

Direction Reconstruction using Simulation-Based Inference

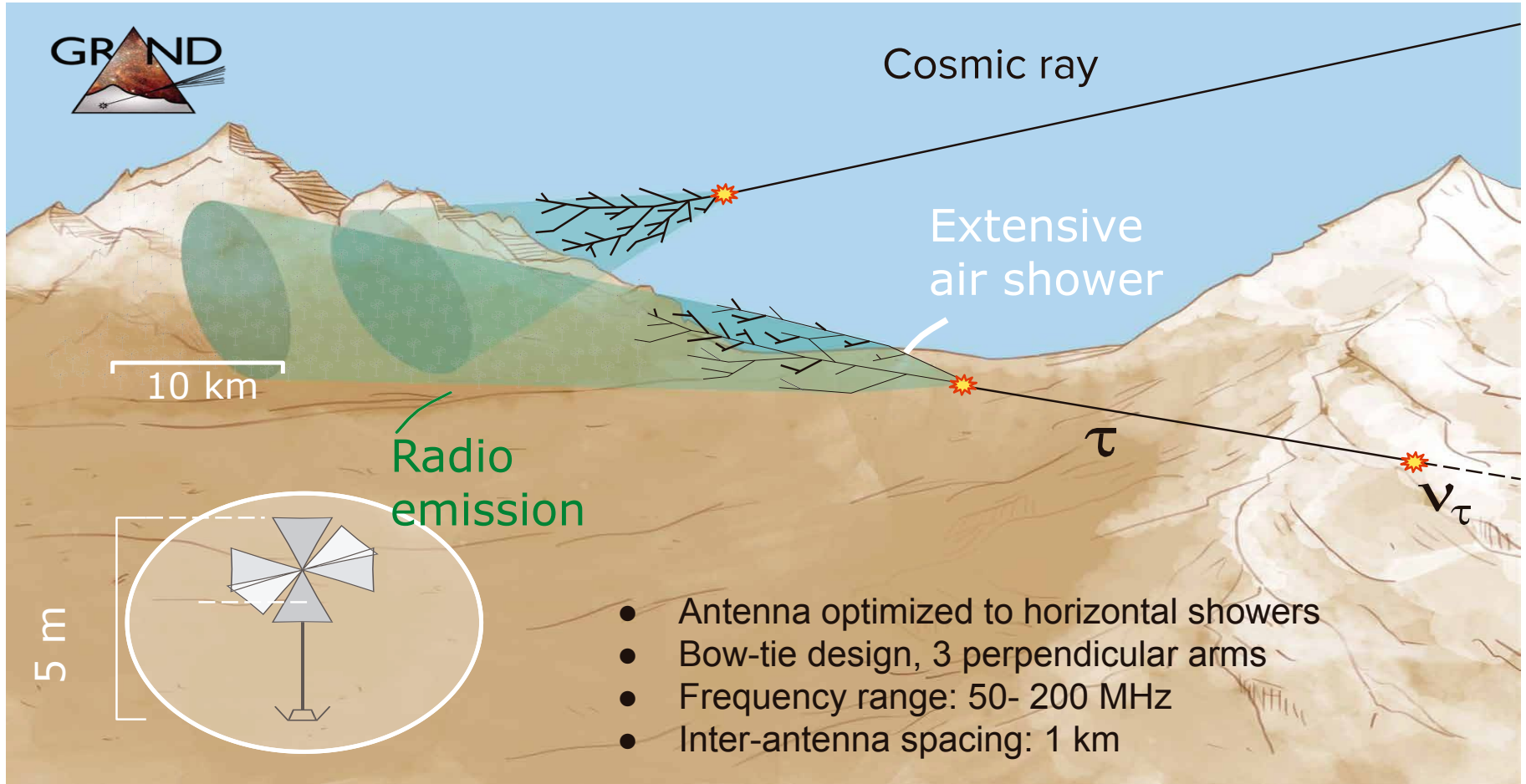
Zachary Mason
(with Oscar Macias & the
GRAND ML working group)

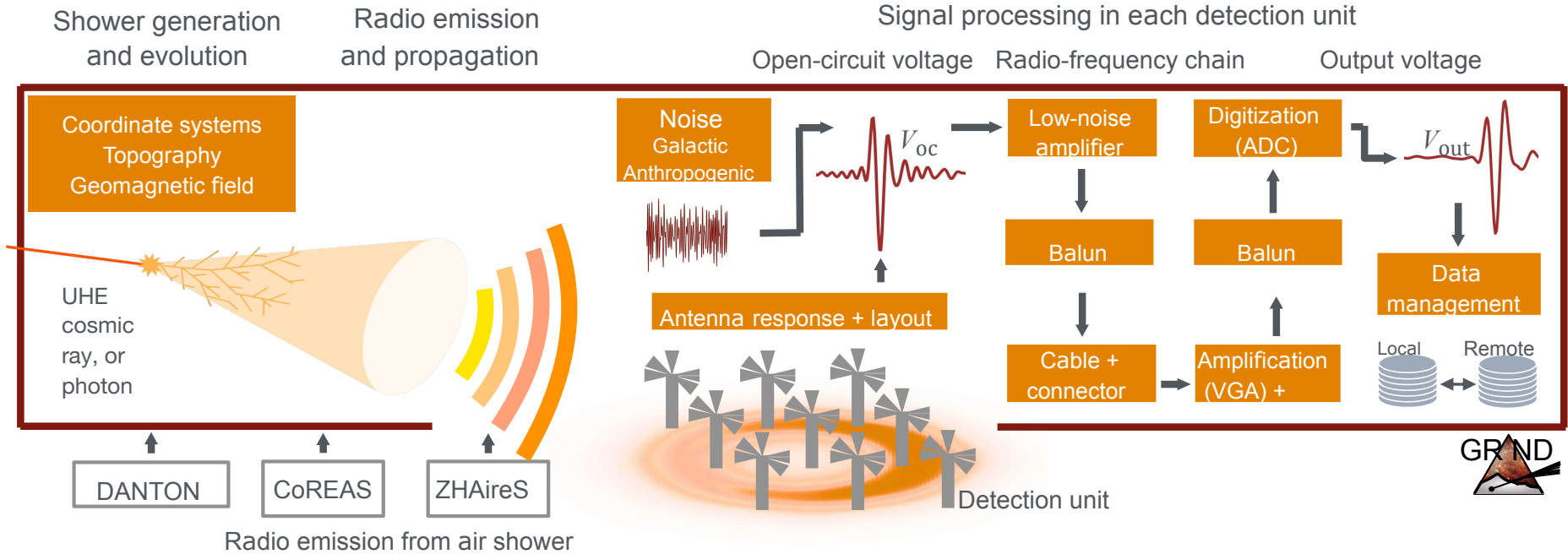
*Workshop on Machine Learning for
Analysis of High-Energy Cosmic Particles*

Jan. 27th, 2025

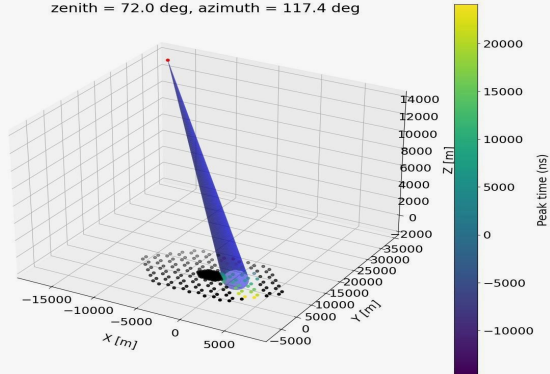
Background

GRAND (Giant Radio Array for Neutrino Detection)

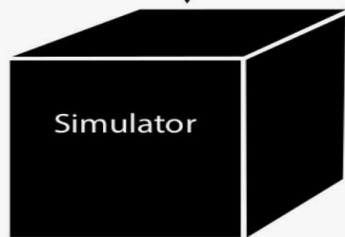




Direction Reconstruction with simulation-based inference (LtU-ILI)



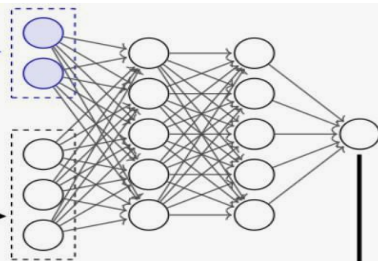
Parameters θ



1. Simulation

~8,000 DC2 Simulations (NJ)
(Filters: events > 5 antennas,
>60 micro-Volt/m)

Observables x



2. Machine Learning

Graph Convolution Network

$\arg \min_g L[g]$

Approximate
likelihood
ratio

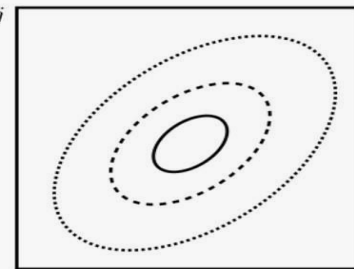
$\hat{r}(x|\theta)$

Observed data

x_{obs}

Prior

θ_j

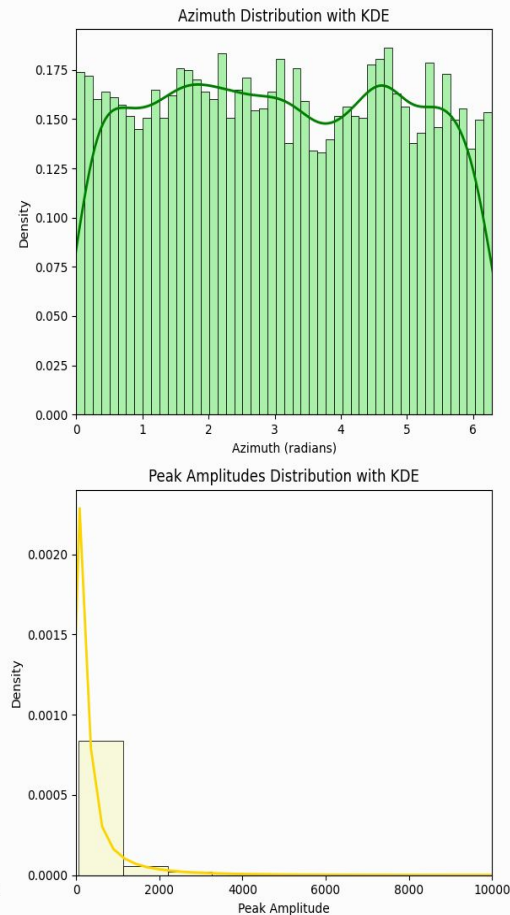
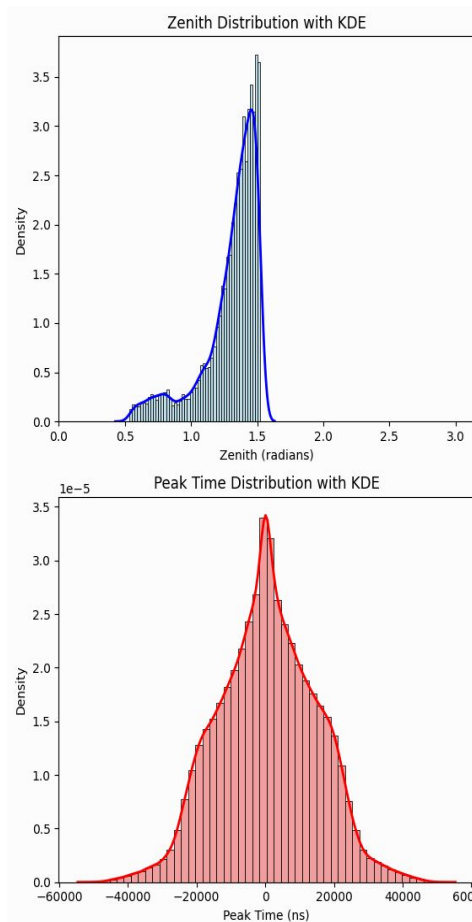


3. Inference

Neural Autoregressive Flow
+
Masked Autoregressive Flow

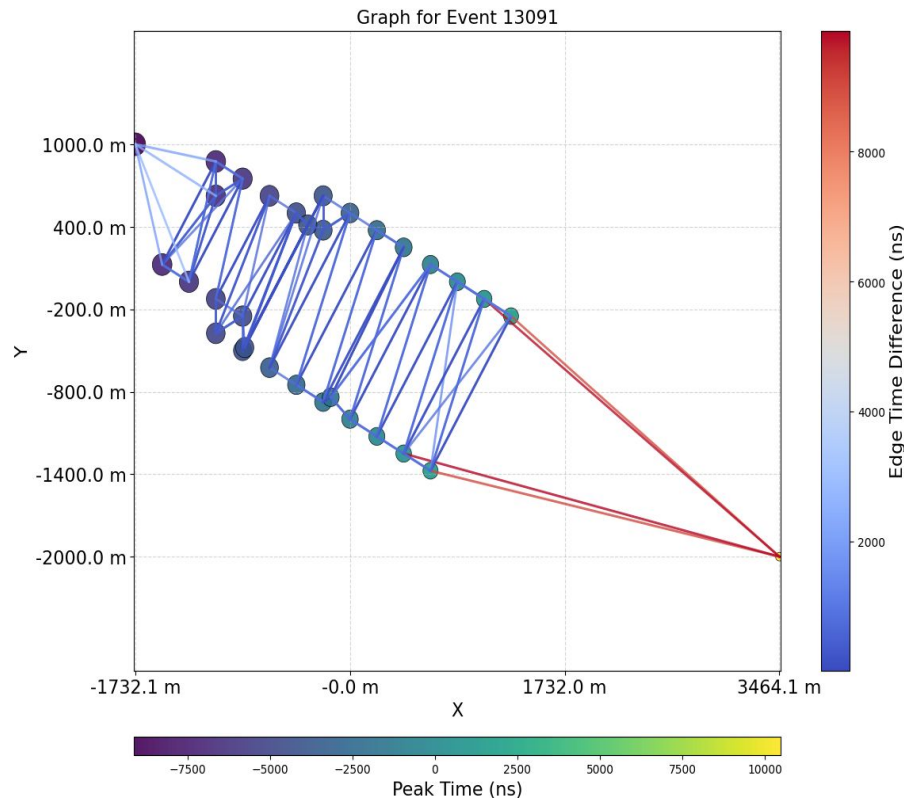
Implementation (DC2 Training Data)

- GRAND Collaboration database of **10,000 ZHAireS simulations**
- Filter simulations based on voltage response level (**>60uV**) and total number of triggered antennas (**>5 antennas**)
- Left with **~8,200 events** for training our GCN



Implementation (Inference)

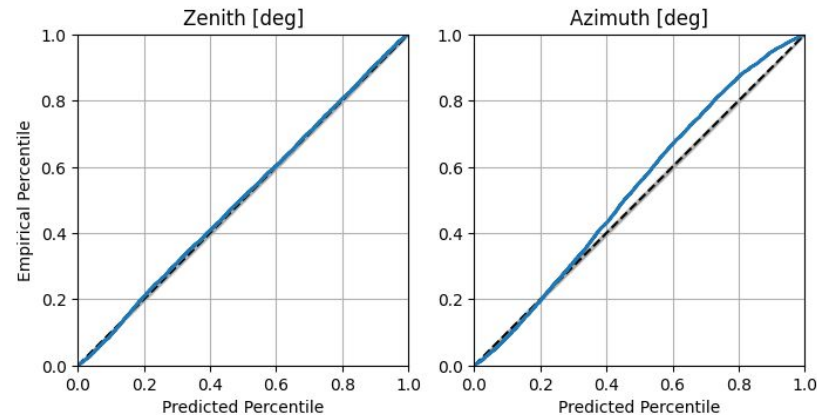
- Pass in a simulated event from DC2 training data to the GCN
 - ◆ **Nodes** created from antenna location & trigger time
 - ◆ **Edges** based on temporal distance between neighboring antennas utilizing k-nearest neighbors (kNN)
- Direction of air-shower is implied from resulting graph architecture
- Outputs posterior distributions of input data-parameter pairs



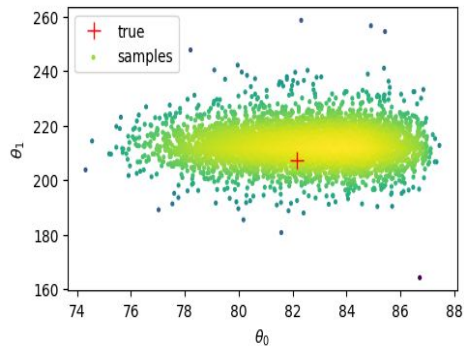
k = 5 nearest neighbors

Implementation (Model Validation)

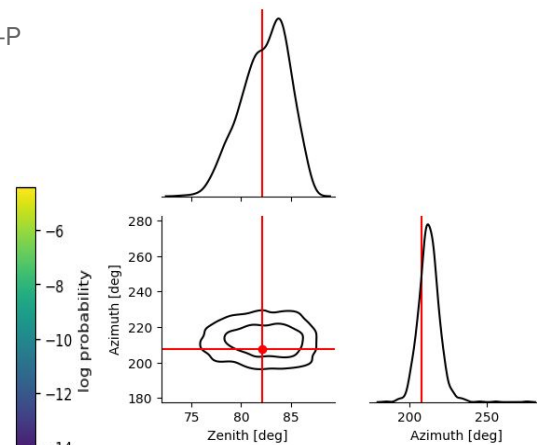
- ~8,200 simulated events (80/20 split for training/validation)
- Takes in posterior distributions from inference step
- Direct comparison to the data-parameter pair distribution from 20% validation dataset



Percentile Coverage Test/P-P plots (error comparison)



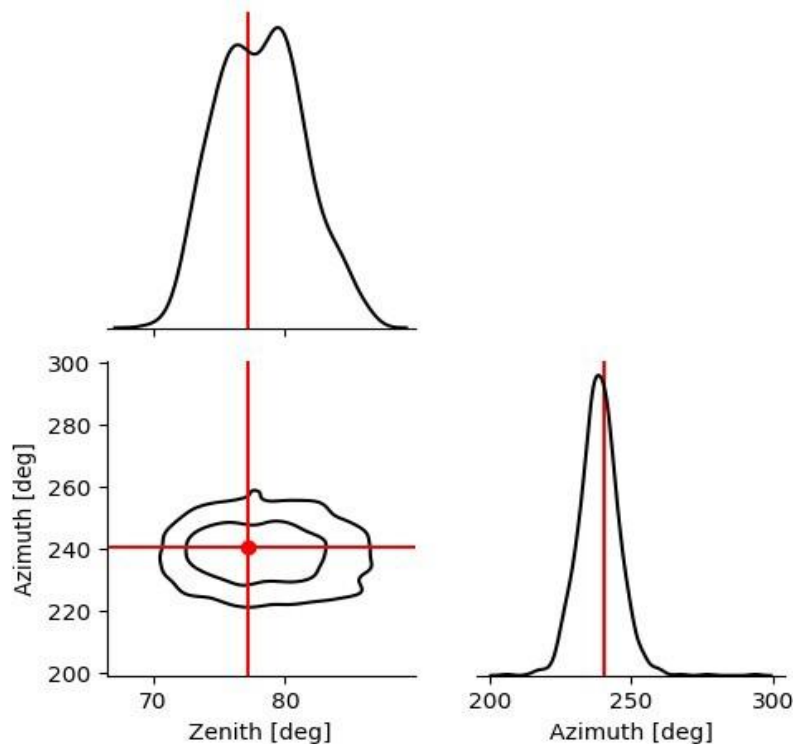
Marginal True vs Predicted Plots



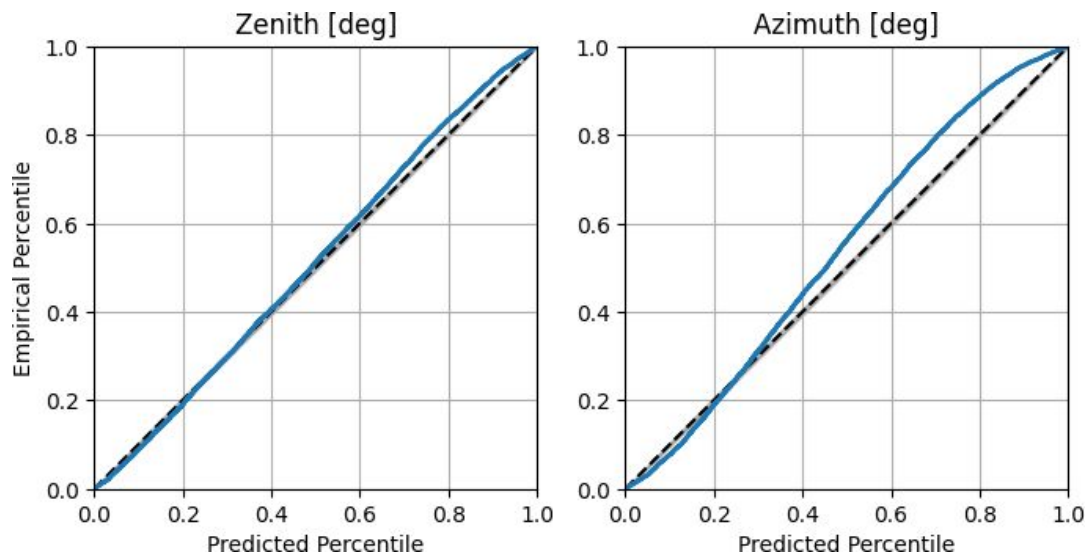
Multivariate corner plots of posterior distributions (model precision)

Preliminary Results

Preliminary Results (data driven)

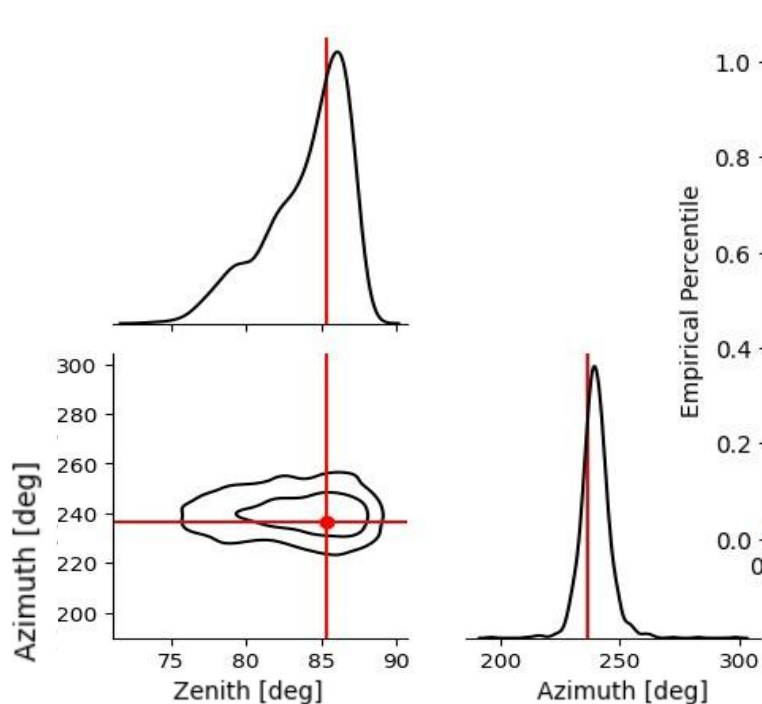


**Direction resolution ~10 deg
(within 1-sigma of true value
indicated by red point)**

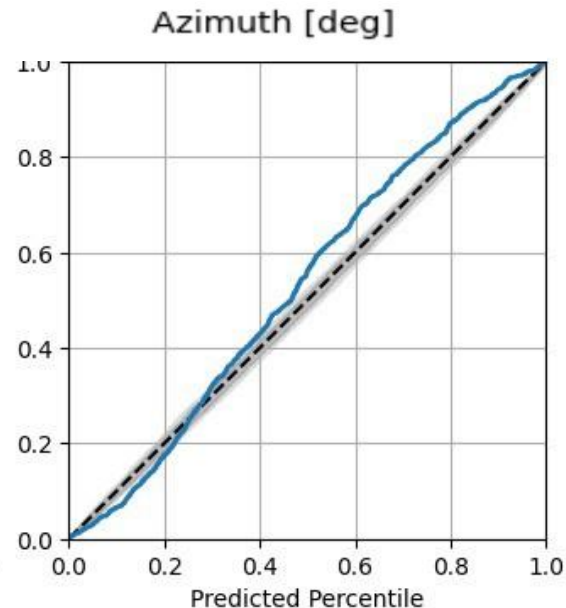
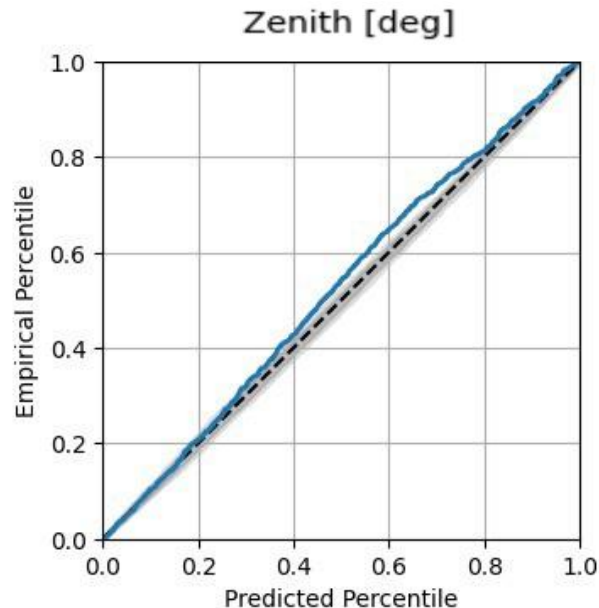


- Tuned k for graph construction, # of channels on GCN, output channels & drop rate
- Best results using:
[$k = 5$, in_channels = 4, gcn_channels = [16,32], out_channels = 8, drop_p = 0.05]

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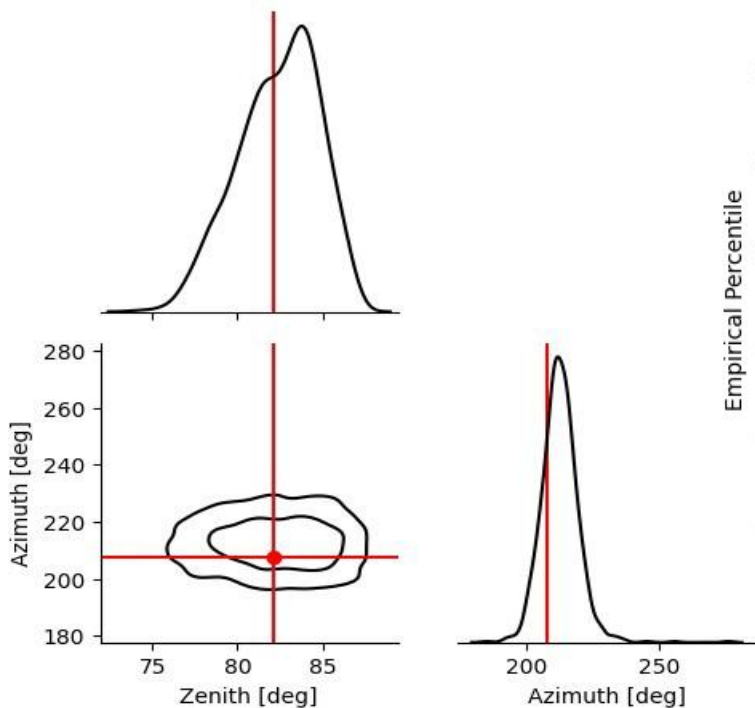


**Direction resolution ~5-10 deg
(within 1-sigma of true value
indicated by red point)**

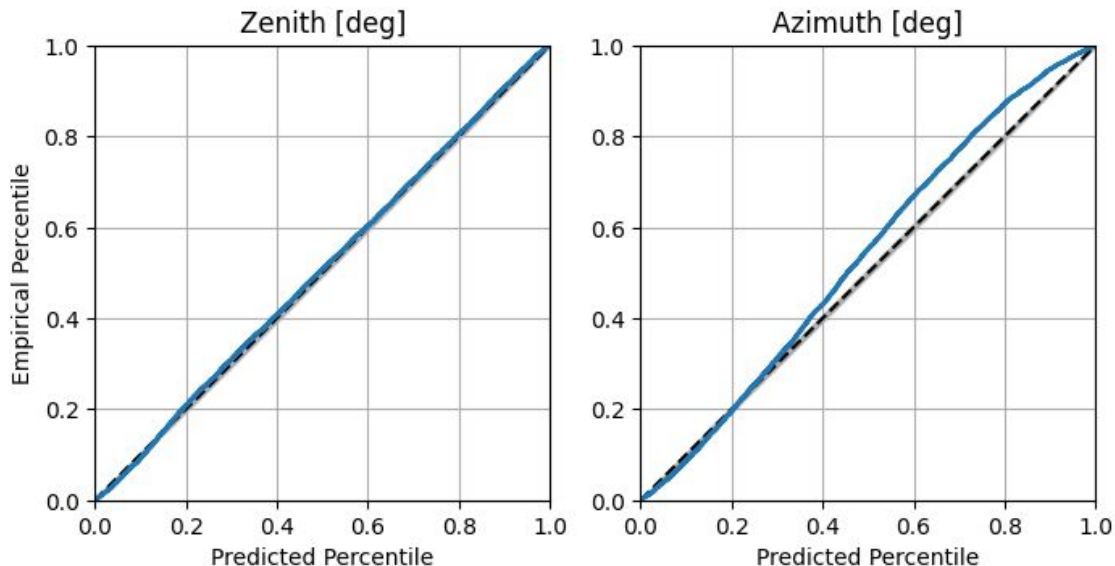


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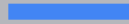
Summary

- Successful implementation of SBI methodology to reconstruct posterior distributions & estimate parameter errors
- Purely data-driven approach correctly reproduces UHE cosmic ray direction within 5-10 degrees resolution

Next Steps

- Implement a physics-informed approach to the ML model, hoping to achieve sub-degree resolution (*cf. Arsene Ferriere talk*).

Thank you!



Backup



Extra

- Using “**lampe**” implicit inference backend offered by LtU-ILI for it’s variety of NDEs & greater flexibility in embedded network choice
- Wanted to use a graph type embedded network given the complexity of the training data
- Best results using GCN:
 - [**k = 5, in_channels = 4, gcn_channels = [16,32], out_channels = 8, drop_p = 0.05**]
- Tried Graph Attention Network (GAT) as embedded network at first, but it struggled to learn the posteriors, mostly recreated entire training data distribution