

Track Reconstruction in IceCube

David J. Boersma

The IceCube Project

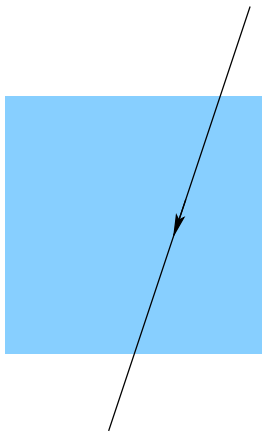


MANTS 2009, September 26

Outline

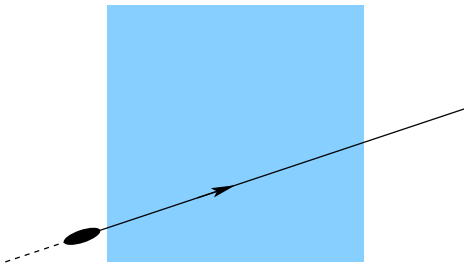
- 1 Event Types
- 2 Light Propagation
- 3 Reconstruction
- 4 Likelihood functions
- 5 Quality Parameters
- 6 References

Event Types (1): single muon



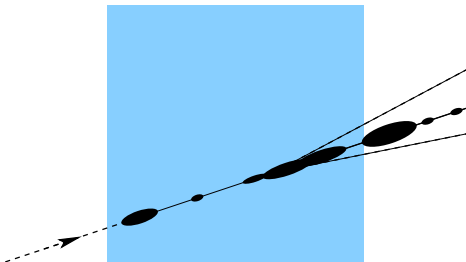
- **CR $\rightarrow \mu$**
- $\nu_\mu \rightarrow \mu$
- $\nu_\tau \rightarrow \tau \rightarrow \mu$
- CR $\rightarrow \mu$ (corner)
- CR $\rightarrow \mu$ (LE)
- $\nu_\mu \rightarrow \mu$ (\sim LE)
- $\nu_\mu \rightarrow \mu$ (\sim LE)
- $\nu_\mu \rightarrow \mu$ (LE)

Event Types (1): single muon



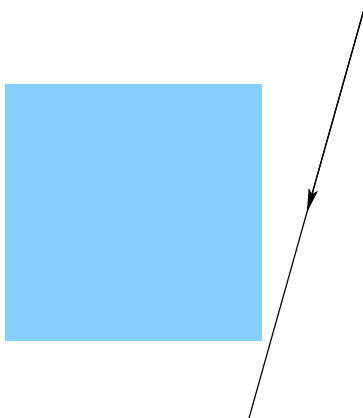
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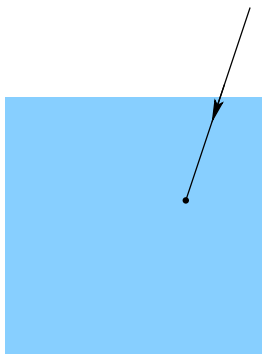
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Event Types (1): single muon



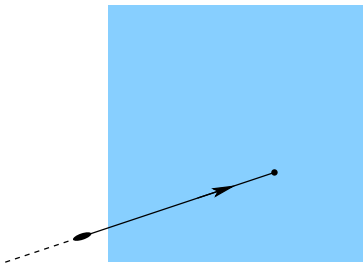
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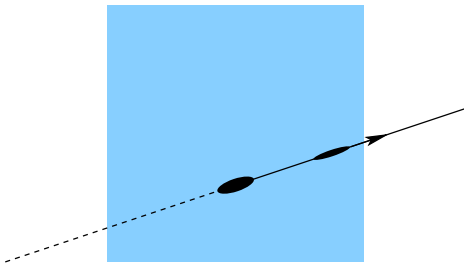
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- $\nu_{\mu} \rightarrow \mu$ (\sim LE)
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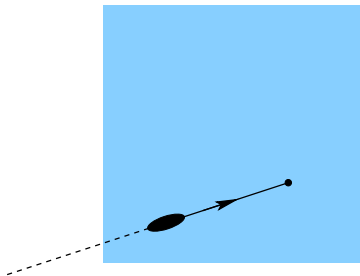
- $CR \rightarrow \mu$
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- $CR \rightarrow \mu$ (corner)
- $CR \rightarrow \mu$ (LE)
- $\nu_{\mu} \rightarrow \mu$ (**\sim LE**)
- $\nu_{\mu} \rightarrow \mu$ (\sim LE)
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Event Types (1): single muon



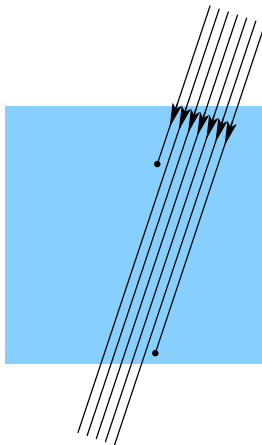
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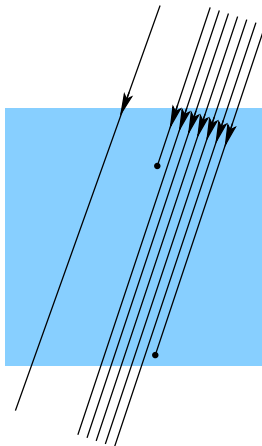
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Event Types (2): multiple muons



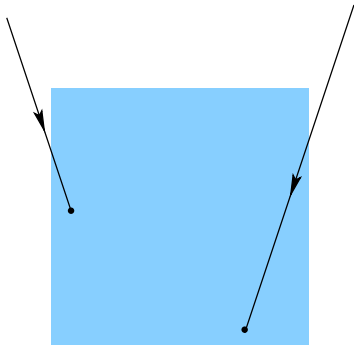
- **CR \rightarrow μ bundle**
- CR \rightarrow μ (HE, high p_T)
- 2CR \rightarrow 2 μ (coinc)
- μ pairs from decay of microscopic black holes

Event Types (2): multiple muons



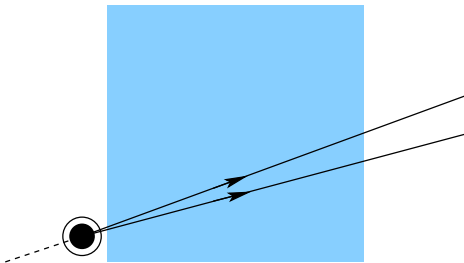
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Event Types (2): multiple muons



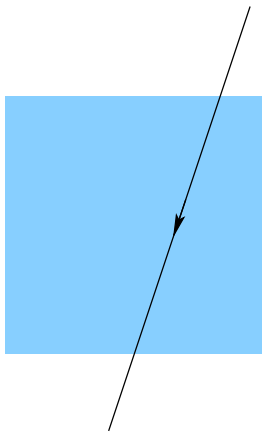
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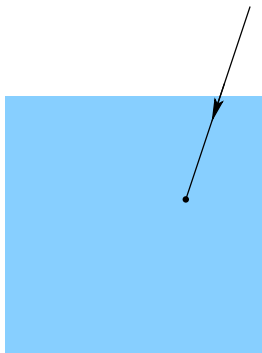
- CR \rightarrow μ bundle
- CR \rightarrow μ (HE, high p_T)
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- μ pairs from decay of microscopic black holes

Event Types (3): energy range



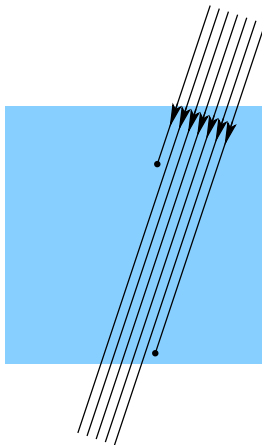
- **CR** \rightarrow μ
- CR \rightarrow μ (LE)
- CR \rightarrow μ (HE)
- ν_{μ} \rightarrow μ
- ν_{μ} \rightarrow μ (LE)
- ν_{μ} \rightarrow μ (HE)

Event Types (3): energy range



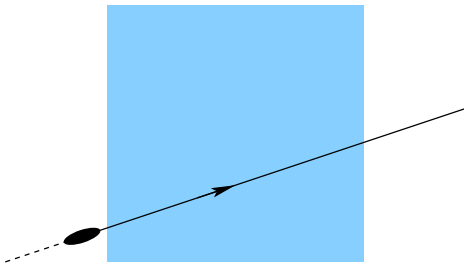
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- **$CR \rightarrow \mu$ (LE)**
- $CR \rightarrow \mu$ (HE)
- $\nu_{\mu} \rightarrow \mu$
- $\nu_{\mu} \rightarrow \mu$ (LE)
- $\nu_{\mu} \rightarrow \mu$ (HE)

Event Types (3): energy range



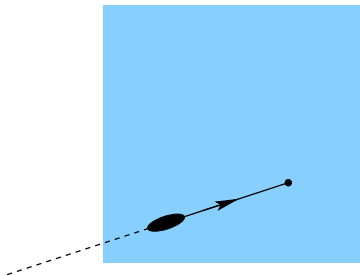
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- $CR \rightarrow \mu$ (LE)
- **$CR \rightarrow \mu$ (HE)**
- $\nu_{\mu} \rightarrow \mu$
- $\nu_{\mu} \rightarrow \mu$ (LE)
- $\nu_{\mu} \rightarrow \mu$ (HE)

Event Types (3): energy range



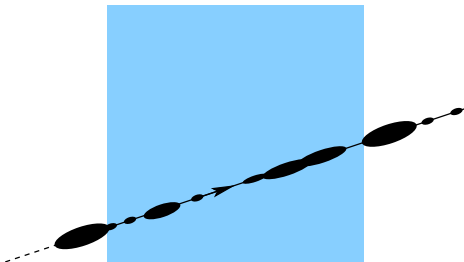
- $CR \rightarrow \mu$
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Event Types (3): energy range



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Event Types (3): energy range

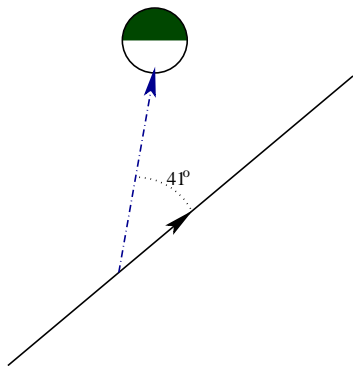


- $CR \rightarrow \mu$
- $CR \rightarrow \mu$ (LE)
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- $\nu_{\mu} \rightarrow \mu$
- $\nu_{\mu} \rightarrow \mu$ (LE)
- $\nu_{\mu} \rightarrow \mu$ (HE)

Event Types (4): many more!

...

Light & Photoelectrons



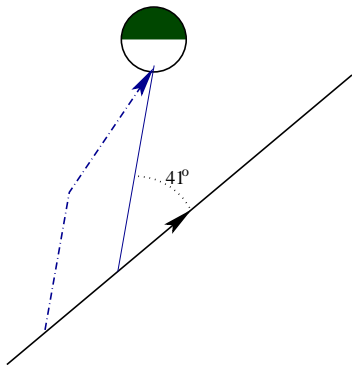
Phenomena:

- Direct light
- Scattering
- Absorption
- Time residual
- Arrival time distribution
- Jitter, noise

Available solutions:

- Analytic: Pandel
- Table: Photonics
- Fits: Photospline

Light & Photoelectrons



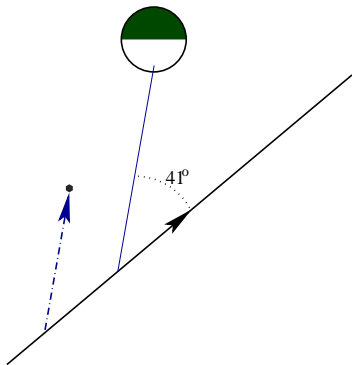
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Light & Photoelectrons



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Light & Photoelectrons

$$t_{residual} = t_{pulse} - t_{direct}$$

Phenomena:

- Direct light
- Scattering
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- **Time residual**
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Available solutions:

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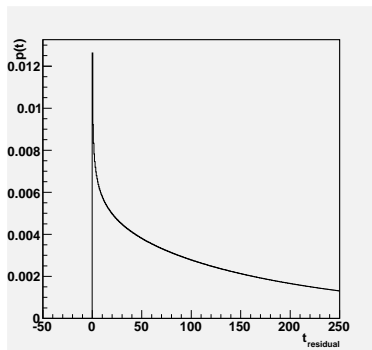
Light & Photoelectrons

Phenomena:

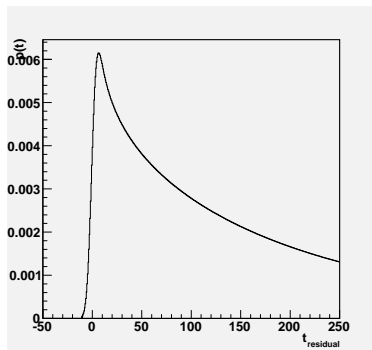
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Light & Photoelectrons



Phenomena:

- Direct light
- Scattering
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- Time residual
- Arrival time distribution
- **Jitter, noise**

Available solutions:

- Analytic: Pandel
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Light & Photoelectrons

$$p(\xi, \rho, t) = \frac{\rho^\xi t^{\xi-1}}{\Gamma(\xi)} e^{-\rho t}$$

$$\xi = R/\lambda$$

$$\rho = \frac{1}{\tau} + \frac{c}{\lambda a}$$

$$\mathcal{F}_\sigma(\xi, \rho, t) = \int_{-\infty}^{+\infty} p(\xi, \rho, t') g_\sigma(t' - t, \sigma) dt'$$

Phenomena:

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Available solutions:

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Light & Photoelectrons

(photonics movie)

Phenomena:

- Direct light
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Light & Photoelectrons

Phenomena:

- Direct light
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- Jitter, noise

Available solutions:

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Elements in Event Reconstruction

- 1 Determine event type(s)
 - 2 Fit variables, parametrization
 - 3 Likelihood L (light emission, propagation)
 - 4 Seeding algorithm
 - 5 Maximize L
- event topology
 - which variables are needed to specify the physics
 - `I3EventHypothesis`

Elements in Event Reconstruction

- 1 Determine event type(s)
 - 2 Fit variables, parametrization**
 - 3 Likelihood L (light emission, propagation)
 - 4 Seeding algorithm
 - 5 Maximize L
- Which physics variables do we want to fit?
 - Choose good parametrization (avoid singularities, cyclic variables)
 - Stepsizes, bounds, etc.
 - `I3ParametrizationBase`

Elements in Event Reconstruction

- 1 Determine event type(s)
- 2 Fit variables, parametrization
- 3 Likelihood L (light emission, propagation)**
- 4 Seeding algorithm
- 5 Maximize L

- light emission (NPE, PDF?)
- data representation (waveforms, pulses?)
- Bayesian terms?
- `I3EventLogLikelihoodBase`

Elements in Event Reconstruction

- 1 Determine event type(s)
- 2 Fit variables, parametrization
- 3 Likelihood L (light emission, propagation)
- 4 Seeding algorithm**
- 5 Maximize L

- first guess
- numerical considerations (e.g. make sure that time residuals are mostly positive)
- `I3SeedServiceBase`

Elements in Event Reconstruction

- 1 Determine event type(s)
- 2 Fit variables, parametrization
- 3 Likelihood L (light emission, propagation)
- 4 Seeding algorithm
- 5 Maximize L**

- *minimize* $-\log(L)$
- Generic minimizer algorithm
- Typically simplex (brute force, particle swarm, simulated annealing, etc.)
- `I3MinimizerBase`

Likelihood (only charge)

$$\begin{aligned}\log(L) &= \sum_{d \in \{\text{all DOMs}\}} \log(L_d) \\ \log(L_d) &= \log\left(\frac{\mu_d^{N_d} e^{-\mu_d}}{N_d!}\right) \\ &= N_d \log(\mu_d) - \mu_d - \log(N_d!) \\ &= L_{d,\text{brightness}} + L_{d,\text{combinatorial}}\end{aligned}$$

Here, for every DOM d :

μ_d = expected number of photoelectrons

N_d = detected number of photoelectrons

Likelihood (only charge)

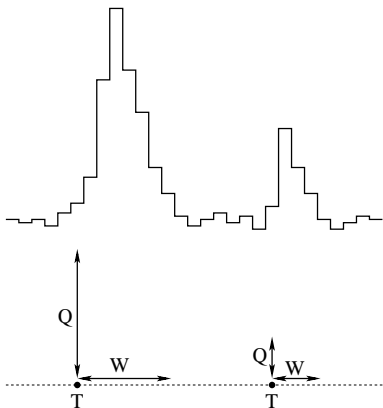
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Here, for every DOM d :

μ_d = expected number of photoelectrons

N_d = detected number of photoelectrons

Time information



- Waveforms
 - ATWD ($128 \times 3.6\text{ns}$)
 - FADC ($256 \times 25.0\text{ns}$)
- "Extracted" pulses

Likelihood (charge and time)

$$\begin{aligned}\log(L_d) &= \sum_i \log \left(\frac{\mu_{di}^{N_{di}} e^{-\mu_{di}}}{N_{di}!} \right) \\ &= \sum_i N_{di} \log(\mu_{di}/\mu_d) \\ &\quad + N_d \log(\mu_d) - \mu_d \\ &\quad - \sum_i \log(N_{di}!) \\ &= L_{d,timing} + L_{d,brightness} + L_{d,combinatorial}\end{aligned}$$

Here, for every DOM d :

μ_{di} = expected number of photoelectrons in time bin i

N_{di} = detected number of photoelectrons in time bin i

μ_d = expected total number of photoelectrons

N_d = detected total number of photoelectrons

Likelihood (charge and time)

$$\begin{aligned}\log(L_d) &= \sum_i \log \left(\frac{\mu_{di}^{N_{di}} e^{-\mu_{di}}}{N_{di}!} \right) \\ &= \sum_i N_{di} \log(\mu_{di}/\mu_d) \\ &\quad + N_d \log(\mu_d) - \mu_d \\ &\quad - \sum_i \log(N_{di}!) \\ &= L_{d,timing} + L_{d,brightness} + L_{d,combinatorial}\end{aligned}$$

Here, for every DOM d :

μ_{di} = expected number of photoelectrons in time bin i

N_{di} = detected number of photoelectrons in time bin i

μ_d = expected total number of photoelectrons

N_d = detected total number of photoelectrons

Simplified likelihood

Reconstruct only track geometry

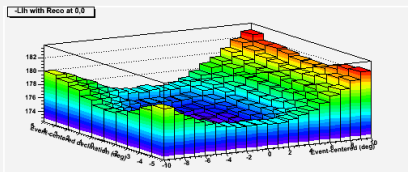
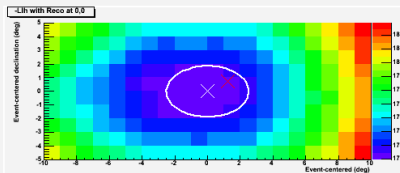
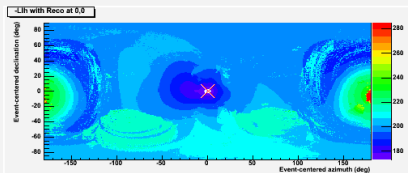
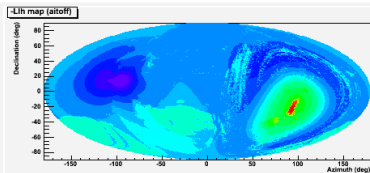
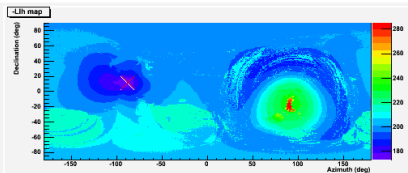
- **"SPE"** likelihood: ignore pulse charges

$$\log(L_d) = \sum_i \log \left(\frac{\mu_{di}}{\mu_d} \right) = \sum_i \log(p(t_i))$$

- **"SPEAll"**: use all pulses
- **"SPE1st"**: use only first pulse every DOM
- **"MPE"** likelihood: use total charge and time of first hit:

$$L_d = N_d p(t_0) \left[\int_{t_0}^{\infty} p(t) dt \right]^{N_d - 1}$$

$-\log(L)$ map (good neutrino event, IC22)



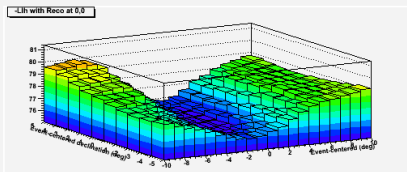
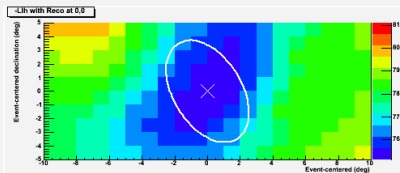
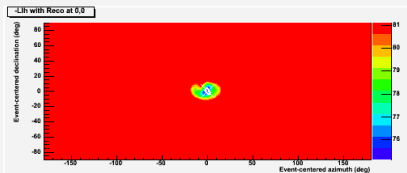
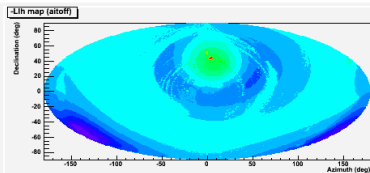
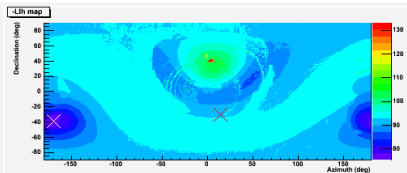
RunID = 1, SubRunID = 0, EventID = 1134, nSamples = 82506

True Zen = 102.2, True Azi = -86.9, Reco Zen = 101.5, Reco Azi = -88.2 (all in deg)

Nchan = 28, Nstring = 5, Ndir = 11, Ldir = 209.3 m

Sigma = 2.21, err_1 = 2.51, err_2 = 1.85, alpha = -89.89 (all in deg)

$-\log(L)$ map (coincident muons, IC22)



RunID = 1, SubRunID = -1, EventID = 27, nSamples = 82506

MC Zen = 59.8, MC Azi = 14.4 (deg), MC E = 1676.7, # muons = 2

Reco Zen = 50.7, Reco Azi = -168.9 (deg)

Nchan = 13, Nstring = 3, Ndir = 7, Ldir = 327.6 m

Sigma = 3.18, err_1 = 3.94, err_2 = 2.17, alpha = 23.25 (all in deg)

Quality Parameters

(To do: a cartoon illustrating what direct hits are)

- Direct hits: N_{dir} , L_{dir}
- Likelihood ratios
- Likelihood width ("paraboloid sigma")

Quality Parameters

(To do: a cartoon illustrating what direct length is)

- Direct hits: N_{dir} , L_{dir}
- Likelihood ratios
- Likelihood width ("paraboloid sigma")

Quality Parameters

(To do: a cartoon illustrating the use of likelihood ratios)

- Direct hits: N_{dir} , L_{dir}
- Likelihood ratios
- Likelihood width ("paraboloid sigma")

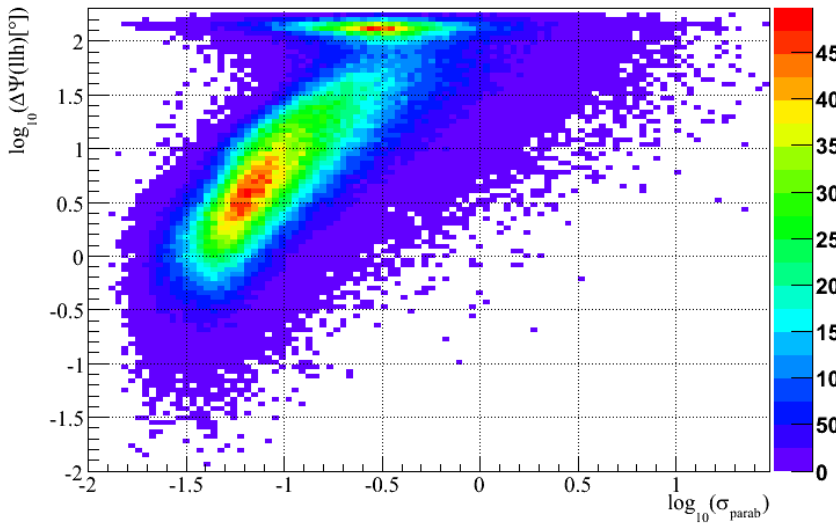
Quality Parameters

(To do: a cartoon illustrating what a paraboloid error ellips)

- Direct hits: N_{dir} , L_{dir}
- Likelihood ratios
- Likelihood width ("paraboloid sigma")

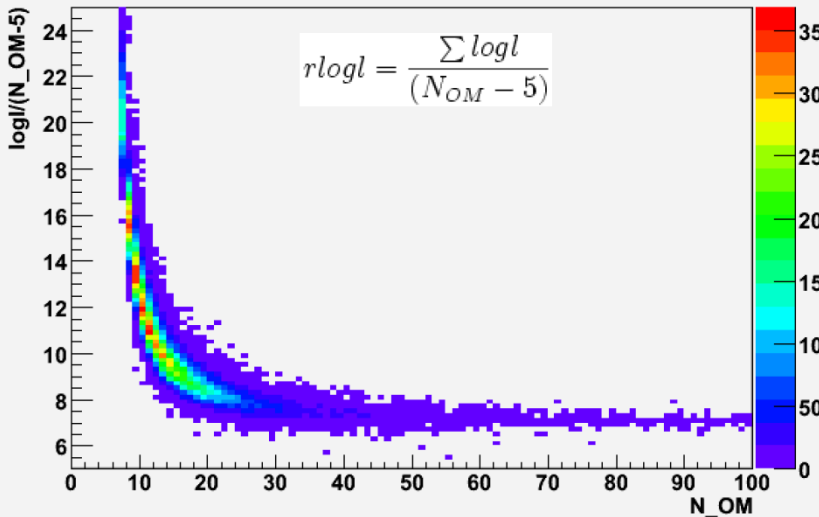
Paraboloid

Error Ellipse vs. Llh Total PSF Minimum Cut dCorsika Single Muons μ -Filtered



Reduced log-likelihood

rlogl_vs_N_OM



Some reference material

- arXiv:astro-ph/0403367v1: Till Neunhöffer, *Estimating the angular resolution of tracks in neutrino telescopes based on a likelihood analysis*, Astropart. Phys. **25** (2006) 220-225
- arXiv:astro-ph/0407044: J. Ahrens *et al.*, *Muon Track Reconstruction and Data Selection Techniques in AMANDA*, Nucl. Instrum. Meth. **A524** (2004) 169
- arXiv:astro-ph/0506136: George Japaridze and Mathieu Ribordy, *Realistic arrival time distribution from an isotropic light source*
- arXiv:astro-ph/0611604: M. Ribordy, *Reconstruction of Composite Events in Neutrino Telescopes*
- arXiv:astro-ph/0702108: J. Lundberg *et al.*, *Light tracking through ice and water – Scattering and absorption in heterogeneous media with Photonics*, Nucl. Instrum. Meth. **A581** (2007) 619-631
- arXiv:0704.1706: N. van Eijndhoven, O. Fadiran, G. Japaridze, *Implementation of a Gauss convoluted Pandel PDF for track reconstruction in Neutrino Telescopes*, Astropart. Phys. **28** (2007) 456-462
- wikipedia: Cramér-Rao bound
- *Reconstruction of high energy muons in IceCube*: paper in preparation