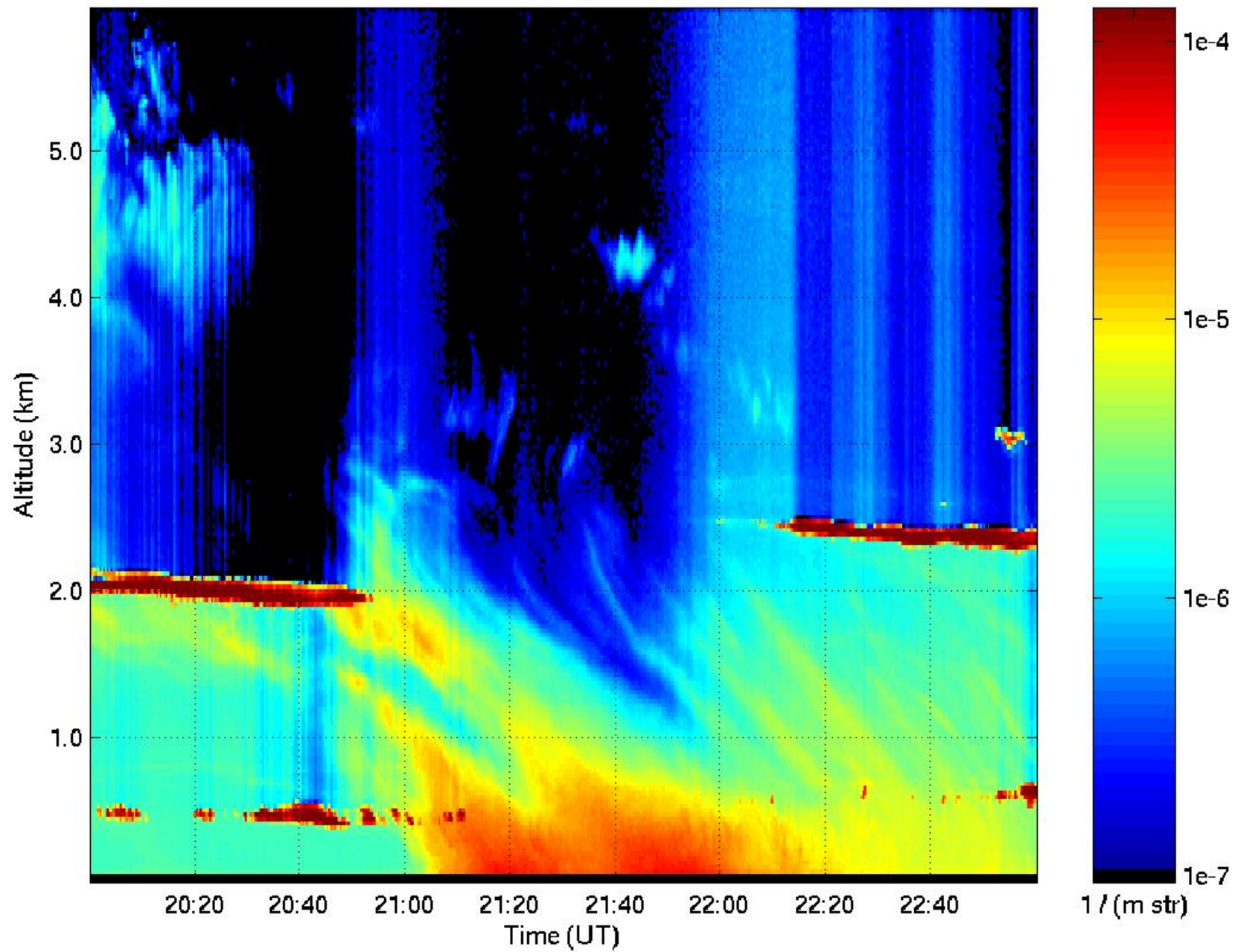


Aerosol backscatter cross section  $\text{m}^{-1}\text{str}^{-1}$  10-Oct-2005

YEU-20051010-1200

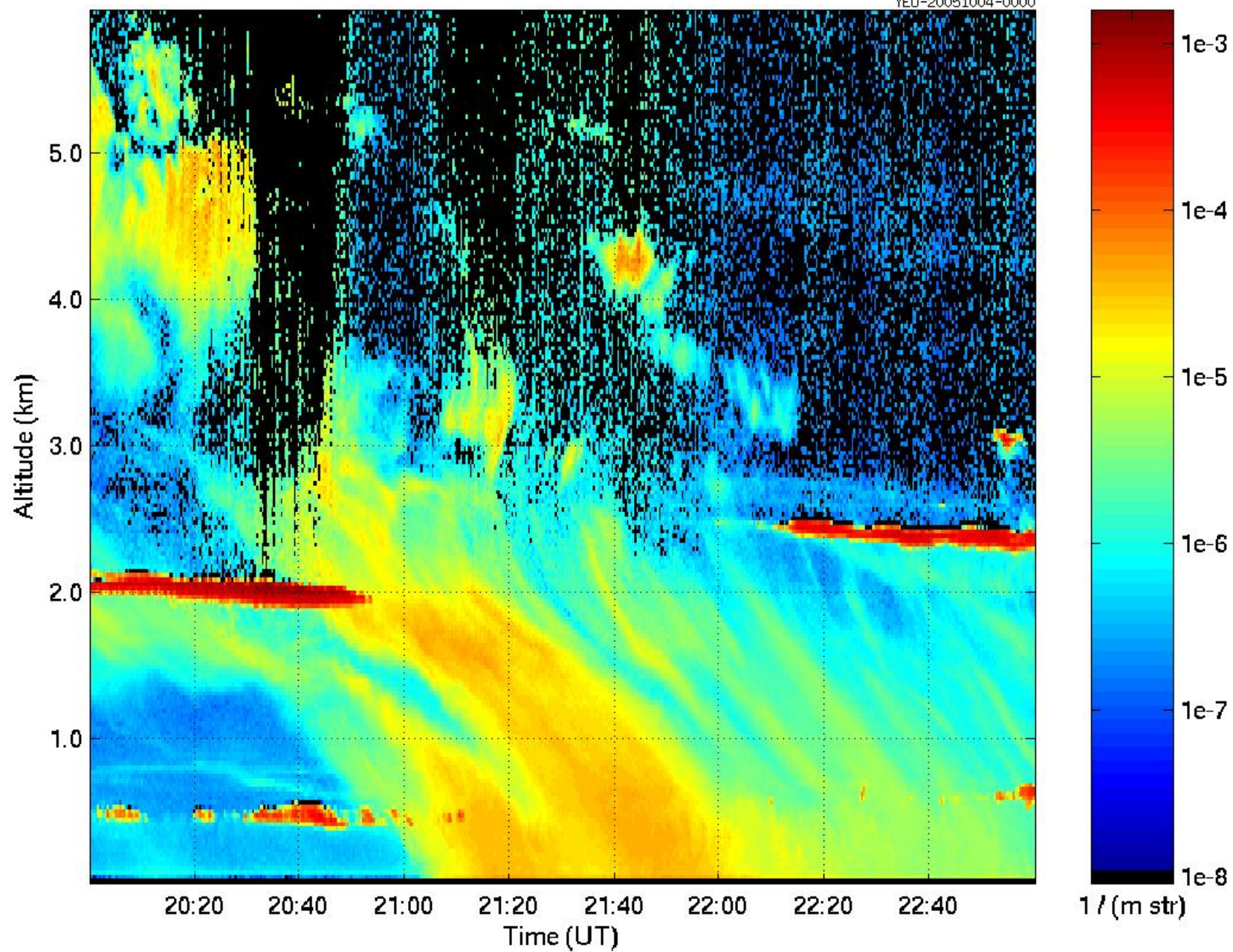


Attenuated backscatter ( $\text{m}^{-1}\text{str}^{-1}$ ) 03-Oct-2005



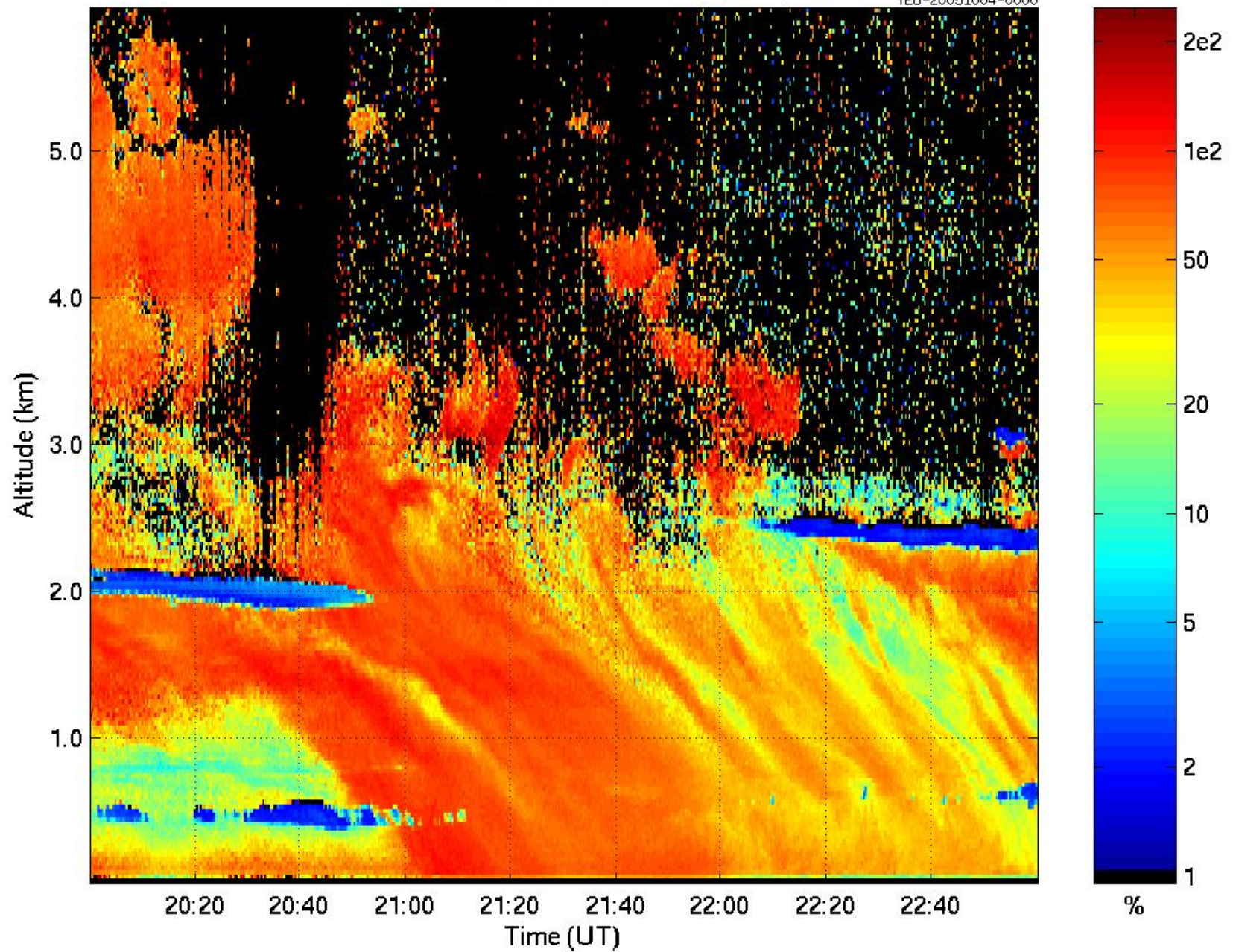
Aerosol backscatter cross section  $\text{m}^{-1}\text{str}^{-1}$  03-Oct-2005

YEU-20051004-0000

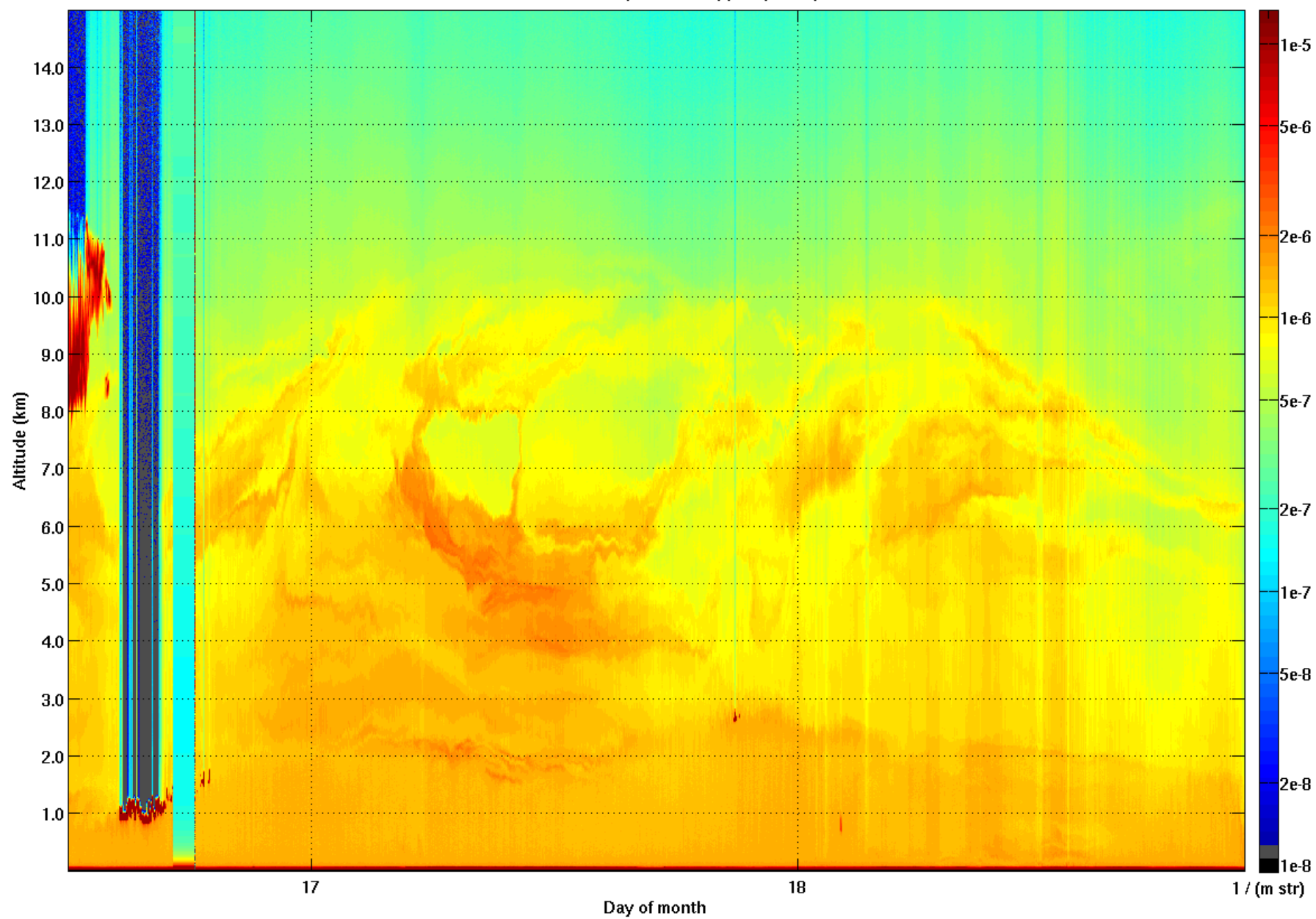


Particulate circular depolarization ratio(%) 03-Oct-2005

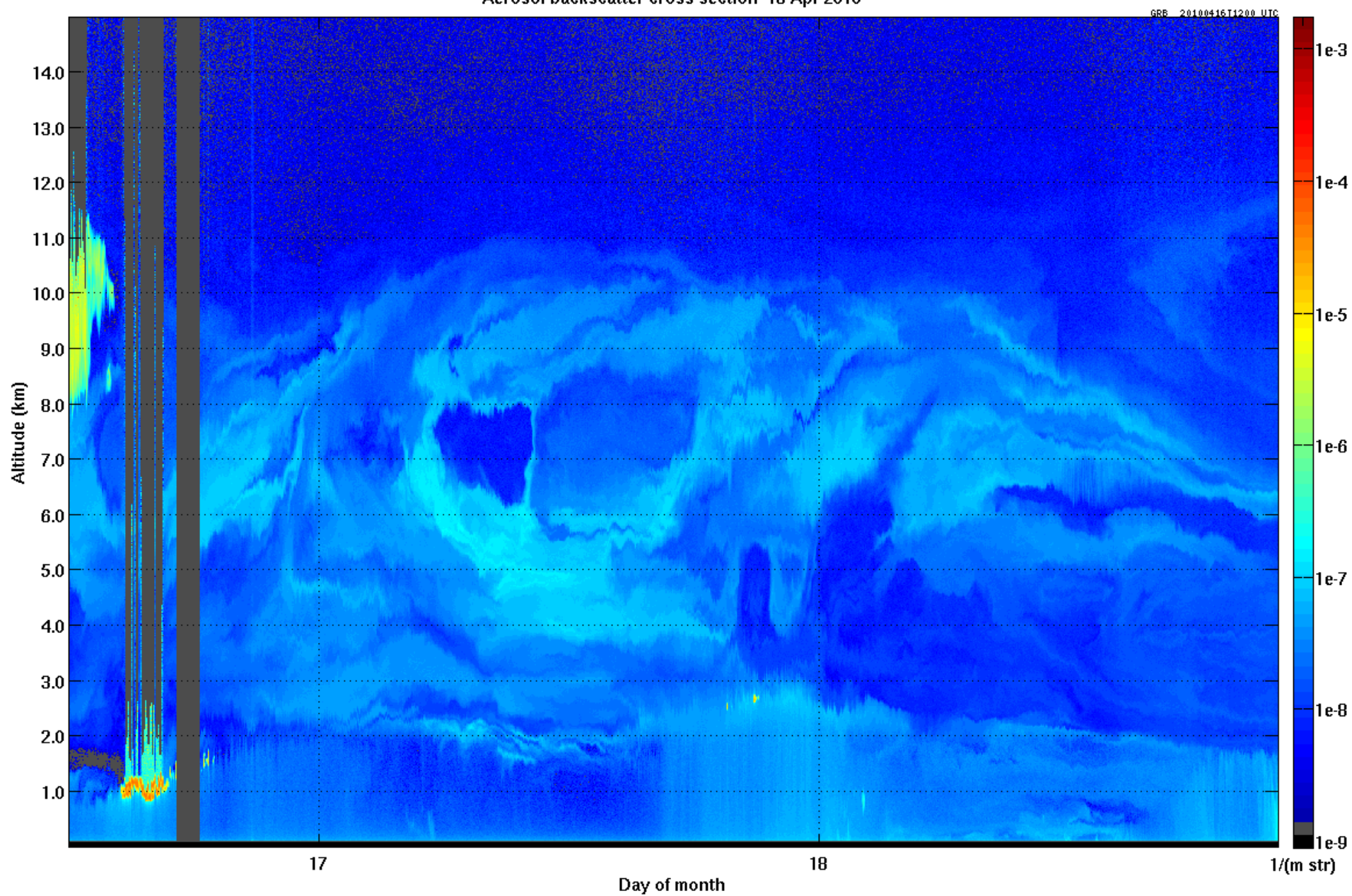
YEU-20051004-0000



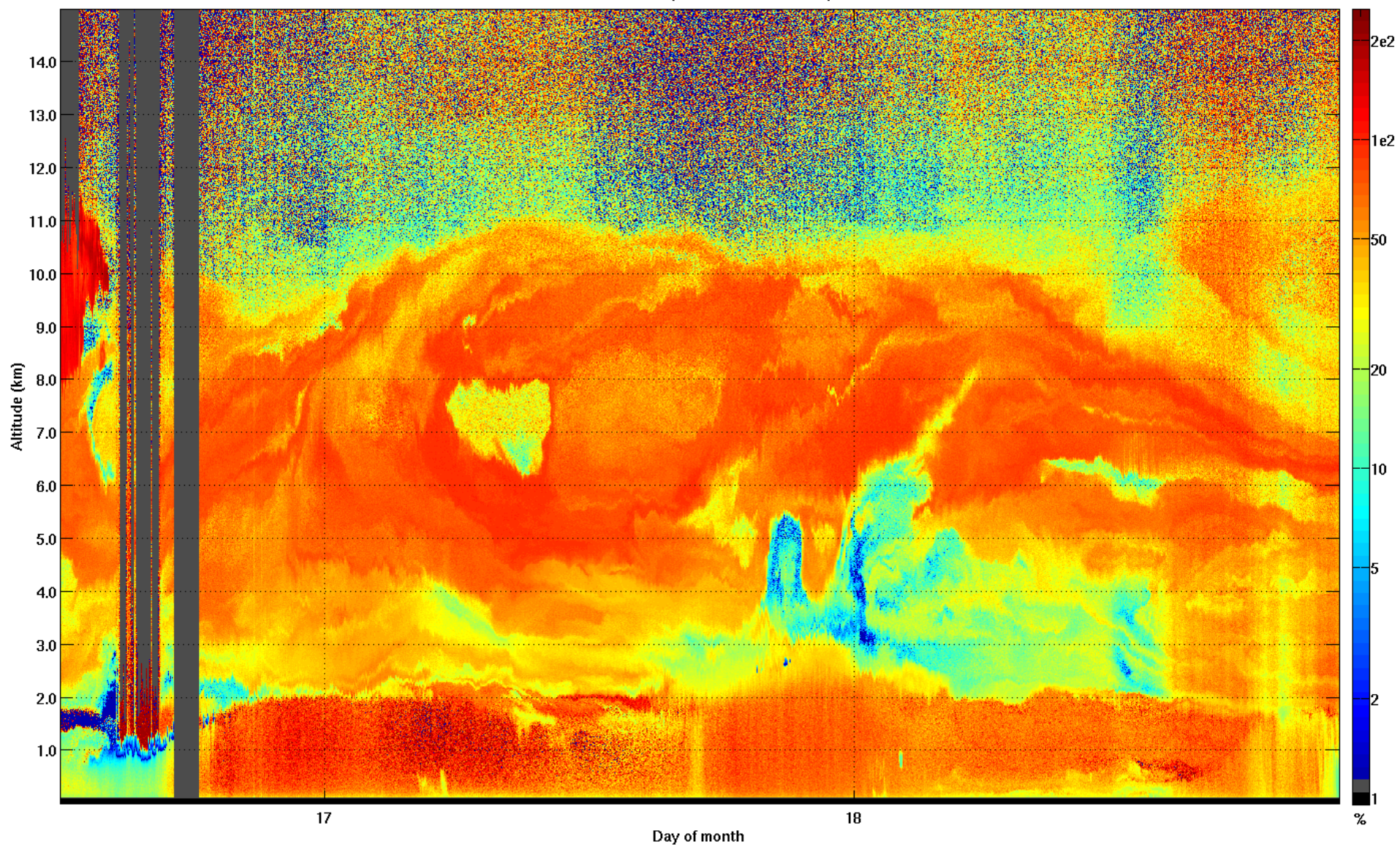
Attenuated backscatter (no masks applied) 16-Apr-2010



Aerosol backscatter cross section 16-Apr-2010



Particulate circular depolarization ratio 16-Apr-2010



## **Advantages of 532 nm operation**

- Iodine adsorption line for filtering
- Important wavelength for radiative transfer
- Allows use of doubled Nd:YAG laser
- Strong molecular scattering

## **Problem with 532 nm—eye safety**

- Wavelength region with smallest permitted exposure  
max single pulse exposure =  $5\text{e-}7 \text{ J/cm}^2$

## Eye safety

532 nm wavelength has smallest permitted exposure

$$\text{ANSI safe exposure} \leq 5 \times 10^{-7} (\text{PRF}/4)^{-1/4} \text{ J/cm}^2$$

Where PRF = the pulse repetition frequency

This forces high repetition rates and large apertures

Range ambiguity limits  $R < \sim 4\text{kHz}$ , i.e.  $r_{\text{max}} < \sim 40 \text{ km}$

Cost, complexity, turbulence limit aperture to  $\sim 0.5 \text{ m}$ .

Thus max transmitted energy laser pulse is limited to:

$$p_{25}^2 * 5 \times 10^{-7} * 1000^{-1/4} = 0.174 \text{ mJ/pulse}$$

and the maximum transmitted power is:

$$0.174 \times 10^{-3} * 4000 \text{ Hz} = 0.7 \text{ Watt}$$

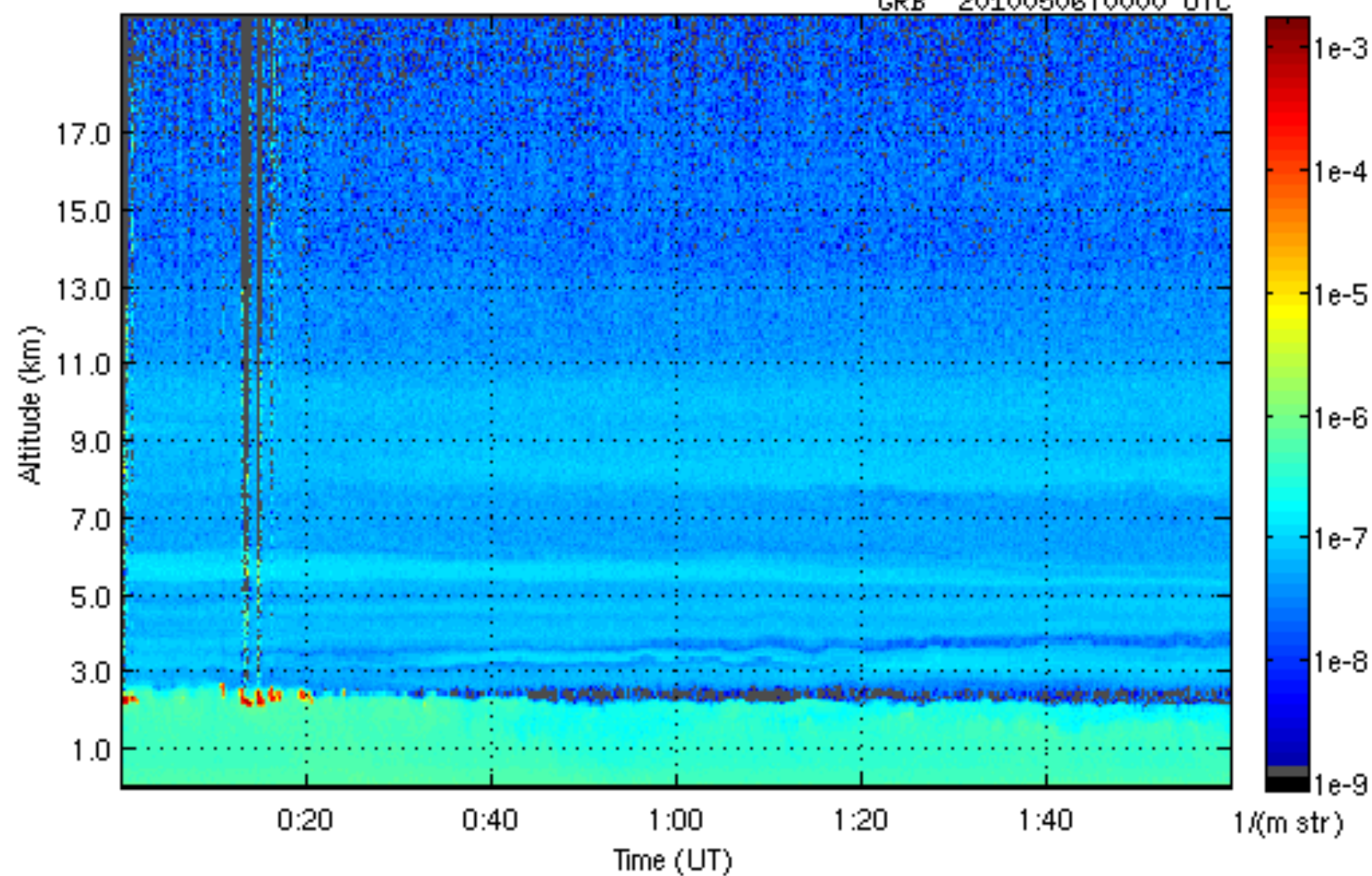
- Low energy laser pulses reduce the signal to noise ratio of the lidar  
small lidar returns must compete with scattered sunlight
- this forces
  - a small receiver acceptance angles (40-100 microradians)
  - a narrow spectral bandpass  $\sim 8$  GHz

# Arctic HSRL Specifications

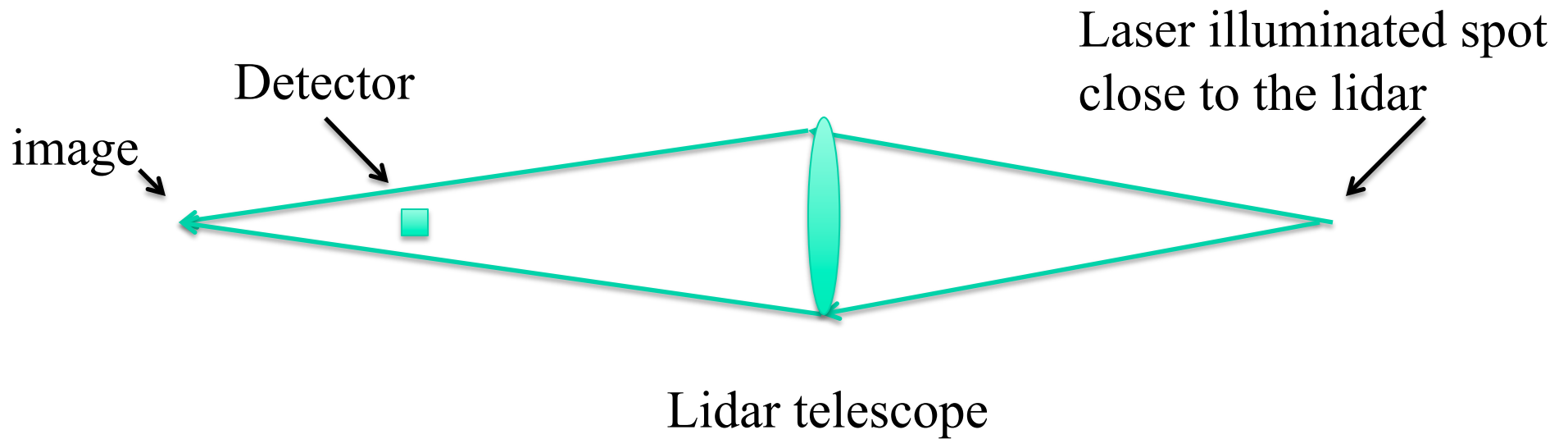
- Altitude coverage ~75m-->30 km
- Altitude resolution 7.5 m
- Time resolution :
  - -Backscatter, depolarization profiles 0.5 sec
  - -Optical depth profiles >20 sec
- Eye safe at output
- Wavelength 532 nm
- Power 200 → 600 mW
- Repetition rate 4 kHz
- Field of view 45 microradians
- Sky noise filter bandwidth 8 GHz
- Typical background noise/bin >1 photon/1000 laser pulses
- Receiver diameter 0.4 m
- I2 filter bandwidth 1.8 GHz

Aerosol backscatter cross section 06-May-2010

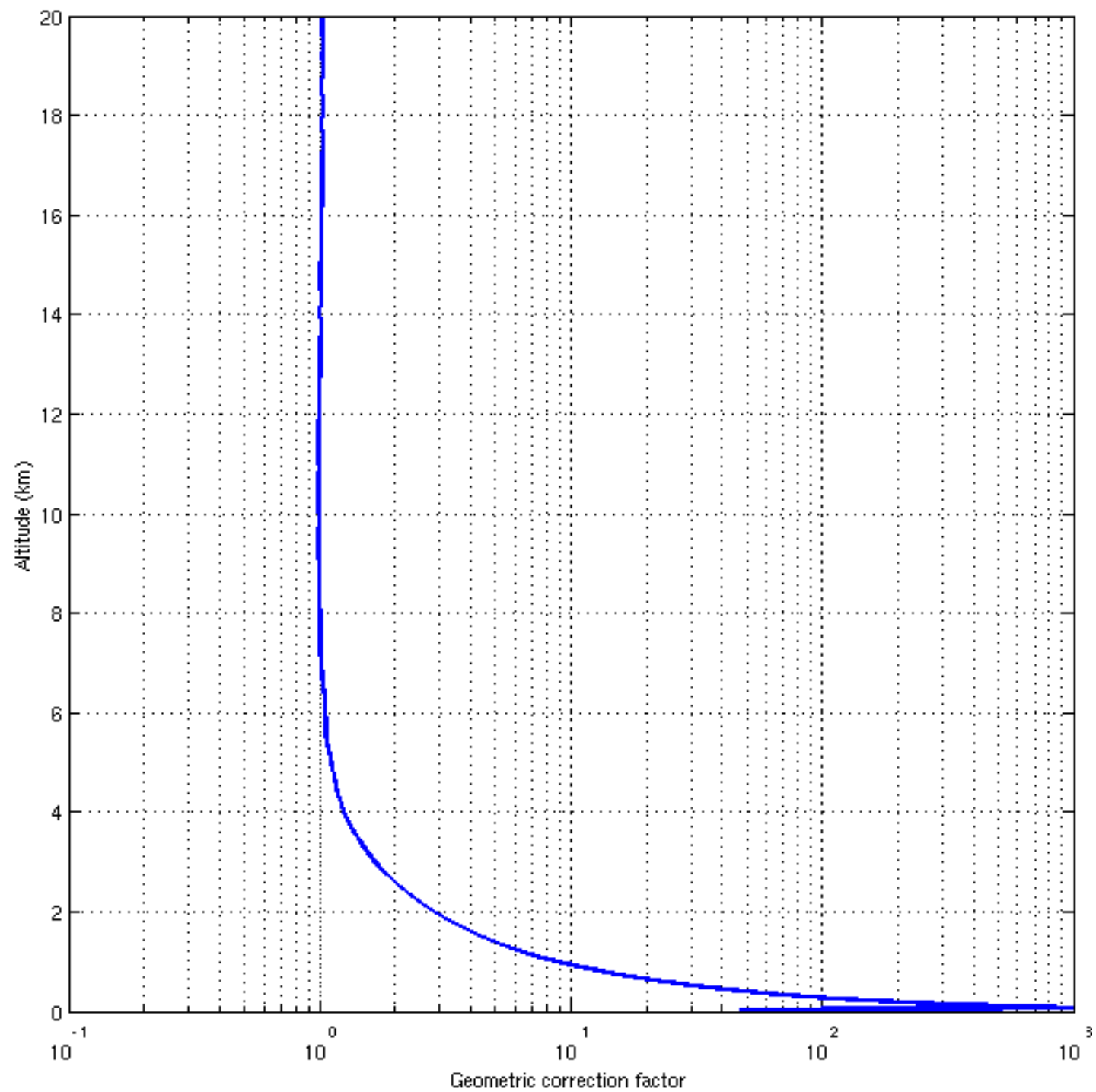
GRB 20100506T0000 UTC



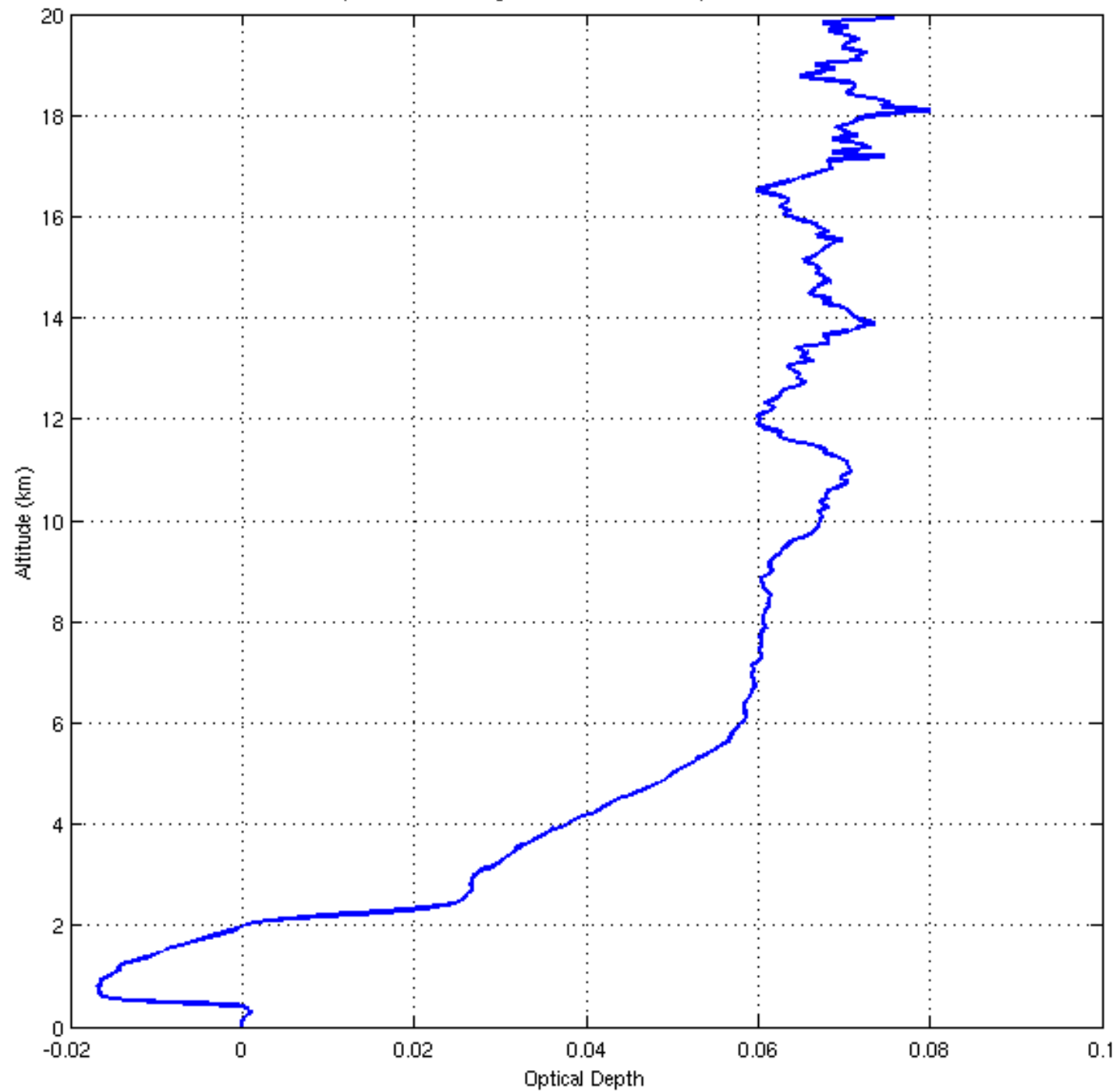
Geometric correction --- overlap correction



A lidar with a small field-of-view will require a large geometric correction at close range because the out of focus image becomes much larger than the detector.



OD computed from average transmission 06-May-10 00:00 ---> 01:59



## Comparison between potential systems

### -- Raman

- scattering cross section  $\sim$  Rayleigh/1000
- requires high average power  $\sim 10$ 's W
- large diameter receiver, typically  $\sim 0.6$  m
- can accommodate larger FOV's
- relatively simple

### --I2 HSRL 532nm

- scattering cross section  $\sim$  Rayleigh/4
- lower average power  $\sim 0.5$  W
- somewhat smaller receiver  $\sim 0.4$  m
- can accommodate larger FOV's
- relatively complex

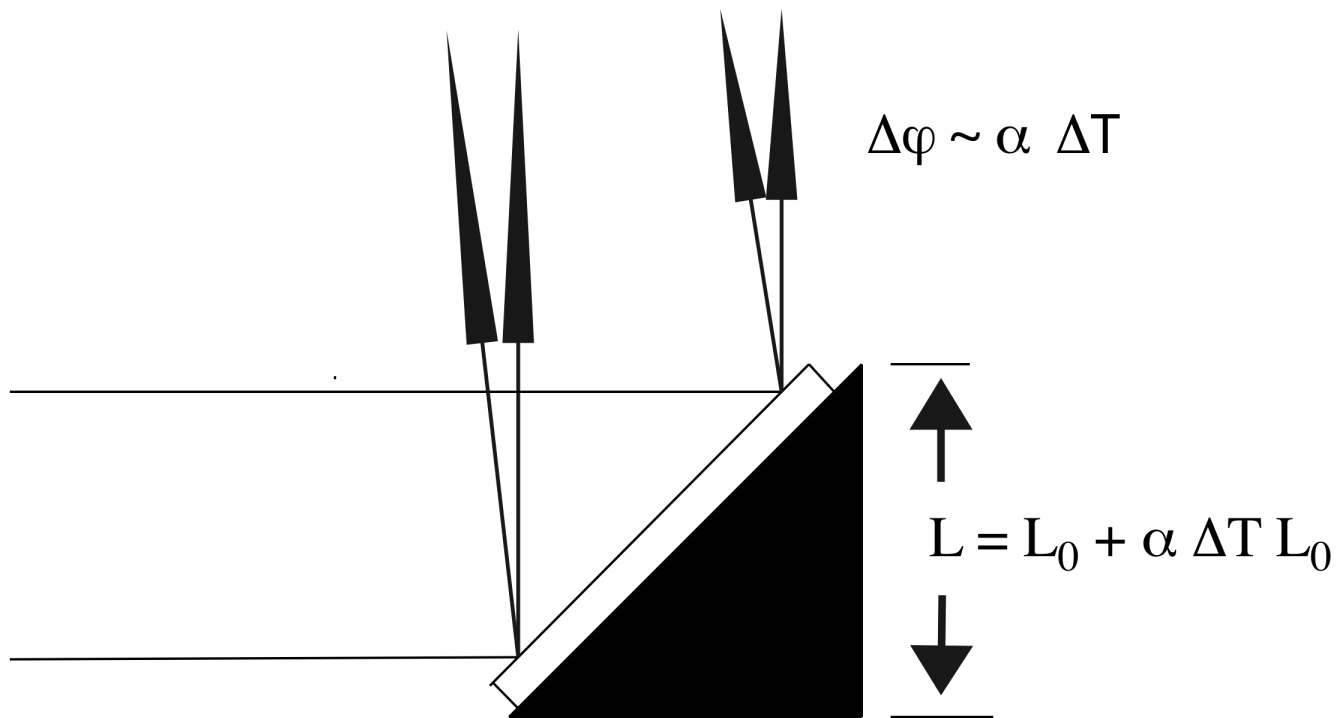
### --Fabry-Perot HSRL 355 nm

- larger cross section than 532nm
- more complex than I2
- field-of-view due to Fabry-Perot

HSRL data can be found at:  
<http://lidar.ssec.wisc.edu>



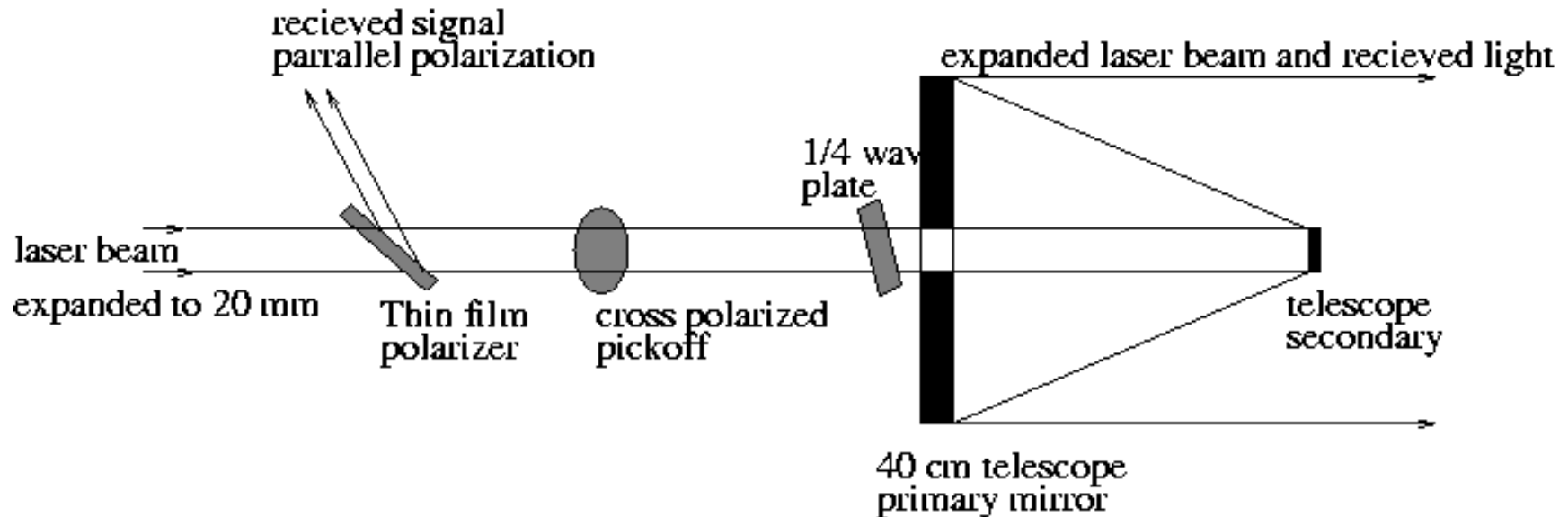
*Furka August 2005 by Igor Razenkov*



Thermal expansion of components effect the alignment of transmitter with the receiver. Here we consider the example of an 45 deg aluminum mountin block for a beam turning mirror.

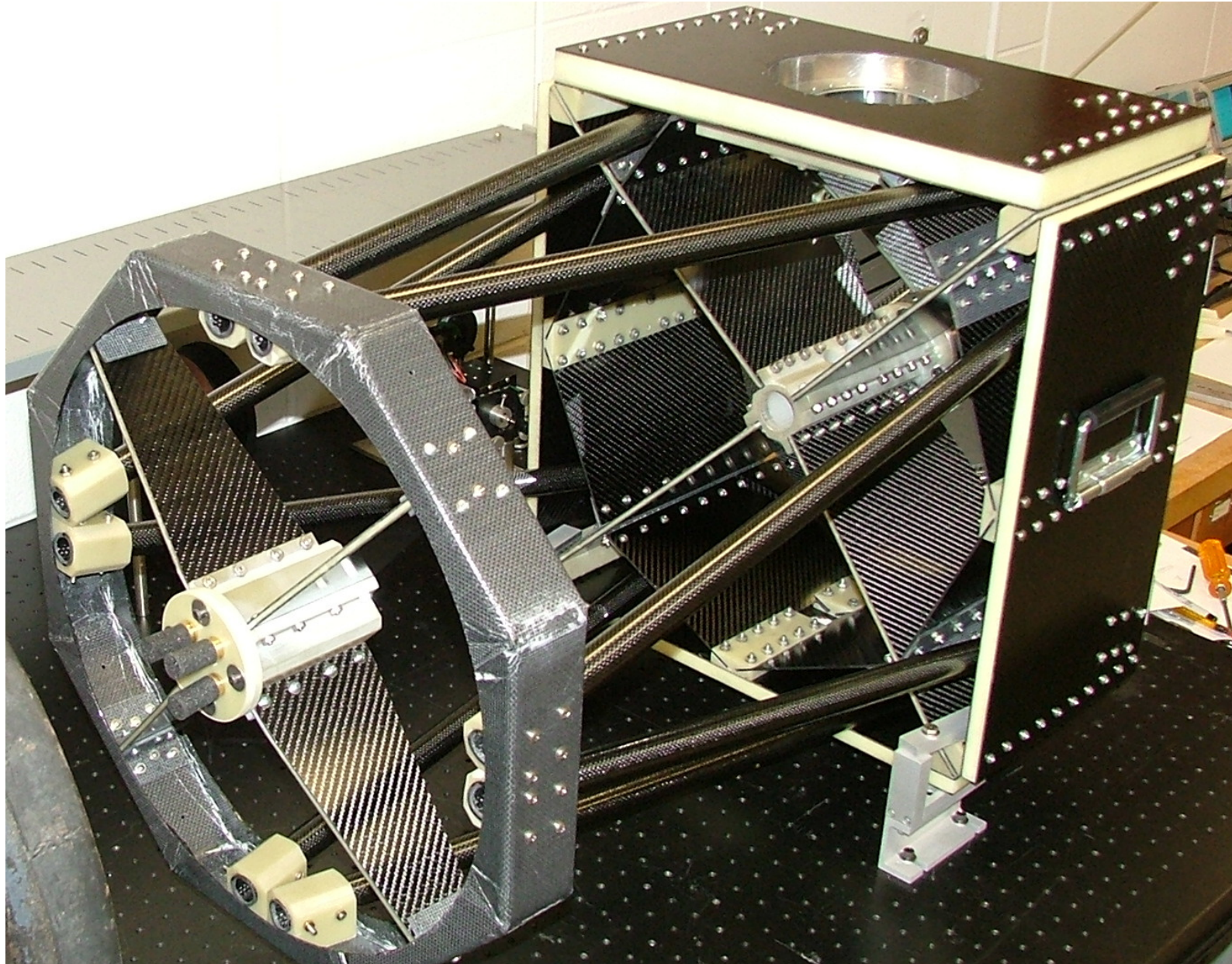
Angle shift due to 10 deg C temperature change:  $\Delta\varphi \sim \alpha \Delta T \sim 2.5 * 10^{-5} * 10$   
 $\Delta\varphi \sim 250$  microradian

# AHSRL transmit-receive telescope



- The 20 mm diameter linearly-polarized laser beam is converted to circular polarization by  $\frac{1}{4}$  wave plate before expansion 40 cm.
- The received signal is converted to linear polarization on return through the  $\frac{1}{4}$  wave plate. Approx. 10% of the signal is separated to measure the cross-polarized component. The parallel-polarized component is separated from the transmit beam by the thin-film polarizer.

# Transmit-Receive Telescope



I was asked to comment on following:

--Cost?

~\$ 1M

--Laser power, possible interference with Cerenkov measurements?

532 nm, maximum eyesafe power  $\sim 0.5$  W

--Maintenance cost?

Relatively low, visit Arctic site  $\sim 2$ -3 times/year

--External data requirements?

Radiosonde profiles from national weather service.

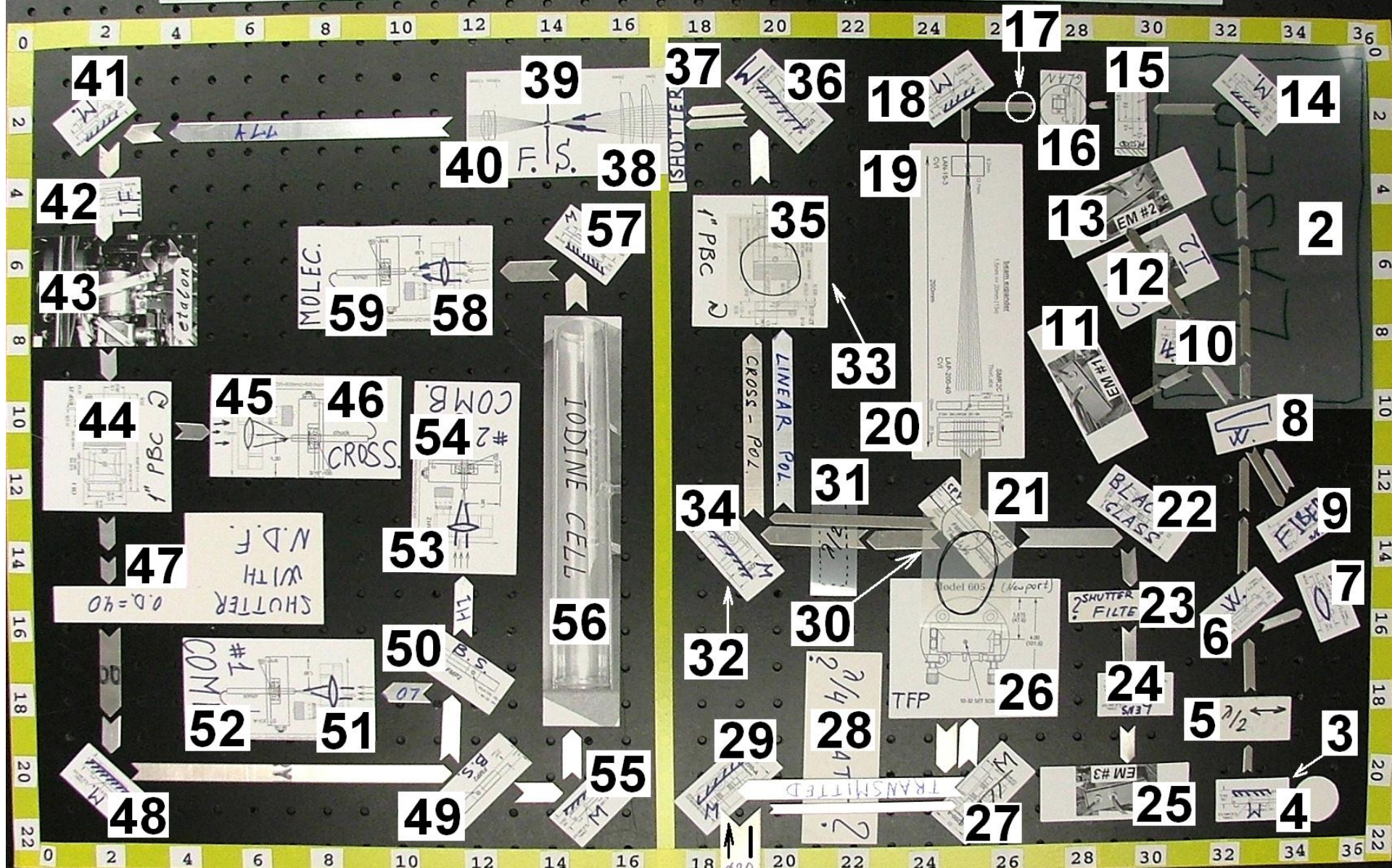


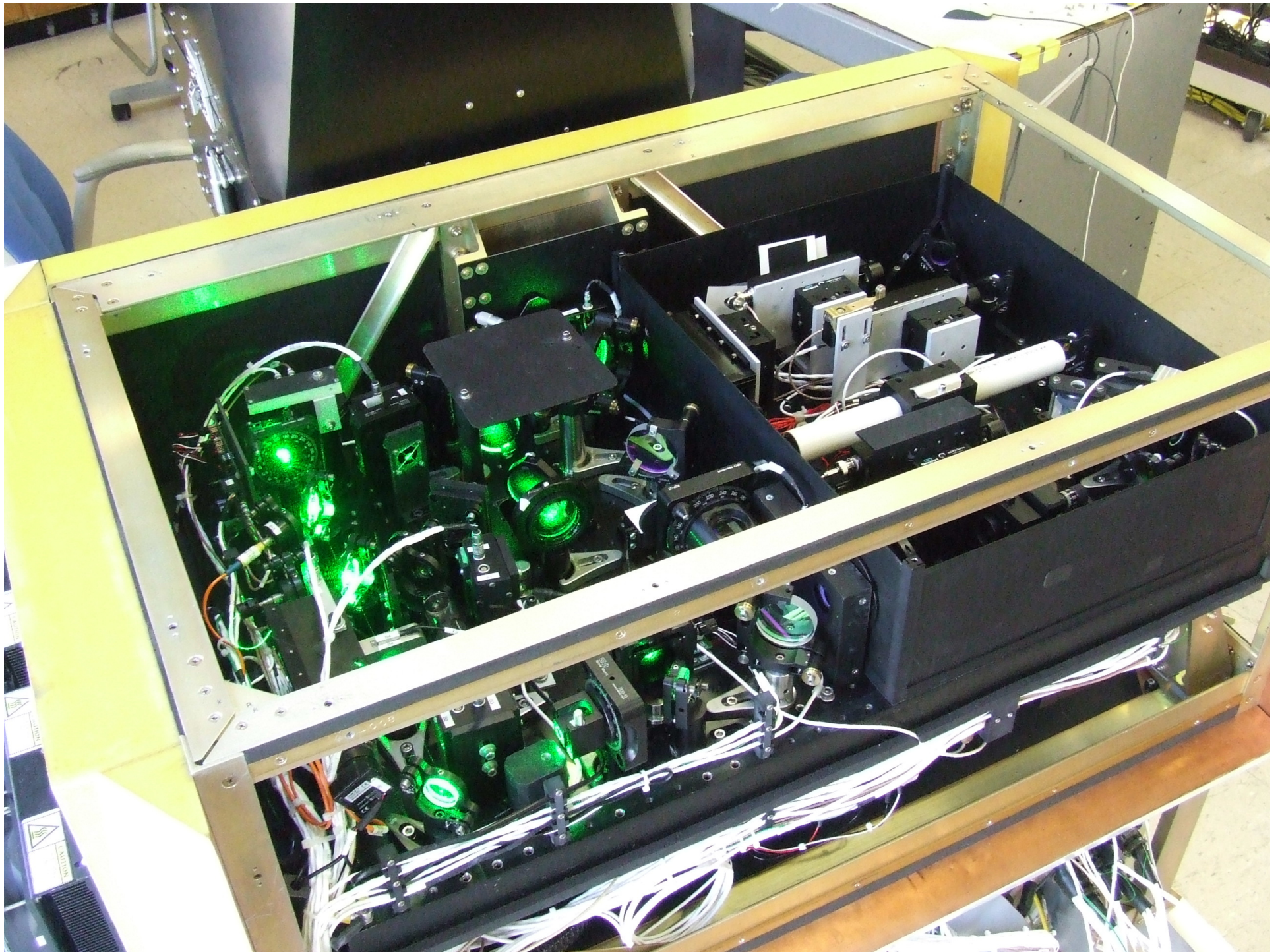
v.08

# RECEIVER

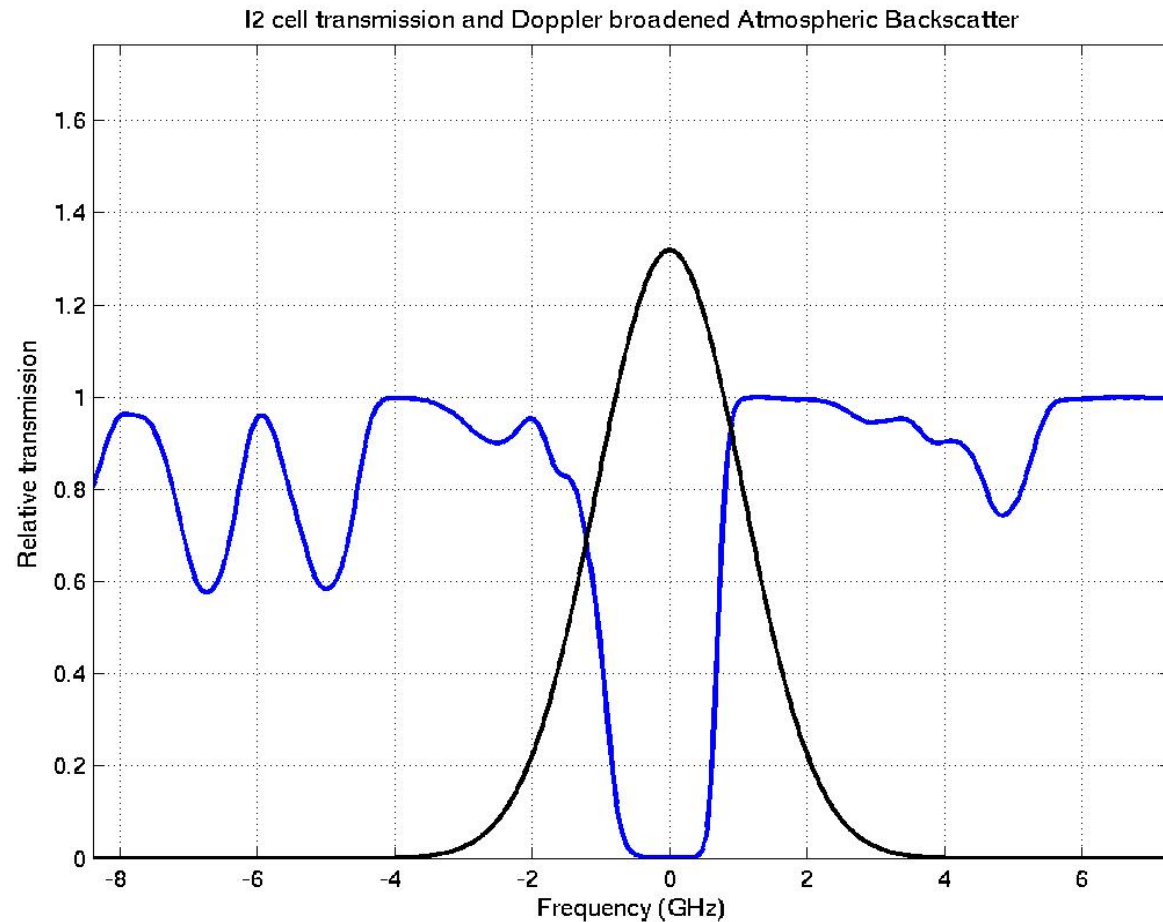
# TRANSMITTER

1

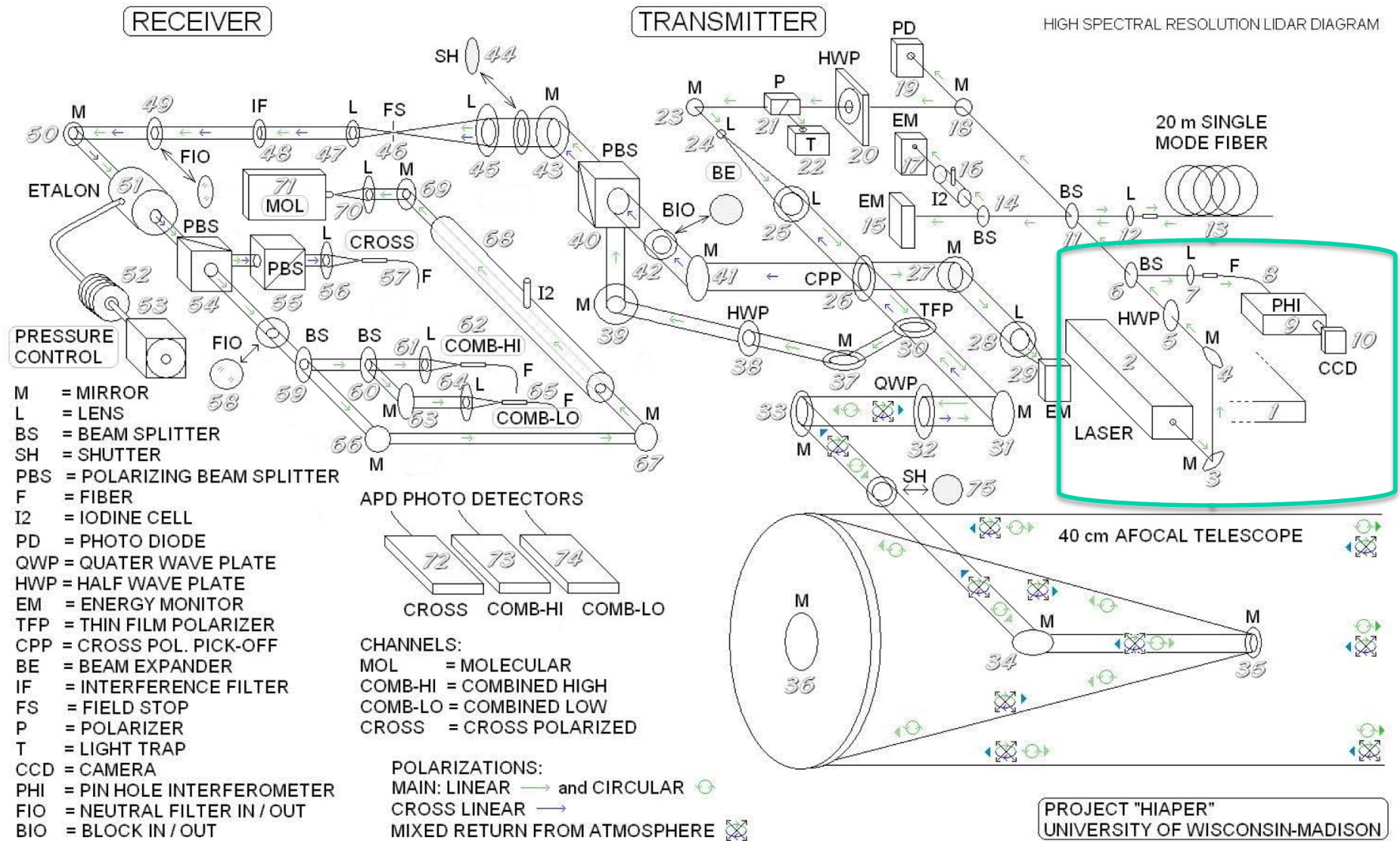




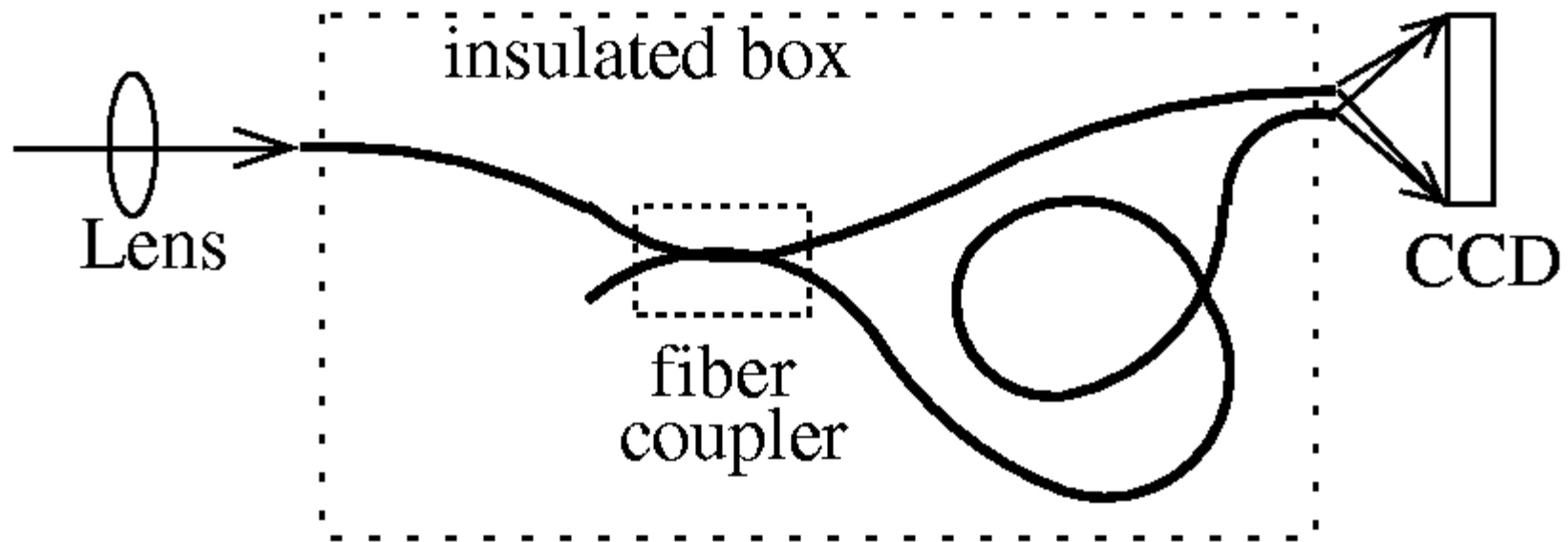
# HSRL calibration requires a spectral scan to determine bandpass of filters



# Laser and interferometer

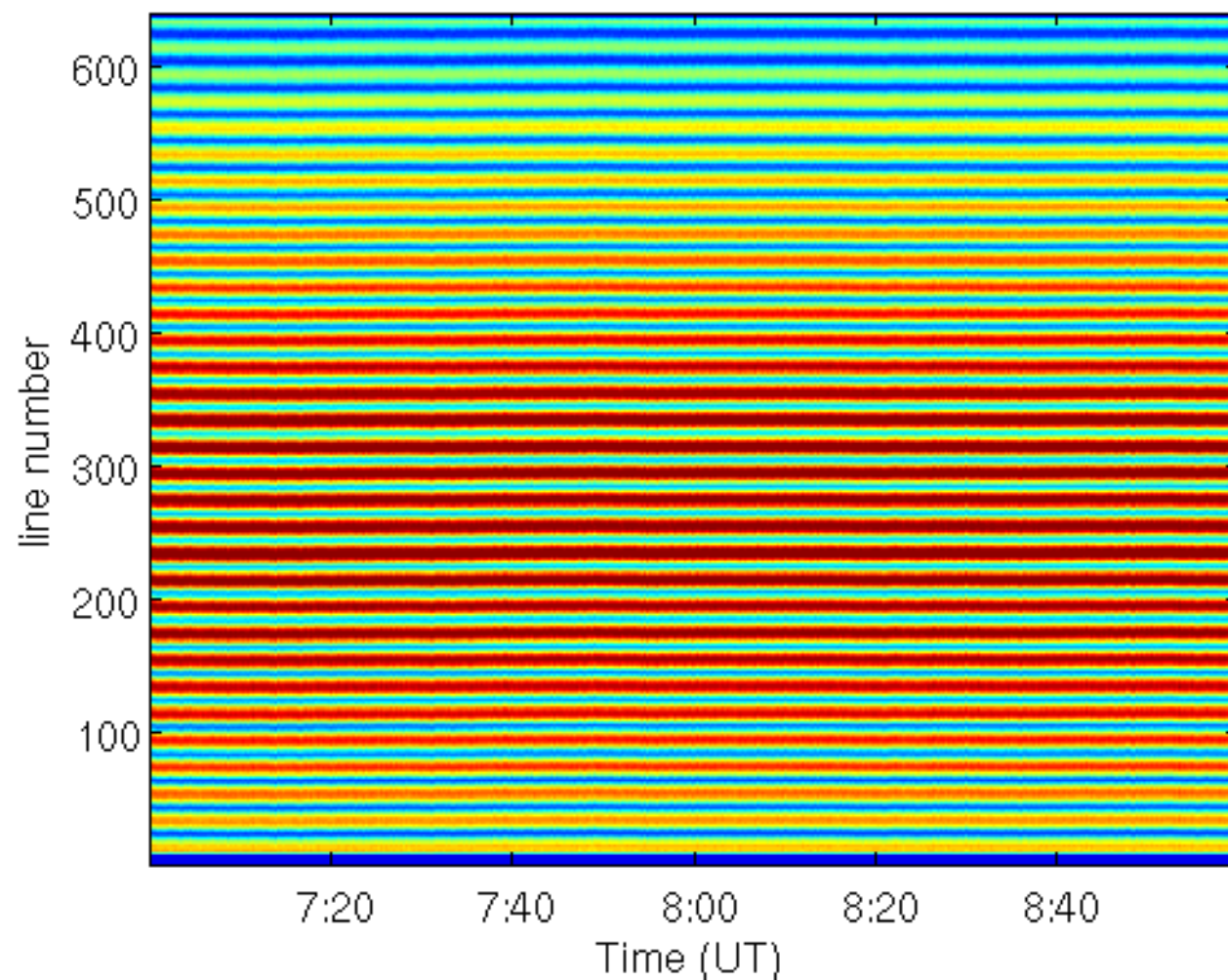


# Young's pinhole interferometer

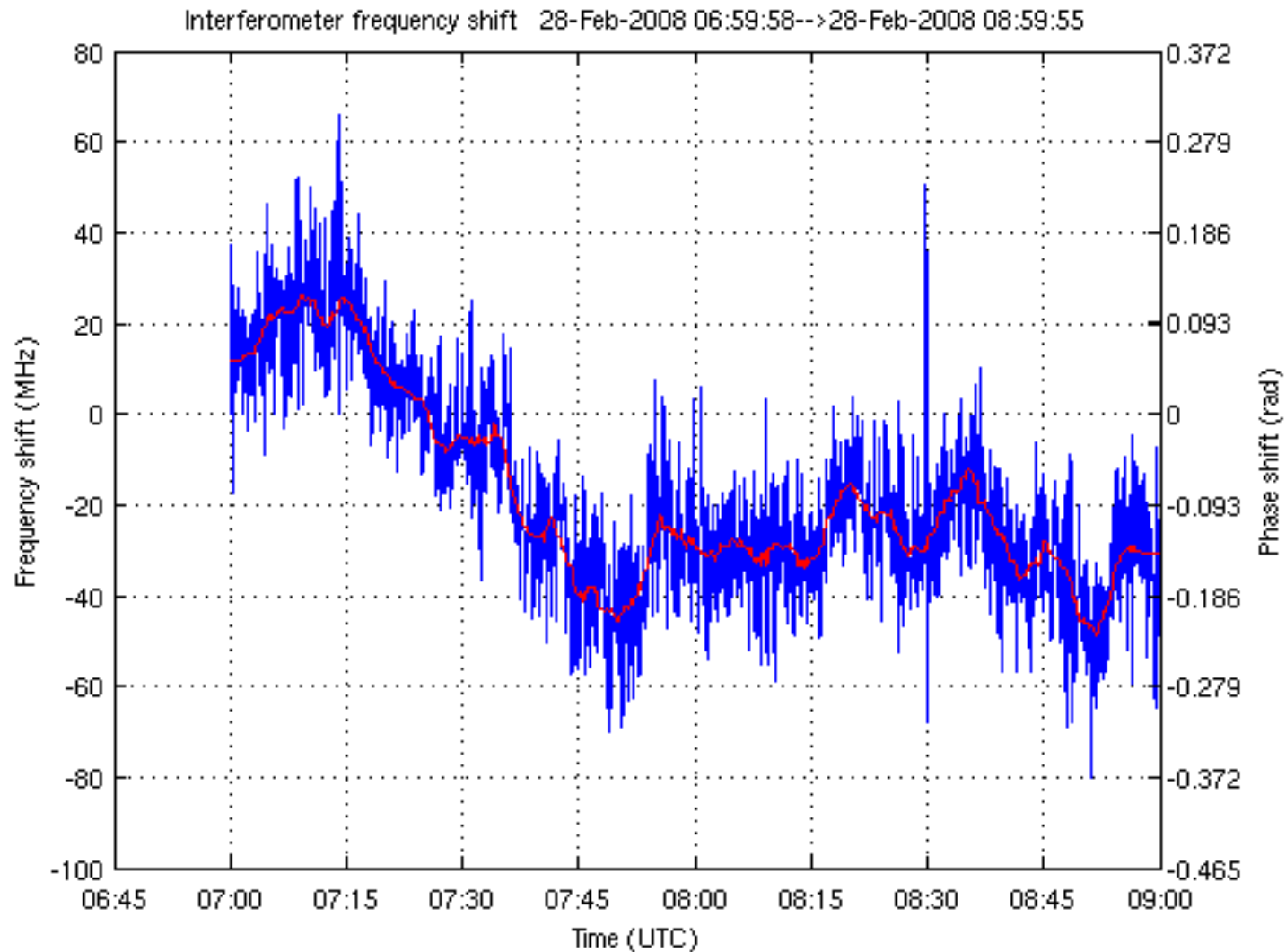


# One column from interferometer

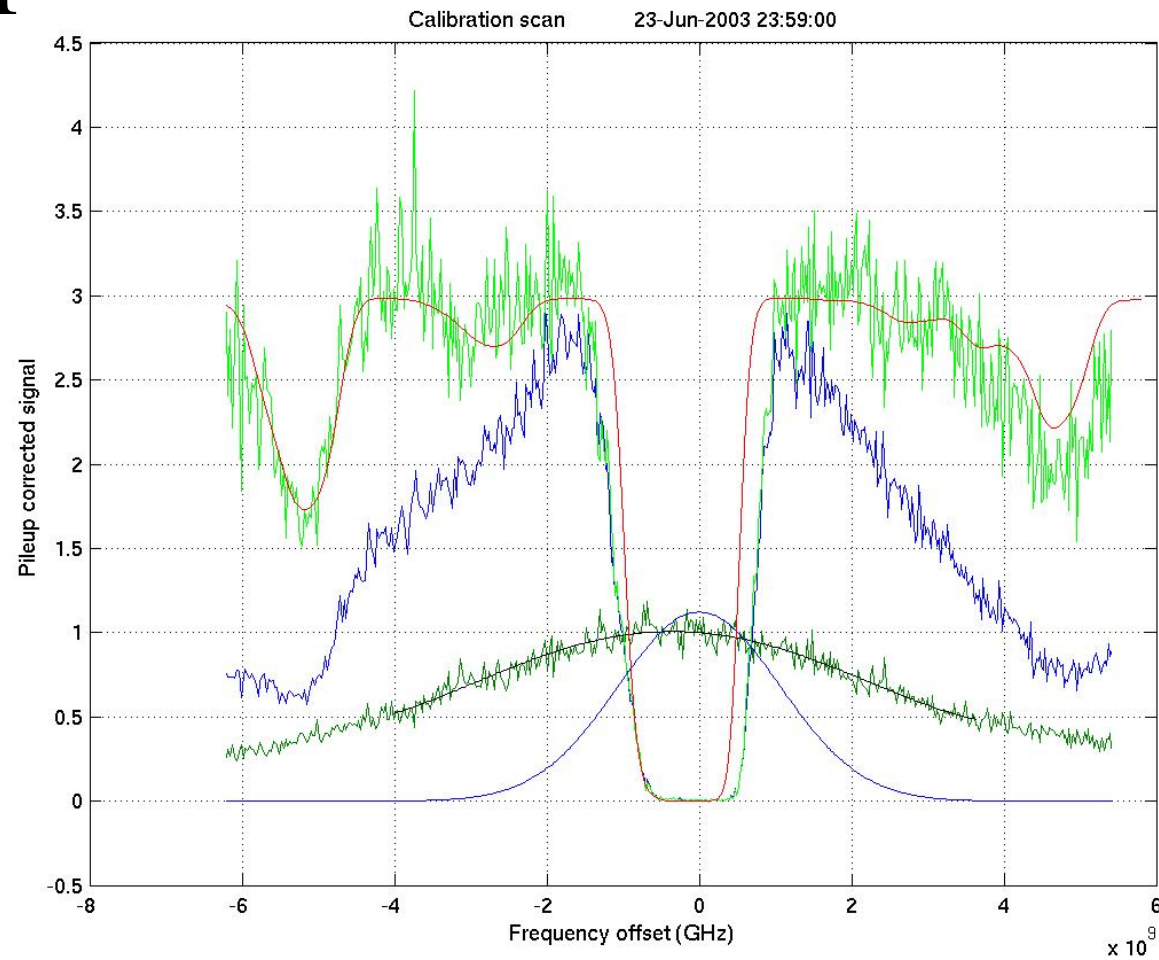
Interferometer 28-Feb-2008 06:59:58-->28-Feb-2008 08:59:55



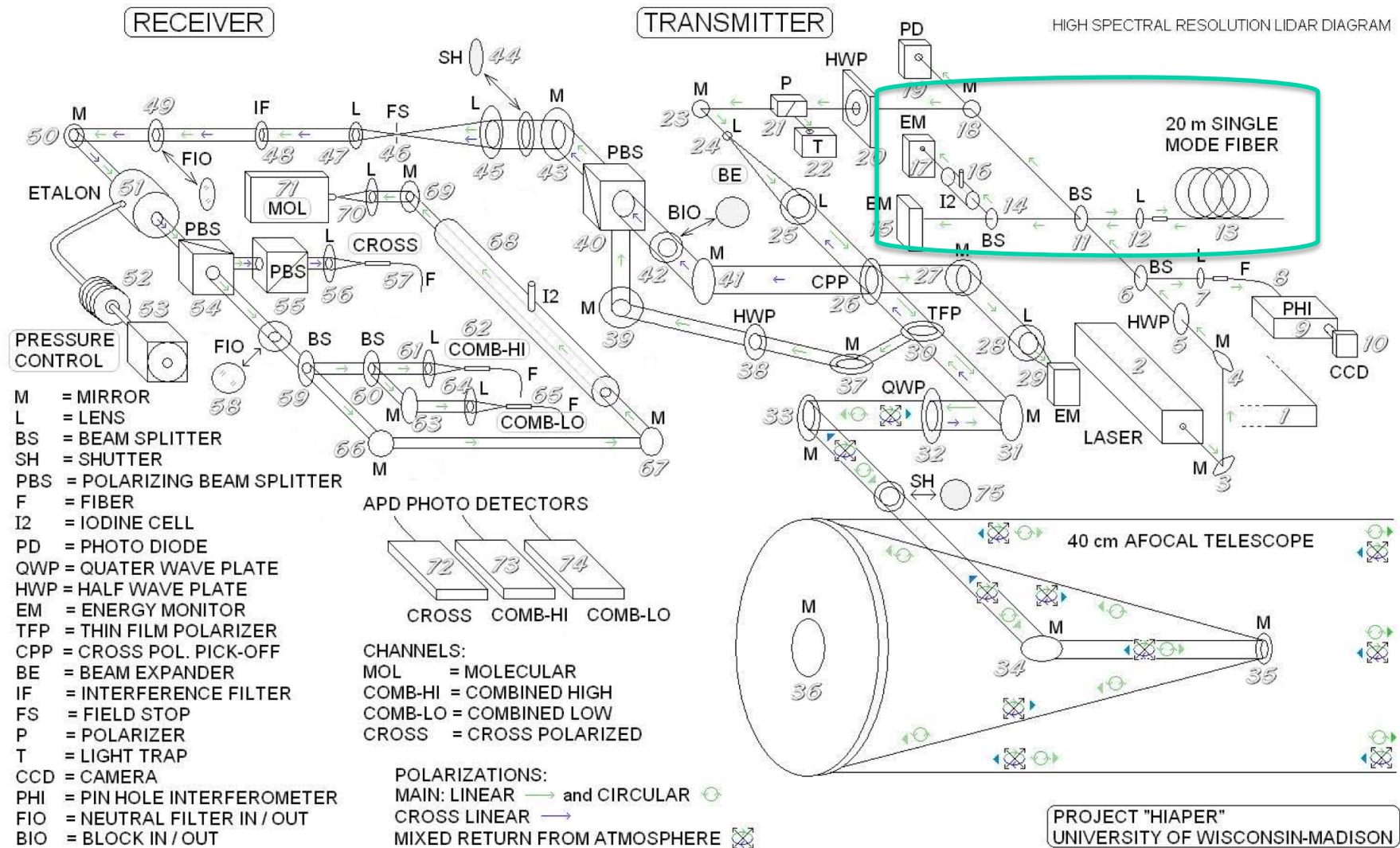
# Frequency vs time from interferometer



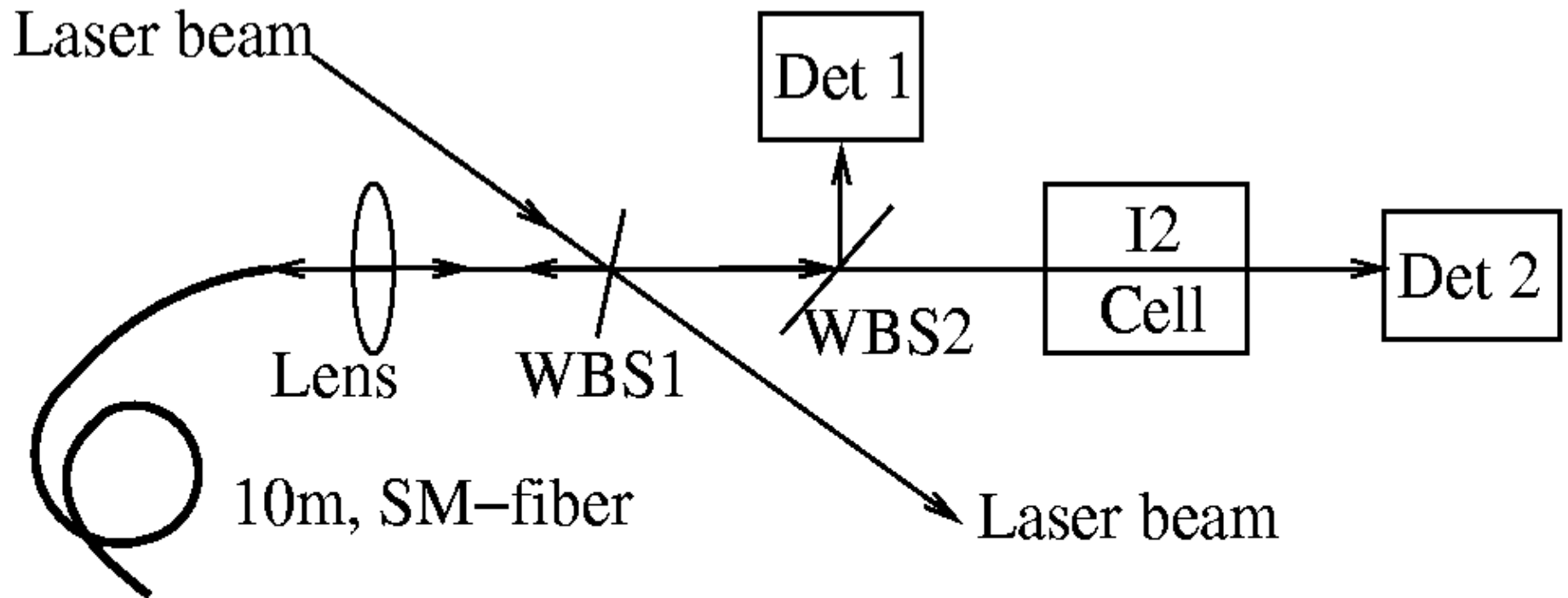
# Spectral scan for calibration



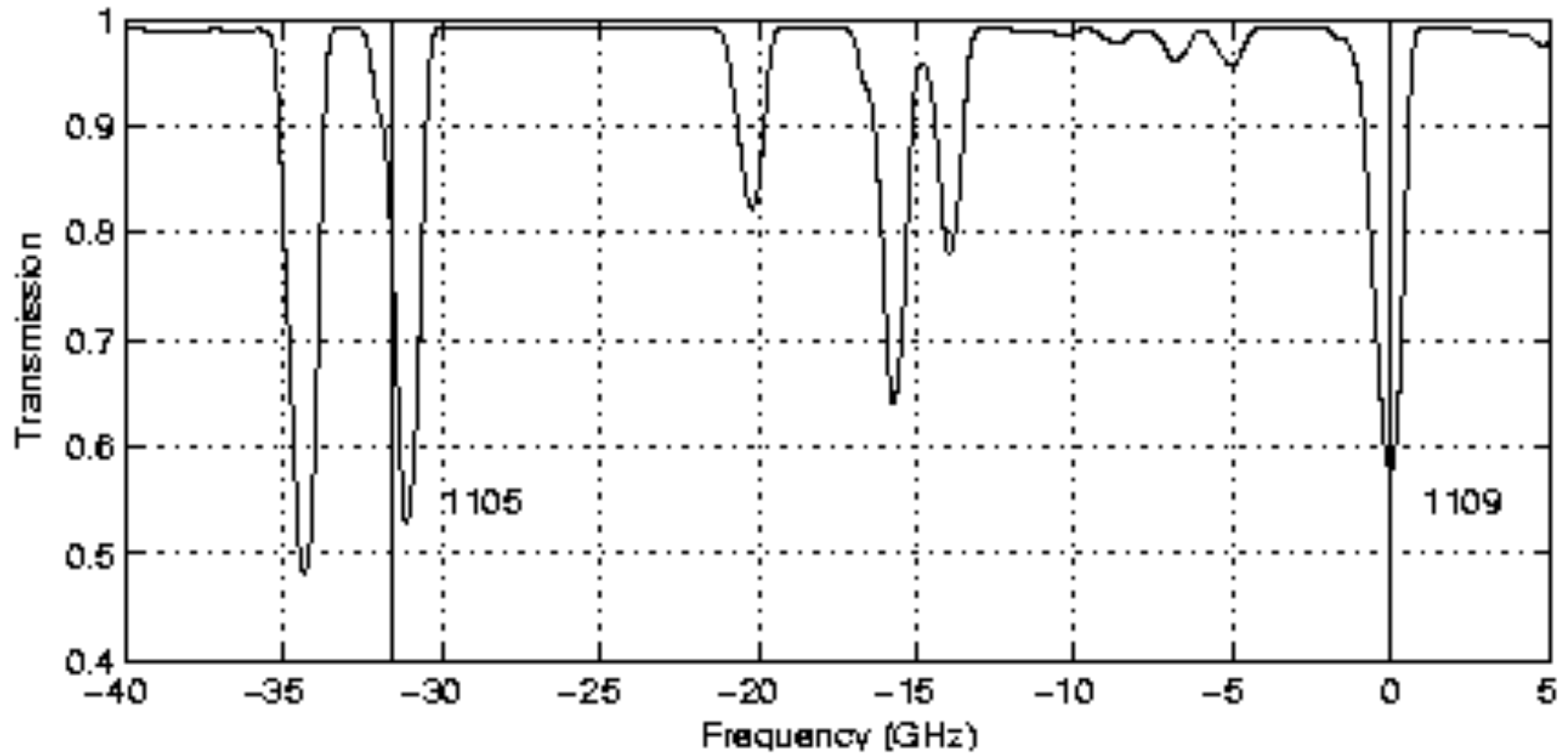
# Brillouin frequency locking



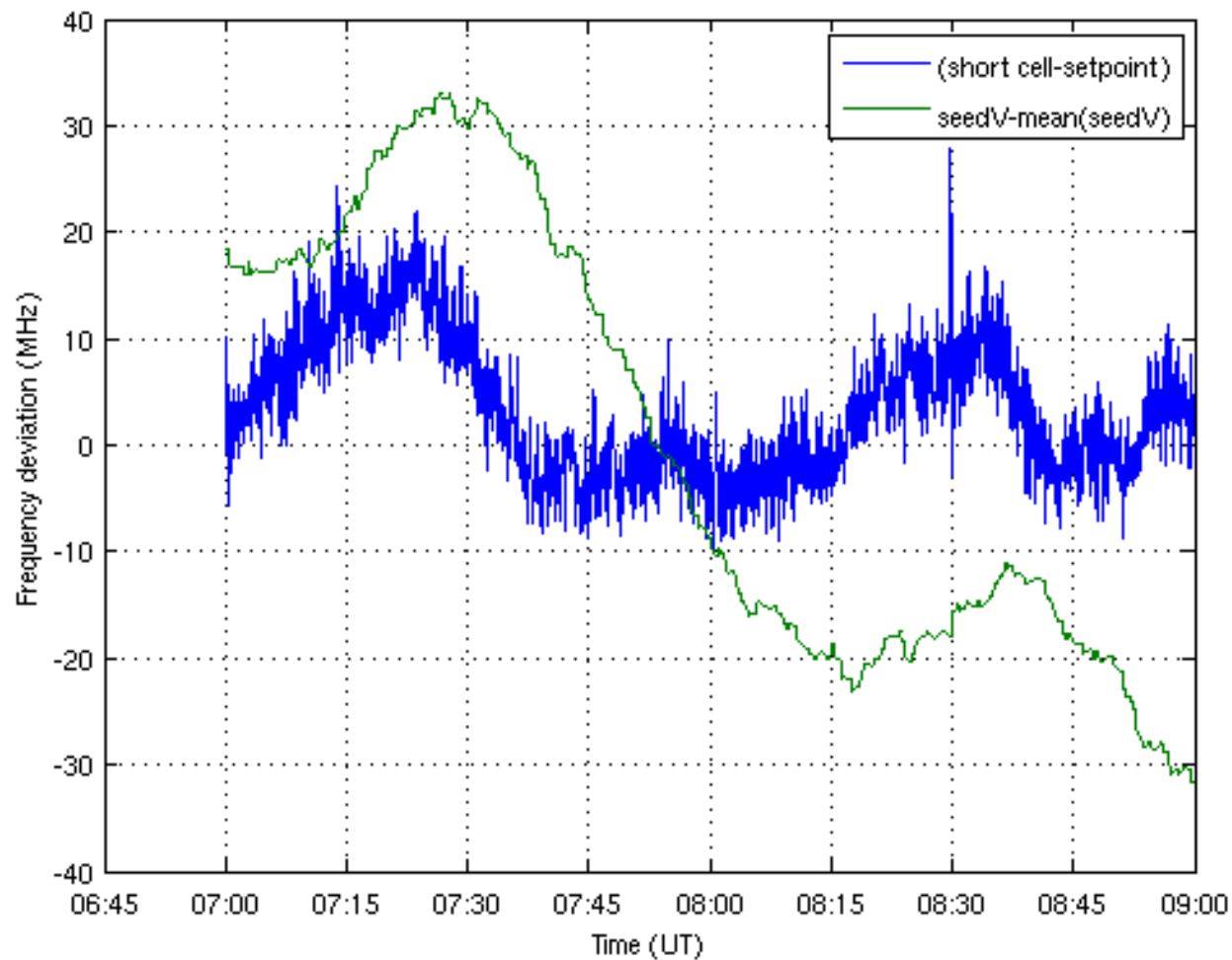
# Brillouin frequency locking system

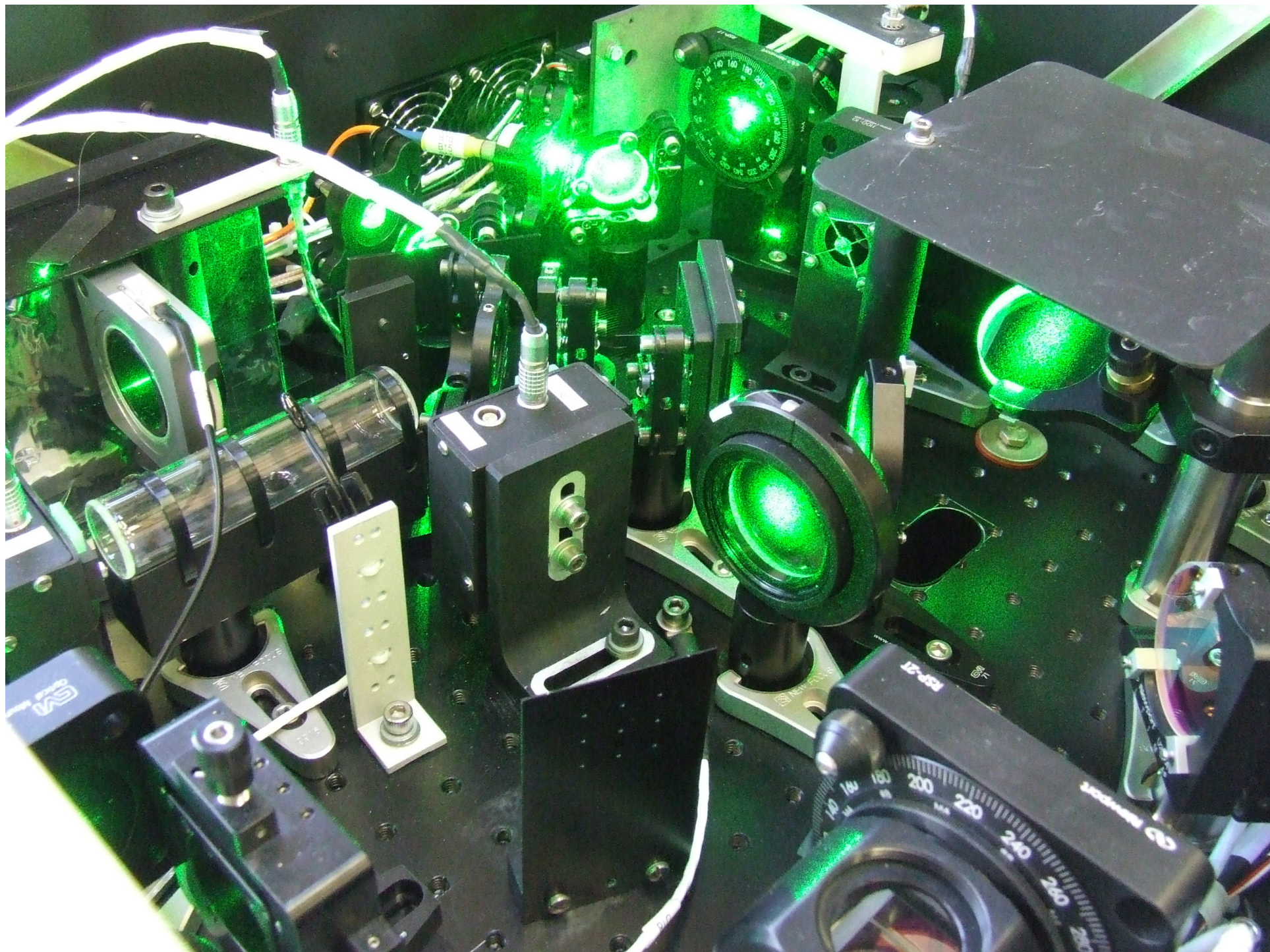


# Transmission of 2-cm iodine cell

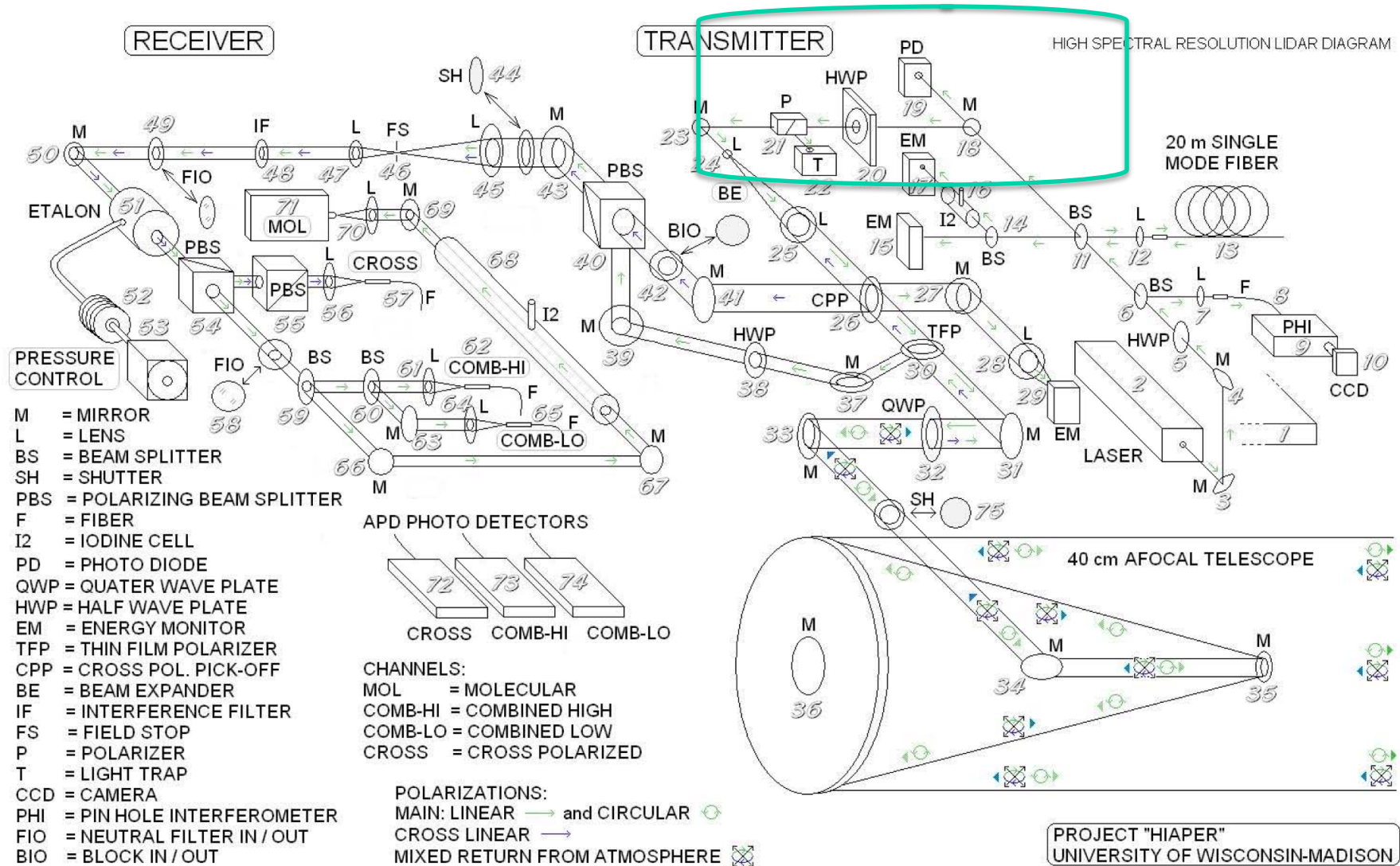


# Example of frequency locking

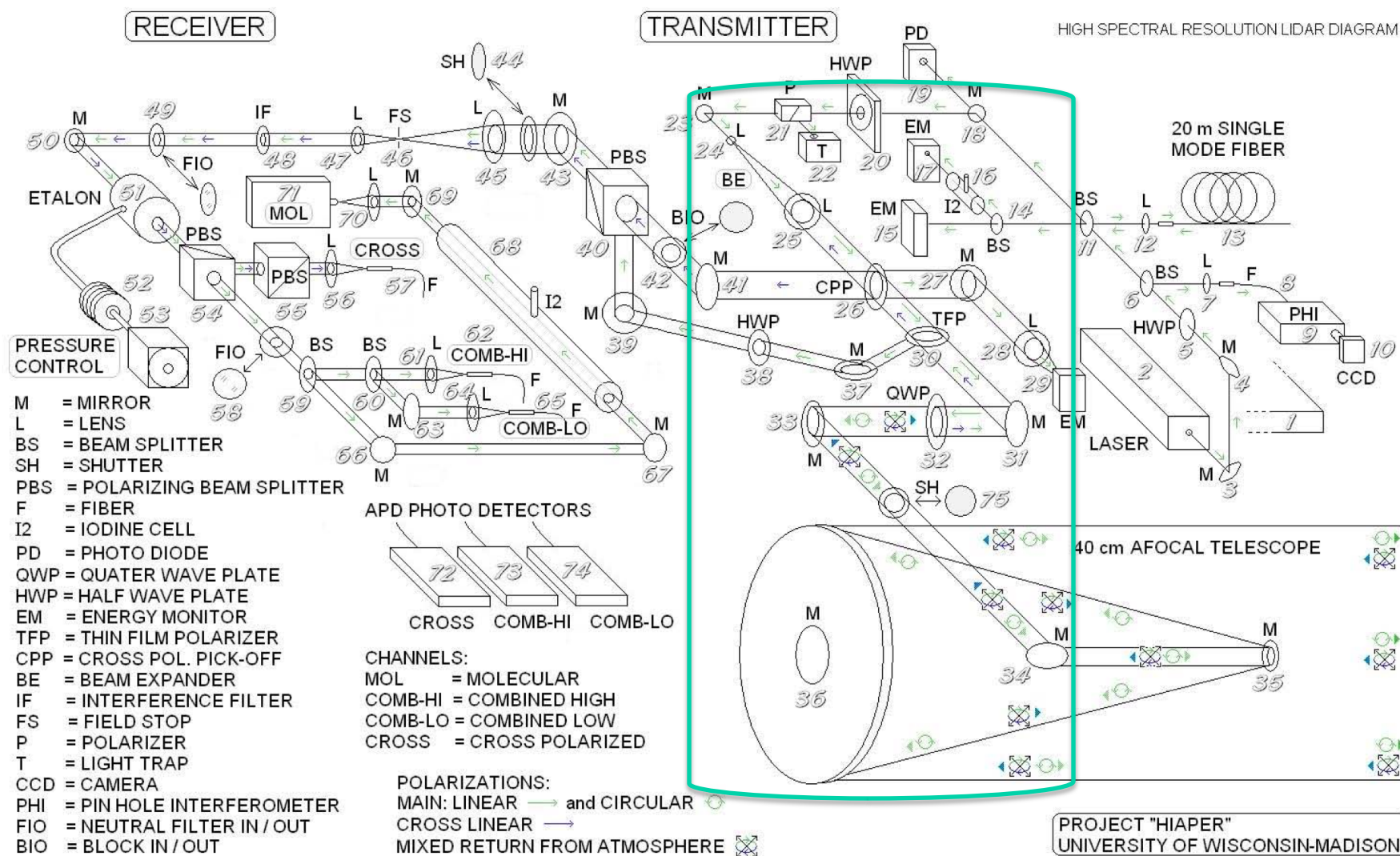




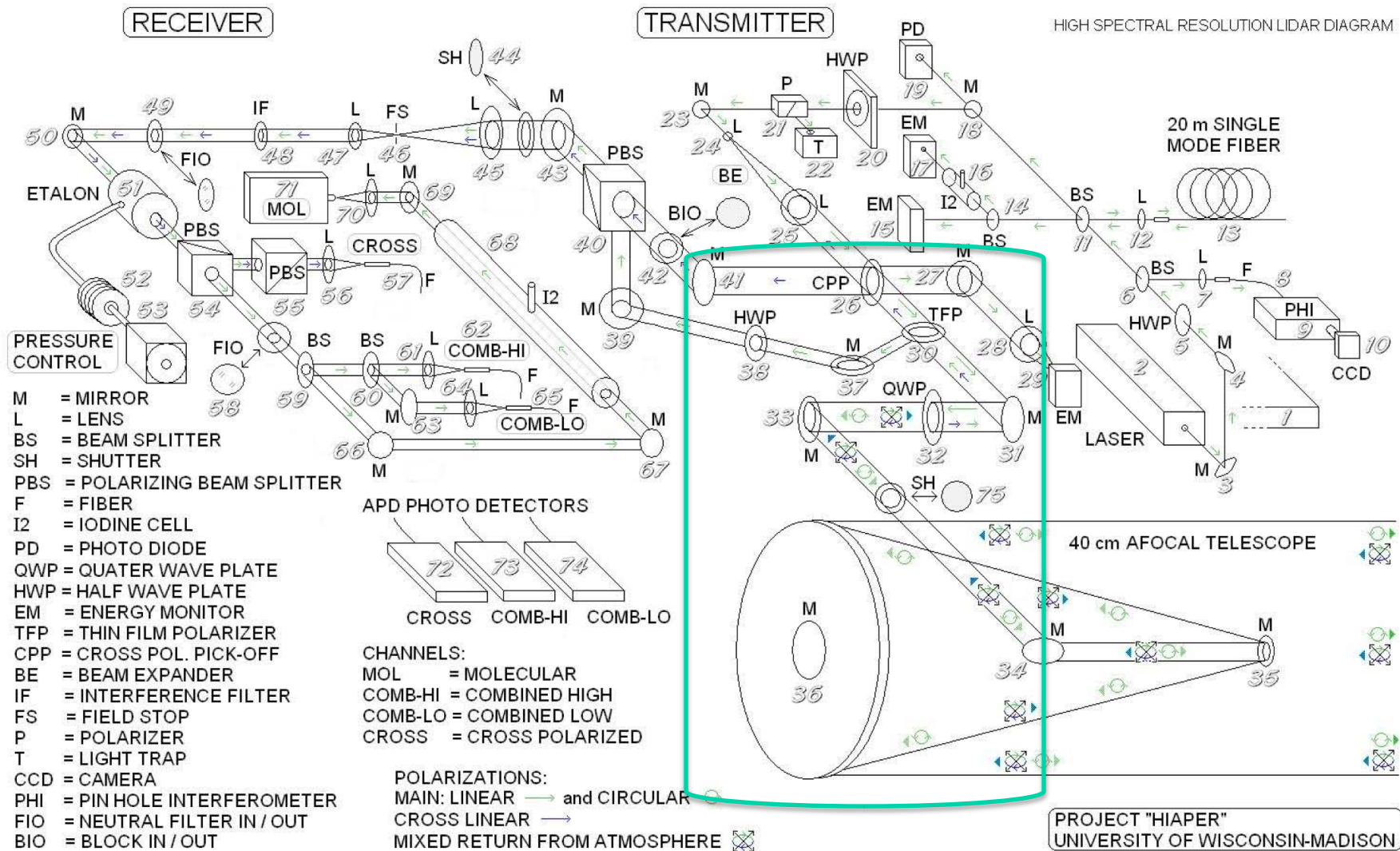
# Power control and photo diode timing detector



# Beam expansion and e-monitor



Received light passes through  $\frac{1}{4}$  plate, cross-pol and parallel pickups





## Specifications

### **Transmitter:**            **GVHSRL**

### **Langley HSRL**

Repetition rate	4000 Hz	200 Hz
Wavelength	532 nm	532 nm
Energy	82 uJ	2.5 mJ
Ave power	339 mW	500 mW

### **Receiver:**

Aperture	40 cm	40 cm
Bandwidth	8 GHz	60 GHz
Quantum Eff	55%	10% (?)
Field of View	100 mrad	250-1000 mrad
Optical trans	~34%	57%

Signal strength ~	1	0.27 (Area*Pwr*QE*h)
Sky Noise        ~	0.24	3.4 (Area*BW*W*QE*h)