

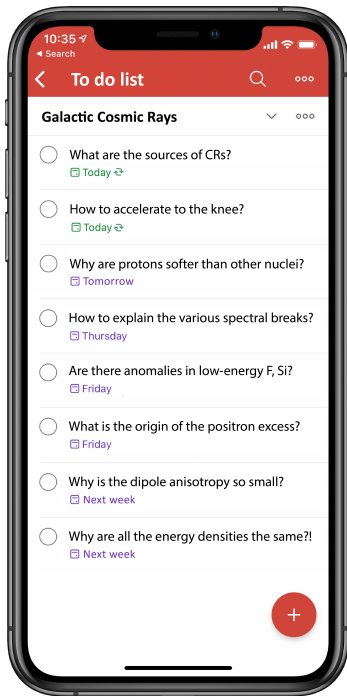
Investigating the CREDIT history of supernova remnants as cosmic-ray sources

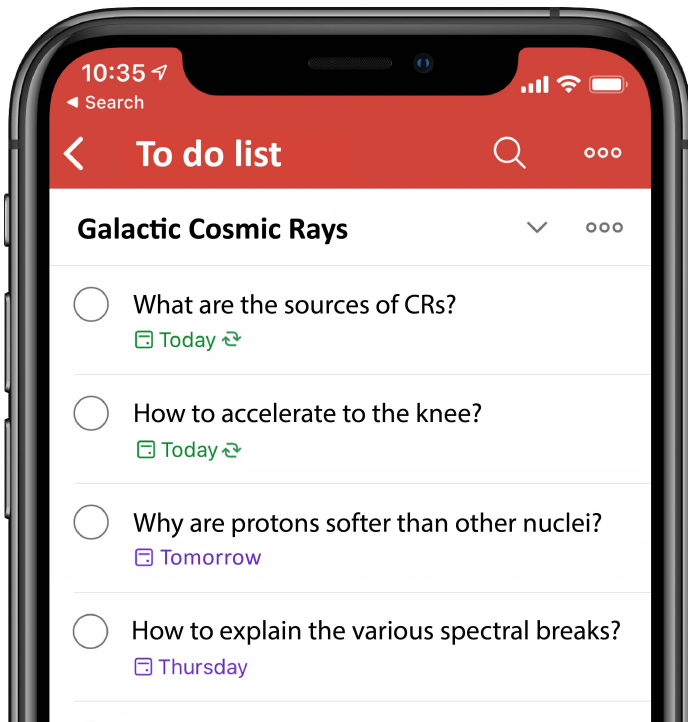
Philipp Mertsch

with Anton Stall and Chun Khai Loo

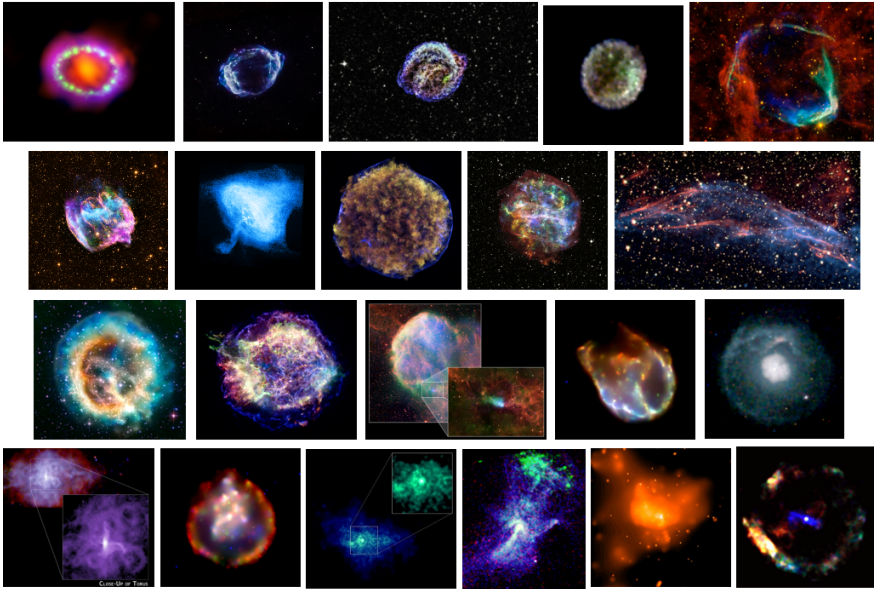
SuGAR 2024

14 October 2024, Madison, WI





Supernova remnants have long been considered the sources of cosmic rays

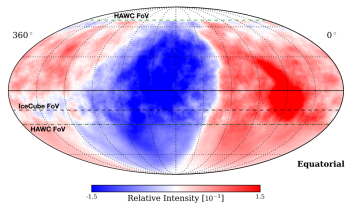


- 1 Observations
- 2 Energetics
- 3 Shock acceleration

Lopez and Fesene (2018)

We do not know individual sources of *local* cosmic rays

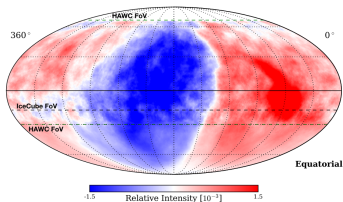
Anisotropies:



Problem: cosmic rays diffuse

We do not know individual sources of *local* cosmic rays

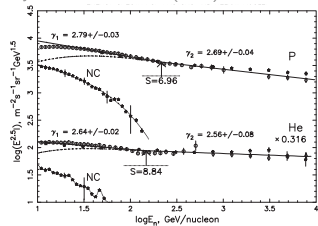
Anisotropies:



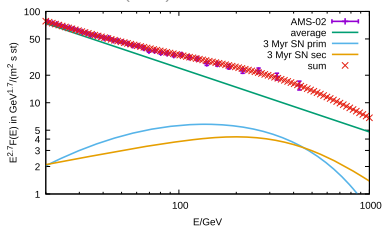
Problem: cosmic rays diffuse

Spectrum:

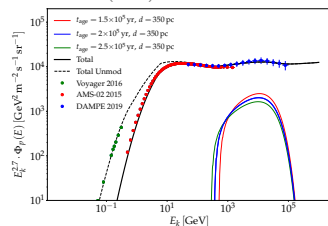
Erlykin and Wolfendale (2012)



Kachelrieß *et al.* (2018)

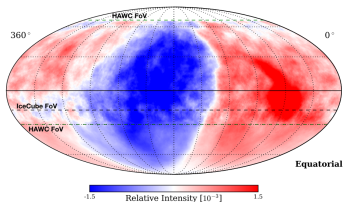


Fornieri *et al.* (2020)



We do not know individual sources of *local* cosmic rays

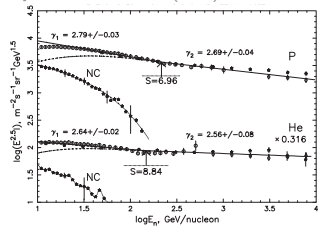
Anisotropies:



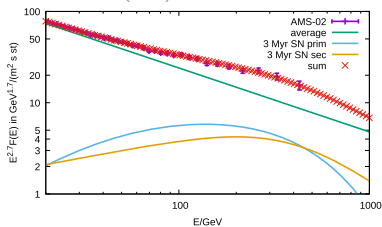
Problem: cosmic rays diffuse

Spectrum:

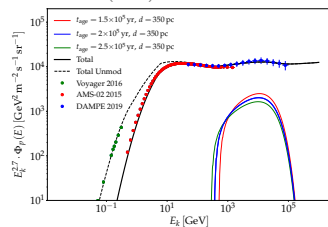
Erlykin and Wolfendale (2012)



Kachelrieß *et al.* (2018)



Fornieri *et al.* (2020)

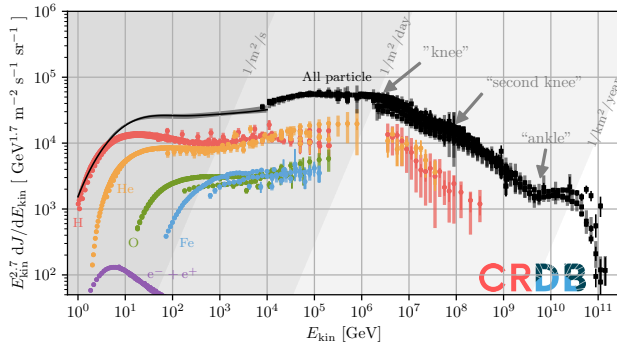


Supernova remnant paradigm

1 000 - 100 000 “active” supernova remnants in the Galaxy

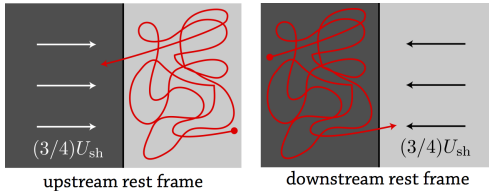
Genolini *et al.* (2017)

Galactic sources should accelerate to E_{knee} , probably via shock acceleration



- $E_{\text{knee}} \simeq 3 \text{ PeV}$:
either maximum energy of source or
change in transport regime
- $E_{\text{max}} \gtrsim 3 \text{ PeV}$ for protons

Axford, Leer, Skadron (1977); Krymskii (1977); Bell (1978); Blandford, Ostriker (1978)



Small energy gain ΔE , little particle loss ΔN
per cycle

$$\left. \begin{aligned} \frac{\Delta E}{E} &\propto \frac{U_{\text{sh}}}{c} \\ \frac{\Delta N}{N} &\propto \frac{U_{\text{sh}}}{c} \end{aligned} \right\} \Rightarrow \frac{dN}{dE} \propto E^{-2}$$

We do not understand how supernova remnants accelerate to E_{knee}

What is E_{max} ?

- Equate age with acceleration time: $t_{\text{age}} = t_{\text{acc}} = 8 \frac{\kappa}{U_{\text{sh}}^2}$ ← Diffusion coefficient

- Assume Bohm diffusion: $\kappa = \frac{c \ell_{\text{mfp}}}{3} = \frac{c r_{\text{g}}}{3} = \frac{c E_{\text{max}}}{3 q B}$ ← Gyro radius

- Hillas-like relation: $\Rightarrow E_{\text{max}} \simeq \frac{U_{\text{sh}}^2}{c} q B t_{\text{age}}$ or $\frac{U_{\text{sh}}}{c} q B R$

We do not understand how supernova remnants accelerate to E_{knee}

What is E_{max} ?

- Equate age with acceleration time: $t_{\text{age}} = t_{\text{acc}} = 8 \frac{\kappa}{U_{\text{sh}}^2}$ ← Diffusion coefficient

- Assume Bohm diffusion: $\kappa = \frac{c \ell_{\text{mfp}}}{3} = \frac{c r_g}{3} = \frac{c E_{\text{max}}}{3 q B}$ ← Gyro radius

- Hillas-like relation: $\Rightarrow E_{\text{max}} \simeq \frac{U_{\text{sh}}^2}{c} q B t_{\text{age}}$ or $\frac{U_{\text{sh}}}{c} q B R$

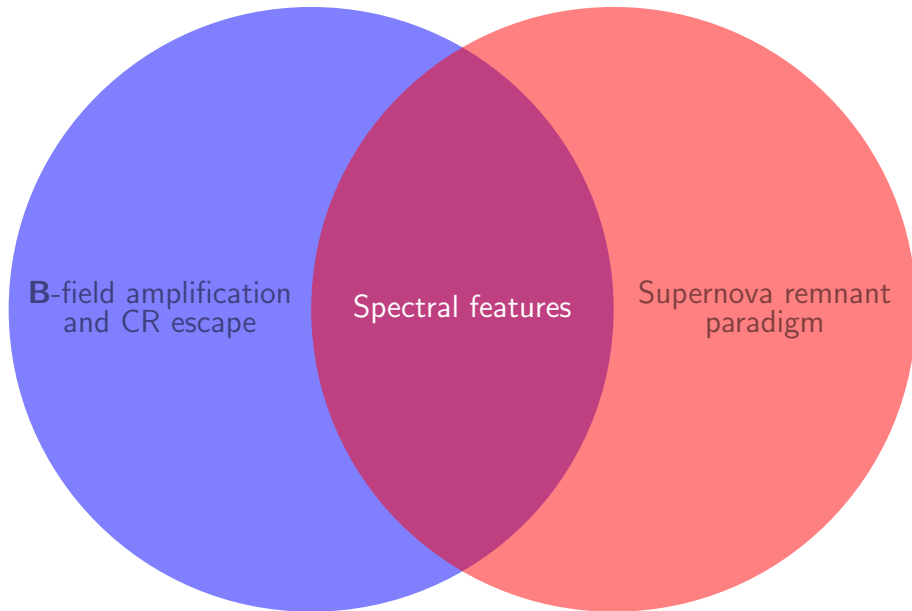
- With typical values: $U_{\text{sh}} = 10^4 \text{ km s}^{-1}$, $B = 1 \mu\text{G}$, $t_{\text{age}} = 10^3 \text{ yr}$

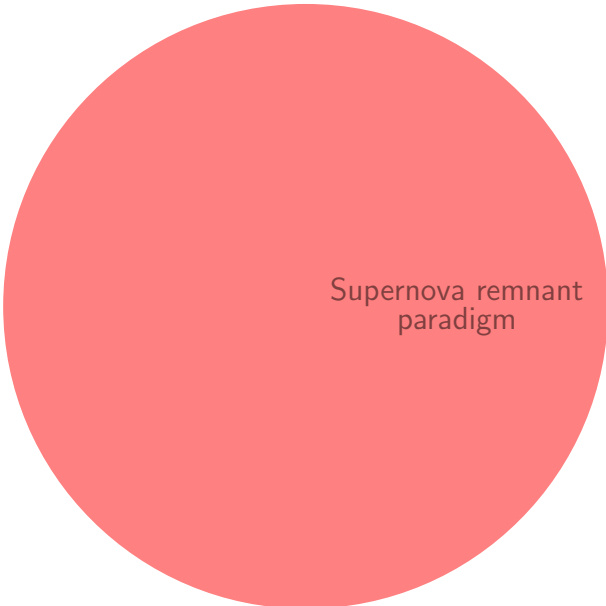
$$\Rightarrow E_{\text{max,b}} \simeq 100 \text{ TeV} \ll E_{\text{knee}}$$

Lagage and Cesarsky (1983)

- 1 Choosing larger t_{age} does not help: $U_{\text{sh}} \propto t_{\text{age}}^{-3/5}$, so E_{max} decreases with time
- 2 Need to amplify **B**-field to $B \simeq 100 \mu\text{G}$

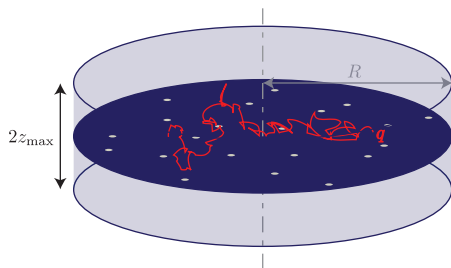
Combining standard ingredients, we predict novel spectral features





Supernova remnant
paradigm

The number of sources contributing to CR flux decreases with energy



- Residence time: $t_{\text{esc}} = \frac{z_{\max}^2}{2\kappa}$
- Diffusion distance: $R = \sqrt{2\kappa t_{\text{esc}}} = z_{\max}$
- Source density: $\sigma = \frac{\nu t_{\text{esc}}}{\pi R_{\text{disk}}^2}$
- Source number: $N_{\text{src}} = \sigma \pi R^2 = \nu t_{\text{esc}} \frac{z_{\max}^2}{R_{\text{disk}}^2}$

With typical parameters (for details → [Appendix](#)):

$$\mathcal{R} = 10 \text{ GV}, \quad 10 \text{ TV}, \quad 10 \text{ PV}$$
$$N_{\text{src}} \simeq 2 \times 10^4, \quad 200, \quad 4$$

Source density is oftentimes considered smooth, while it really is discrete

Transport equation

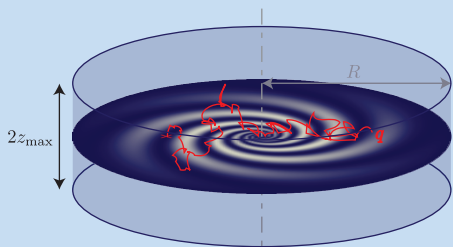
$$\frac{\partial \psi}{\partial t} - \nabla \cdot \kappa \cdot \nabla \psi + \dots = q$$

Source density is oftentimes considered smooth, while it really is discrete

Transport equation

$$\frac{\partial \psi}{\partial t} - \nabla \cdot \kappa \cdot \nabla \psi + \dots = q$$

Smooth source density



$$q = q(\mathbf{r}, t, E) = \nu \rho(\mathbf{r}) Q(E)$$

SN rate

smooth function

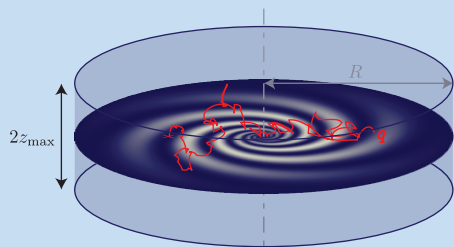
spectrum

Source density is oftentimes considered smooth, while it really is discrete

Transport equation

$$\frac{\partial \psi}{\partial t} - \nabla \cdot \kappa \cdot \nabla \psi + \dots = q$$

Smooth source density



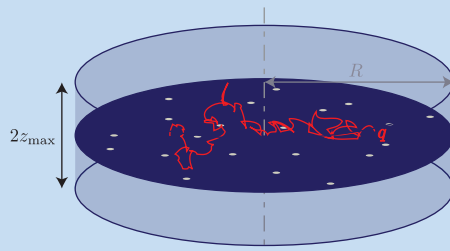
$$q = q(\mathbf{r}, t, E) = \nu \rho(\mathbf{r}) Q(E)$$

SN rate

smooth function

spectrum

Discrete sources



$$q = q(\mathbf{r}, t, E) = \sum_i \delta^{(3)}(\mathbf{r} - \mathbf{r}_i) \delta(t - t_i) Q(E)$$

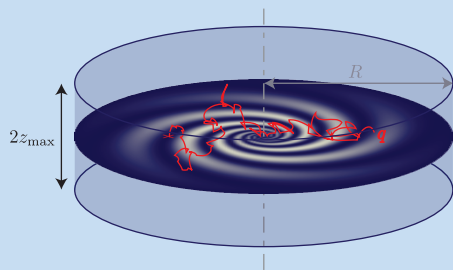
\mathbf{r}_i drawn from $\rho(\mathbf{r})$ and t_i from uniform distribution

Source density is oftentimes considered smooth, while it really is discrete

Transport equation

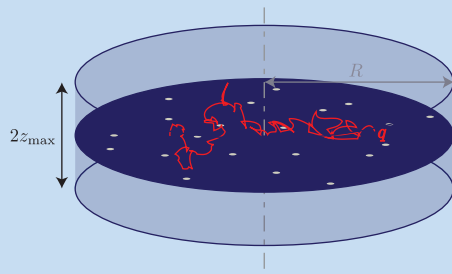
$$\frac{\partial G}{\partial t} - \nabla \cdot \kappa \cdot \nabla G + \dots = \delta^{(3)}(\mathbf{r} - \mathbf{r}_i) \delta(t - t_i) Q(E)$$

Smooth source density



$$q = q(\mathbf{r}, t, E) = \nu \rho(\mathbf{r}) Q(E)$$

Discrete sources



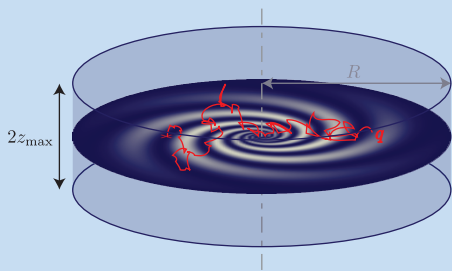
$$q = q(\mathbf{r}, t, E) = \sum_i \delta^{(3)}(\mathbf{r} - \mathbf{r}_i) \delta(t - t_i) Q(E)$$

Source density is oftentimes considered smooth, while it really is discrete

Transport equation

$$\frac{\partial G}{\partial t} - \nabla \cdot \kappa \cdot \nabla G + \dots = \delta^{(3)}(\mathbf{r} - \mathbf{r}_i) \delta(t - t_i) Q(E)$$

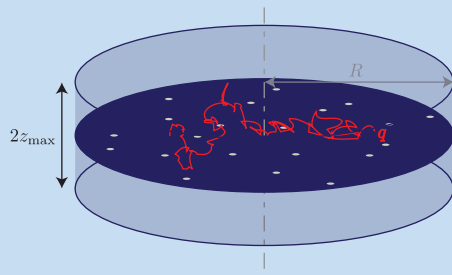
Smooth source density



$$q = q(\mathbf{r}, t, E) = \nu \rho(\mathbf{r}) Q(E)$$

$$\psi(\mathbf{r}, t, E) = \int d^3\mathbf{r}' dt' \nu \rho(\mathbf{r}') G(\mathbf{r} - \mathbf{r}', t - t', E)$$

Discrete sources



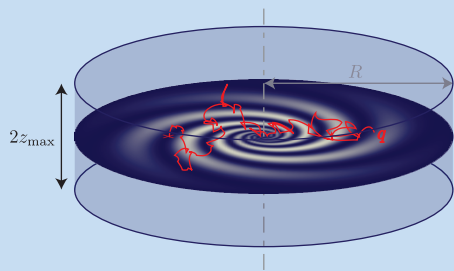
$$q = q(\mathbf{r}, t, E) = \sum_i \delta^{(3)}(\mathbf{r} - \mathbf{r}_i) \delta(t - t_i) Q(E)$$

Source density is oftentimes considered smooth, while it really is discrete

Transport equation

$$\frac{\partial G}{\partial t} - \nabla \cdot \kappa \cdot \nabla G + \dots = \delta^{(3)}(\mathbf{r} - \mathbf{r}_i) \delta(t - t_i) Q(E)$$

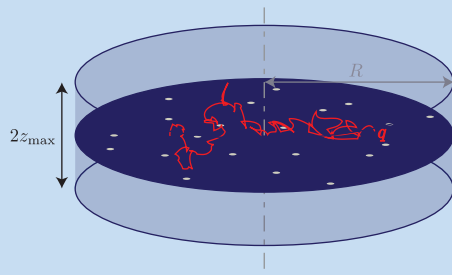
Smooth source density



$$q = q(\mathbf{r}, t, E) = \nu \rho(\mathbf{r}) Q(E)$$

$$\psi(\mathbf{r}, t, E) = \int d^3\mathbf{r}' dt' \nu \rho(\mathbf{r}') G(\mathbf{r} - \mathbf{r}', t - t', E)$$

Discrete sources



$$q = q(\mathbf{r}, t, E) = \sum_i \delta^{(3)}(\mathbf{r} - \mathbf{r}_i) \delta(t - t_i) Q(E)$$

$$\psi(\mathbf{r}, t, E) = \sum_i G(\mathbf{r} - \mathbf{r}_i, t - t_i, E)$$

Stochastic nature of sources implies fluctuations in spectrum

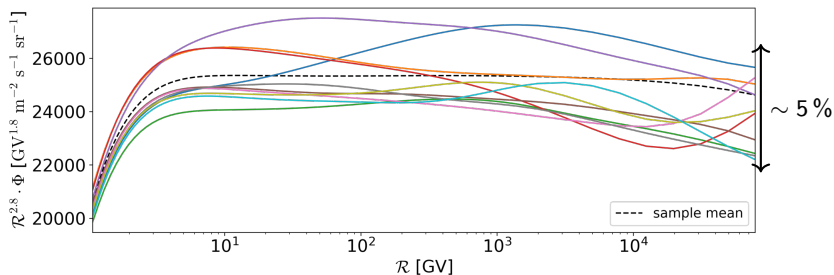
- Solution:
$$\psi(\mathbf{r}, t, p) = \sum_i G(\mathbf{r} - \mathbf{r}_i, t - t_i, E)$$
- \mathbf{r}_i, t_i are random variables $\Rightarrow \psi(\mathbf{r}, t, p)$ is random variable
- Mean:
$$\langle \psi(\mathbf{x}, t, p) \rangle = \int d^3\mathbf{r}' dt' \nu \rho(\mathbf{r}') G(\mathbf{r} - \mathbf{r}', t - t', E)$$

Can we use $\psi - \langle \psi \rangle$ to find sources?

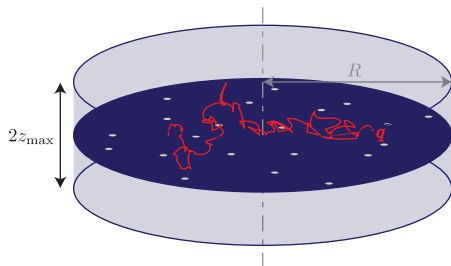
Stochastic nature of sources implies fluctuations in spectrum

- Solution:
$$\psi(\mathbf{r}, t, p) = \sum_i G(\mathbf{r} - \mathbf{r}_i, t - t_i, E)$$
- \mathbf{r}_i, t_i are random variables $\Rightarrow \psi(\mathbf{r}, t, p)$ is random variable
- Mean:
$$\langle \psi(\mathbf{x}, t, p) \rangle = \int d^3\mathbf{r}' dt' \nu \rho(\mathbf{r}') G(\mathbf{r} - \mathbf{r}', t - t', E)$$

Can we use $\psi - \langle \psi \rangle$ to find sources?



The number of sources contributing to CR flux decreases with sharply energy



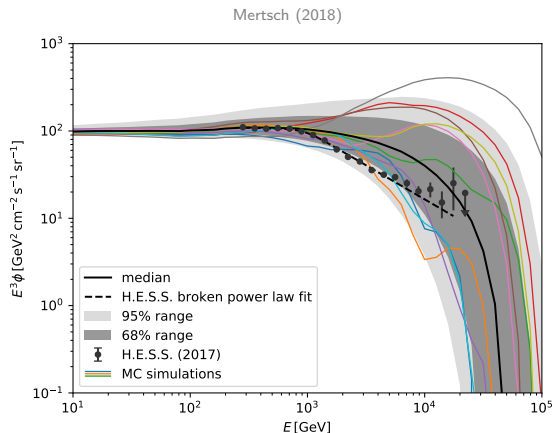
- Residence time: $t_{\text{cool}} = \frac{E}{\dot{E}}$
- Diffusion distance: $R = \sqrt{2\kappa t_{\text{cool}}}$
- Source density: $\sigma = \frac{\nu t_{\text{cool}}}{\pi R_{\text{disk}}^2}$
- Source number: $N_{\text{src}} = \sigma \pi R^2 = \nu t_{\text{cool}} \frac{2\kappa t_{\text{cool}}}{R_{\text{disk}}^2}$

With typical parameters (for details → [Appendix](#)):

$$\mathcal{R} = 10 \text{ GV}, \quad 10 \text{ TV}, \quad 10 \text{ PV}$$
$$N_{\text{src}} \simeq 2 \times 10^4, \quad 1, \quad 10^{-4}$$

Electrons and positrons at high energies

- Sensitivity to source distances and ages
- Need to consider when comparing to data
- Great potential for identifying sources



Monte Carlo study

- 1 Draw random distances $\{d_i\}$ and ages $\{t_i\}$
- 2 Add contributions from $i = 1, \dots, N_{\text{SRC}}$ sources in *one realisation* of the Galaxy
- 3 Repeat for *different realisations* of the Galaxy

Density estimation task

N. Frediani, M. Krämer, K. Nippel, P. Mertsch

- Have discrete samples of flux vector $\{\phi_1, \phi_2, \dots, \phi_N\}$
 - Want multivariate distribution $p(\phi_1, \phi_2, \dots, \phi_N)$
- Density estimation task

Conditional probabilities

$$p(\phi_1, \phi_2, \dots, \phi_N) = p(\phi_1)p(\phi_2|\phi_1) \dots p(\phi_N|\phi_1, \dots, \phi_{N-1})$$

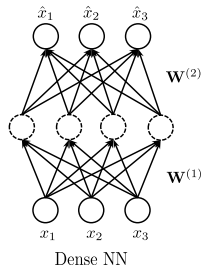
Density estimation task

N. Frediani, M. Krämer, K. Nippel, P. Mertsch

- Have discrete samples of flux vector $\{\phi_1, \phi_2, \dots, \phi_N\}$
 - Want multivariate distribution $p(\phi_1, \phi_2, \dots, \phi_N)$
- Density estimation task

Conditional probabilities

$$p(\phi_1, \phi_2, \dots, \phi_N) = p(\phi_1)p(\phi_2|\phi_1) \dots p(\phi_N|\phi_1, \dots, \phi_{N-1})$$



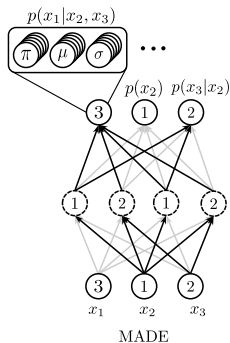
Density estimation task

N. Frediani, M. Krämer, K. Nippel, P. Mertsch

- Have discrete samples of flux vector $\{\phi_1, \phi_2, \dots, \phi_N\}$
 - Want multivariate distribution $p(\phi_1, \phi_2, \dots, \phi_N)$
- Density estimation task

Conditional probabilities

$$p(\phi_1, \phi_2, \dots, \phi_N) = p(\phi_1)p(\phi_2|\phi_1) \dots p(\phi_N|\phi_1, \dots, \phi_{N-1})$$



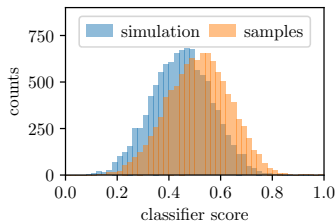
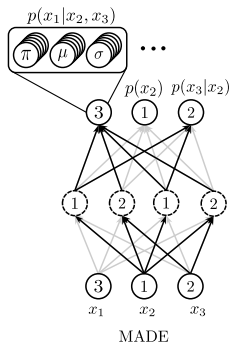
Density estimation task

N. Frediani, M. Krämer, K. Nippel, P. Mertsch

- Have discrete samples of flux vector $\{\phi_1, \phi_2, \dots, \phi_N\}$
 - Want multivariate distribution $p(\phi_1, \phi_2, \dots, \phi_N)$
- Density estimation task

Conditional probabilities

$$p(\phi_1, \phi_2, \dots, \phi_N) = p(\phi_1)p(\phi_2|\phi_1) \dots p(\phi_N|\phi_1, \dots, \phi_{N-1})$$

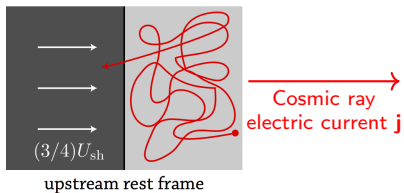




B-field amplification
and CR escape

The Bell instability can amplify B-fields

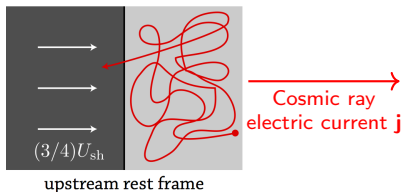
Bell (2004)



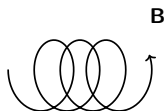
- If B -field too weak, particles escape
- Electric current \mathbf{j}
- Waves modes unstable in the presence of current \mathbf{j}

The Bell instability can amplify B-fields

Bell (2004)



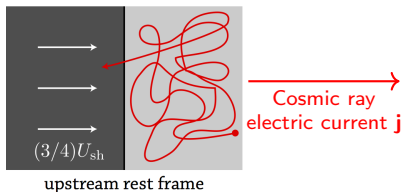
- If B -field too weak, particles escape
- Electric current \mathbf{j}
- Waves modes unstable in the presence of current \mathbf{j}



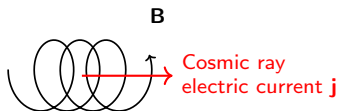
- CRs with gyroradius r_g tied to field lines
- Instability saturates once $\lambda \sim r_g$
- \mathbf{B} -field density satisfies $\epsilon_B \sim \frac{U_{sh}}{c} \epsilon_{CR}$

The Bell instability can amplify B-fields

Bell (2004)



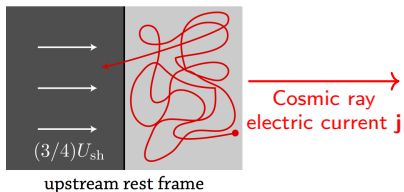
- If B -field too weak, particles escape
- Electric current \mathbf{j}
- Waves modes unstable in the presence of current \mathbf{j}



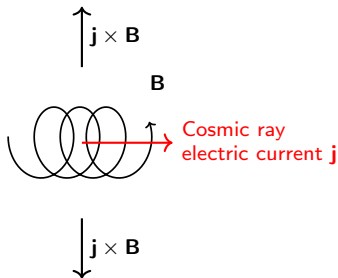
- CRs with gyroradius r_g tied to field lines
- Instability saturates once $\lambda \sim r_g$
- \mathbf{B} -field density satisfies $\epsilon_B \sim \frac{U_{sh}}{c} \epsilon_{CR}$

The Bell instability can amplify B-fields

Bell (2004)



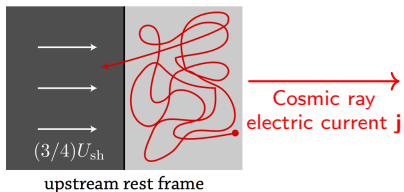
- If B -field too weak, particles escape
- Electric current \mathbf{j}
- Waves modes unstable in the presence of current \mathbf{j}



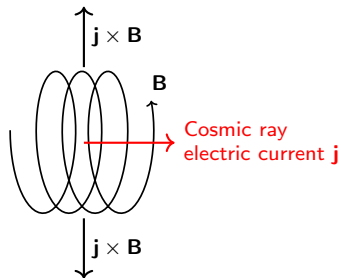
- CRs with gyroradius r_g tied to field lines
- Instability saturates once $\lambda \sim r_g$
- B -field density satisfies $\epsilon_B \sim \frac{U_{sh}}{c} \epsilon_{CR}$

The Bell instability can amplify B-fields

Bell (2004)



- If B -field too weak, particles escape
- Electric current \mathbf{j}
- Waves modes unstable in the presence of current \mathbf{j}



- CRs with gyroradius r_g tied to field lines
- Instability saturates once $\lambda \sim r_g$
- B -field density satisfies $\epsilon_B \sim \frac{U_{sh}}{c} \epsilon_{CR}$

Bell instability makes optimal use of $\mathbf{j} \times \mathbf{B}$ force

Slide concept: T. Bell

- Growth rate: $\gamma \sim \sqrt{\frac{jBk}{\rho}}$ or $\frac{\gamma^2}{k} \sim \frac{jB}{\rho}$
- Compare to acceleration of fluid element of size $z \sim 1/k$ in time $t \sim 1/\gamma$:

$$\frac{z}{t^2} \sim \frac{1}{\rho} |\mathbf{j} \times \mathbf{B}| \lesssim \frac{jB}{\rho} \quad \rightarrow \quad \frac{\gamma^2}{k} \lesssim \frac{jB}{\rho}$$

Wave number



Bell instability makes optimal use of $\mathbf{j} \times \mathbf{B}$ force

Slide concept: T. Bell

- Growth rate:

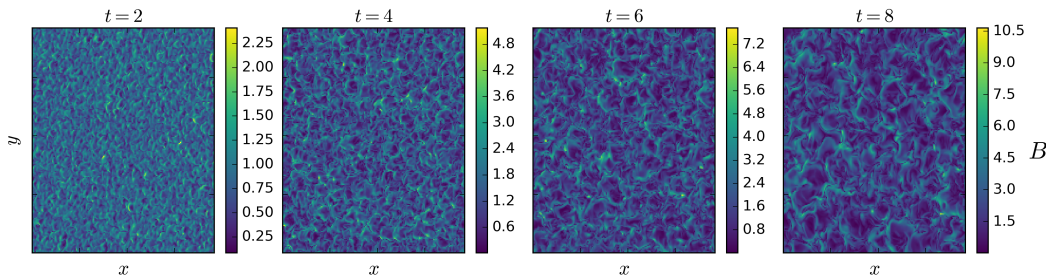
$$\gamma \sim \sqrt{\frac{jBk}{\rho}} \quad \text{or} \quad \frac{\gamma^2}{k} \sim \frac{jB}{\rho}$$

Wave number

- Compare to acceleration of fluid element of size $z \sim 1/k$ in time $t \sim 1/\gamma$:

$$\frac{z}{t^2} \sim \frac{1}{\rho} |\mathbf{j} \times \mathbf{B}| \lesssim \frac{jB}{\rho} \quad \rightarrow \quad \frac{\gamma^2}{k} \lesssim \frac{jB}{\rho}$$

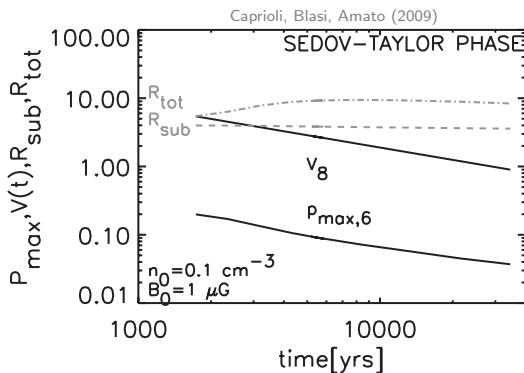
Matthews *et al.* (2017)



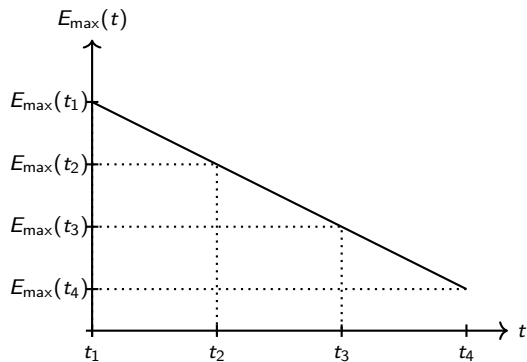
Grows rapidly on small scales

The highest CR energies can be achieved at start of Sedov-Taylor phase

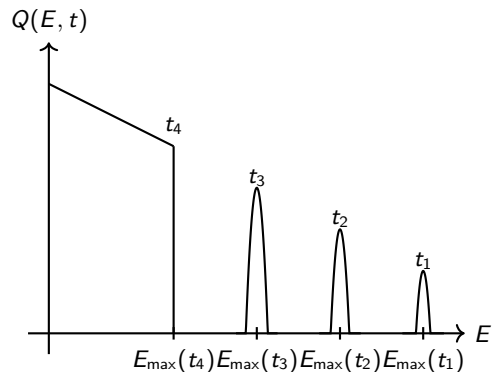
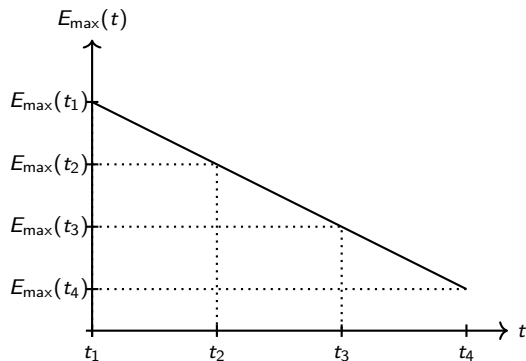
- Shock speed U_{sh} enters into growth rate γ through escape current j
 - Saturation field $B \propto U_{\text{sh}}^{3/2}$
 - $U_{\text{sh}} \propto t_{\text{age}}^{-3/5}$
- $E_{\text{max}} \propto U_{\text{sh}}^2 B t_{\text{age}} \propto t_{\text{age}}^{-11/10}$



Time-dependence of B-field amplification determines CR escape



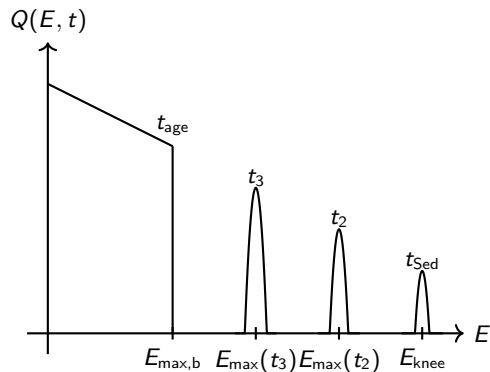
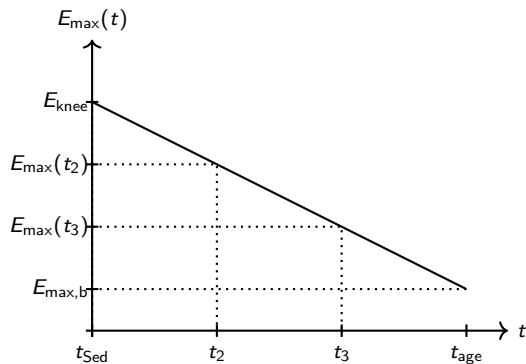
Time-dependence of B-field amplification determines CR escape



also Gabici, Aharonian, Casanova (2009); Caprioli, Blasi, Amato (2010);
Blasi and Amato (2012); Thoudam and Hörandel (2012)

- E_{\max} decreases with time
- At any one time t , particles of energy $E_{\max}(t)$ escape
- Ultimately, all particles with $E < E_{\max,b}$ escape

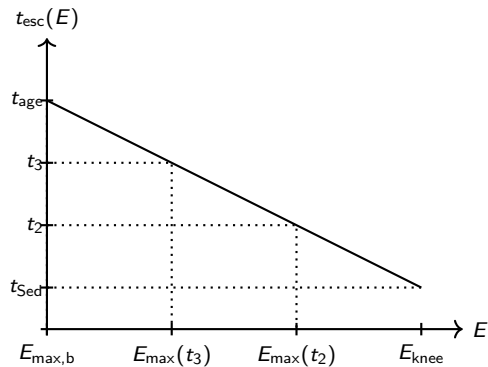
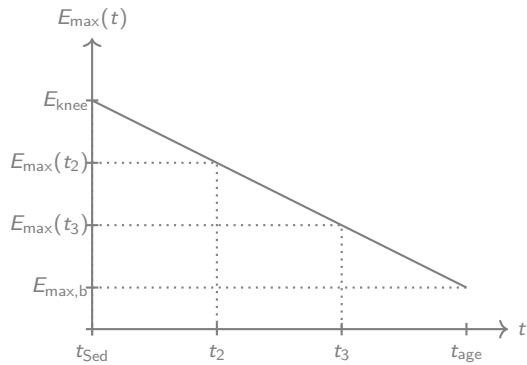
Time-dependence of B-field amplification determines CR escape



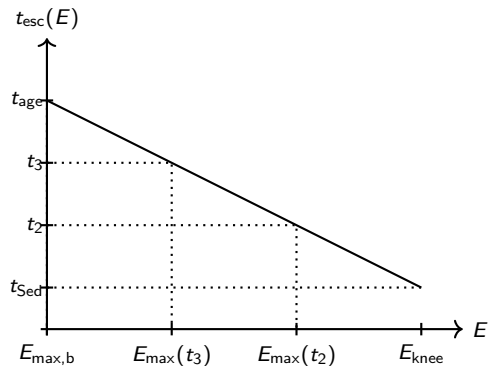
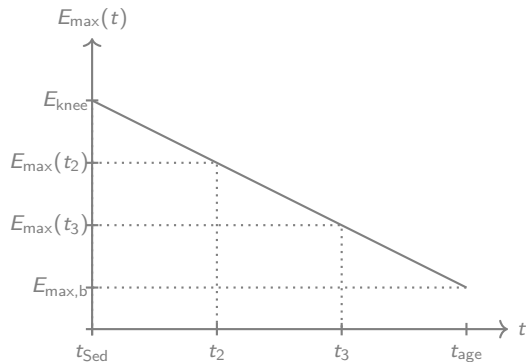
also Gabici, Aharonian, Casanova (2009); Caprioli, Blasi, Amato (2010);
Blasi and Amato (2012); Thoudam and Hörandel (2012)

- E_{\max} decreases with time
- At any one time t , particles of energy $E_{\max}(t)$ escape
- Ultimately, all particles with $E < E_{\max,b}$ escape

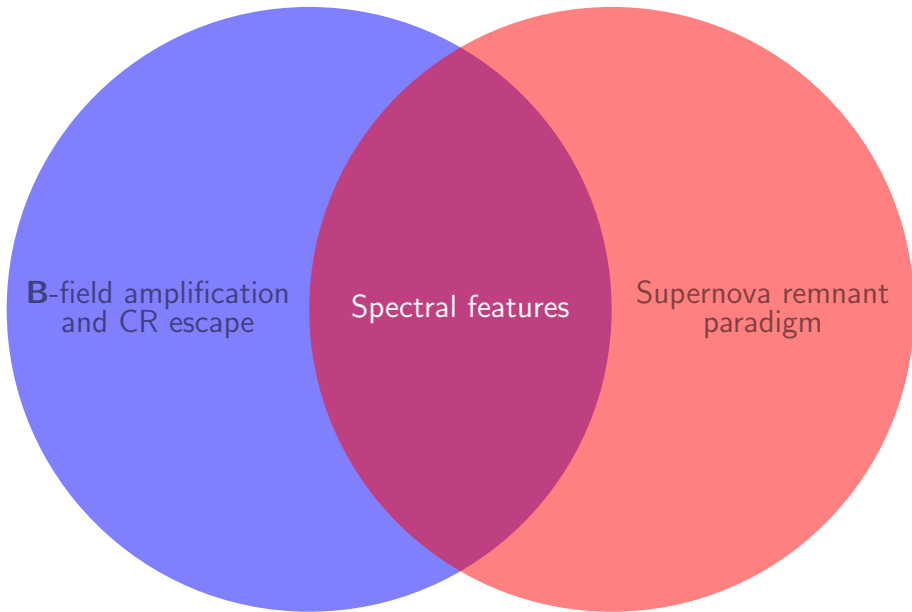
Time-dependence of B-field amplification determines CR escape



Time-dependence of B-field amplification determines CR escape

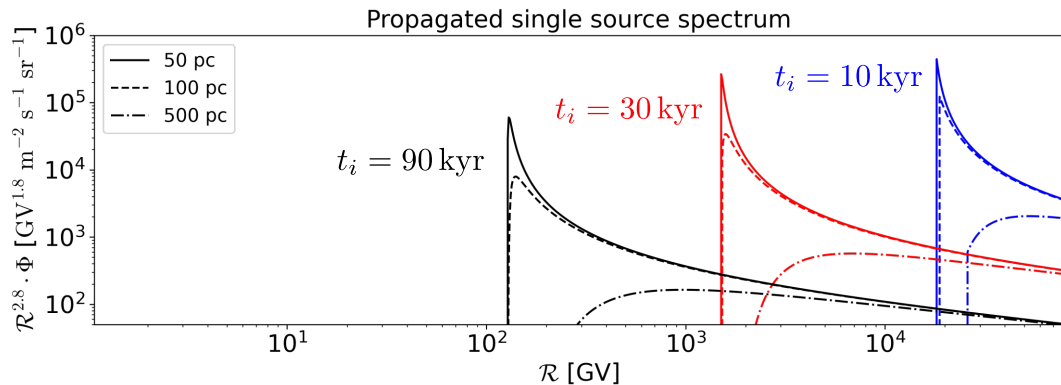


Cosmic-Ray **Energy-Dependent Injection Time**
(CREDIT) scenario



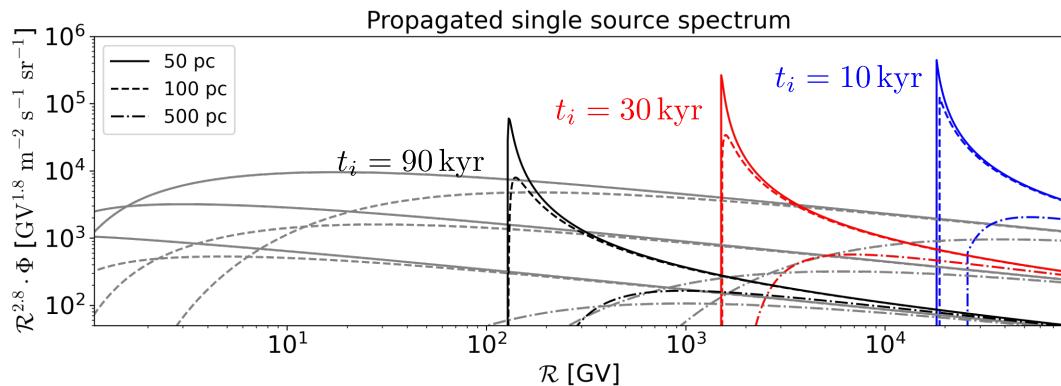
The Green's function has narrow spectral features

$$\frac{\partial G}{\partial t} - \nabla \cdot \kappa \cdot \nabla G = \delta^{(3)}(\mathbf{r} - \mathbf{r}_i) \delta(t - t_i - t_{\text{esc}}(E)) Q(E)$$



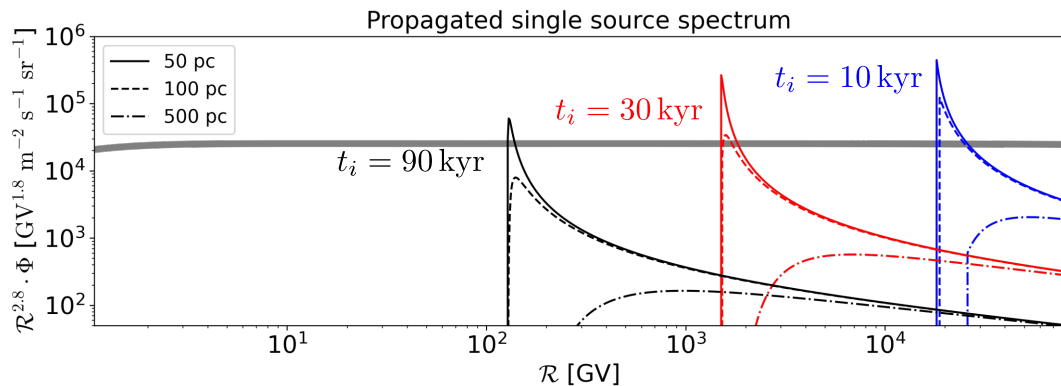
The Green's function has narrow spectral features

$$\frac{\partial G}{\partial t} - \nabla \cdot \kappa \cdot \nabla G = \delta^{(3)}(\mathbf{r} - \mathbf{r}_i) \delta(t - t_i - t_{\text{esc}}(E)) Q(E)$$



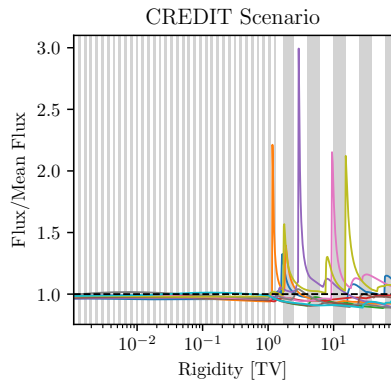
The Green's function has narrow spectral features

$$\frac{\partial G}{\partial t} - \nabla \cdot \kappa \cdot \nabla G = \delta^{(3)}(\mathbf{r} - \mathbf{r}_i) \delta(t - t_i - t_{\text{esc}}(E)) Q(E)$$



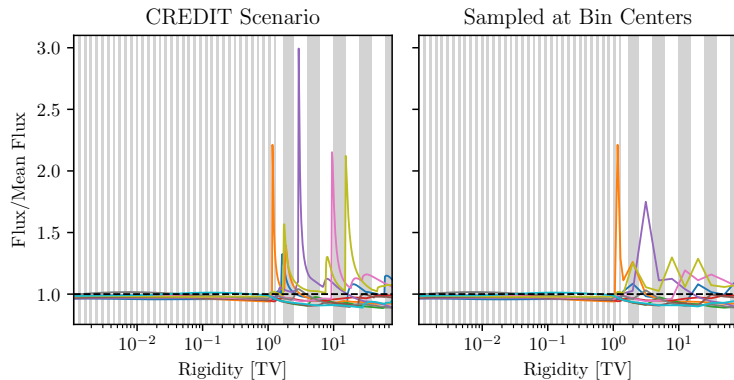
CREDIT scenario predicts dramatic spectral features

Stall, Loo, Mertsch, arXiv:2409.11012



CREDIT scenario predicts dramatic spectral features

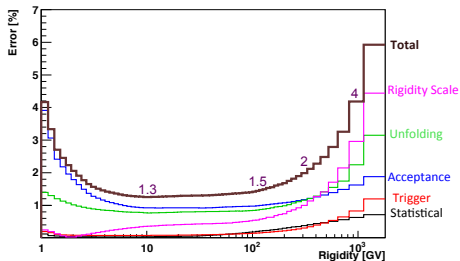
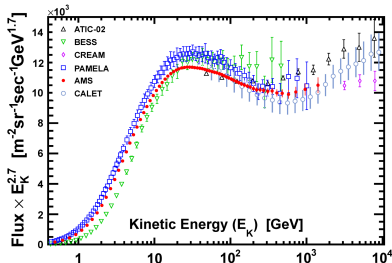
Stall, Loo, Mertsch, arXiv:2409.11012



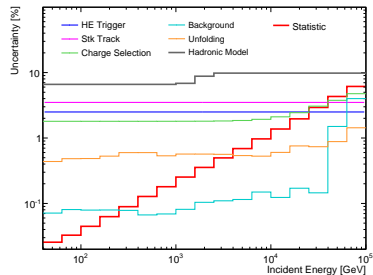
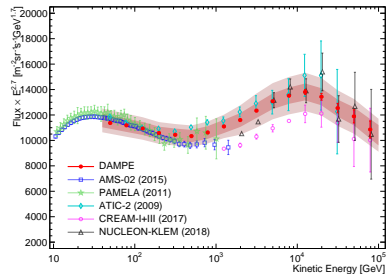
Modern proton data offer unprecedented accuracy

V. Choutko (2015), An *et al.* (2019), Aguilar *et al.* (2020),

AMS-02

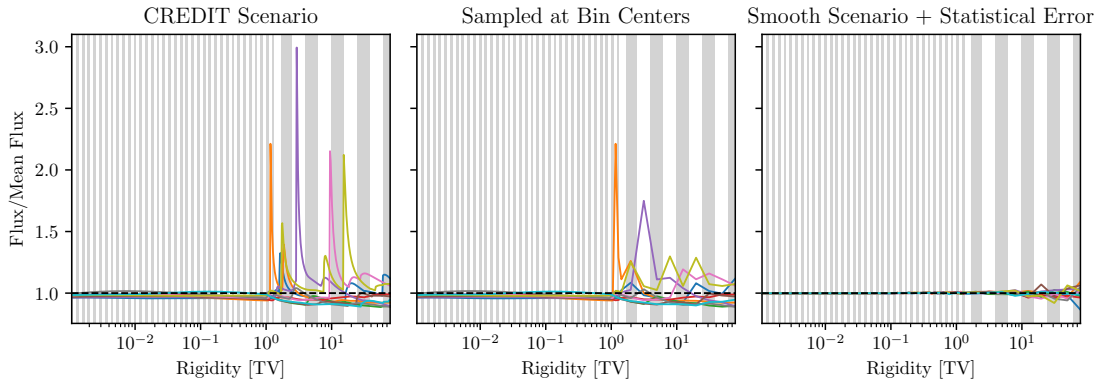


DAMPE



Statistical errors are much smaller than CREDIT features

Stall, Loo, Mertsch, arXiv:2409.11012

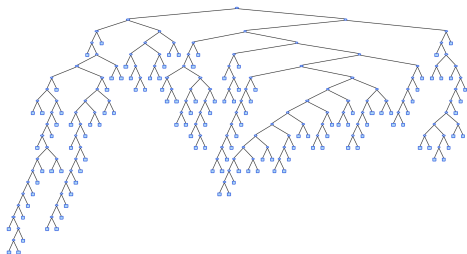


We can confidently discriminate between the different scenarios

Stall, Loo, Mertsch, arXiv:2409.11012

Can discriminate features
from statistical fluctuations?

→ Classical machine learning task



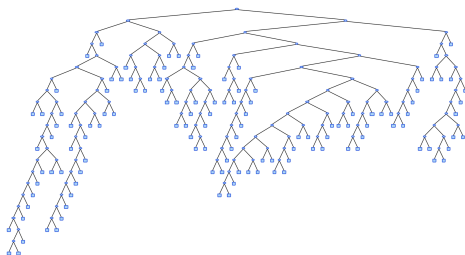
Decision tree

We can confidently discriminate between the different scenarios

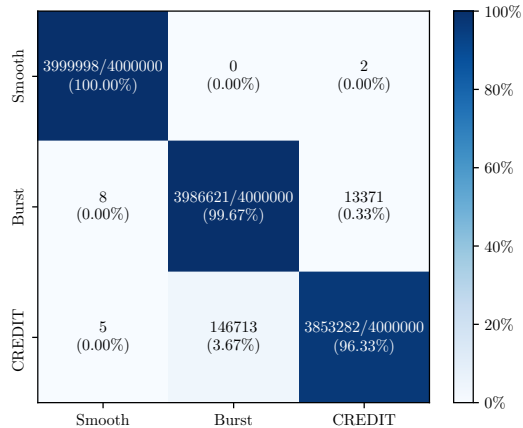
Stall, Loo, Mertsch, arXiv:2409.11012

Can discriminate features
from statistical fluctuations?

→ Classical machine learning task



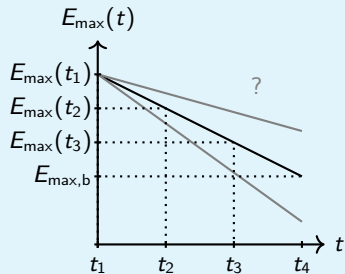
Decision tree



The classification is very robust

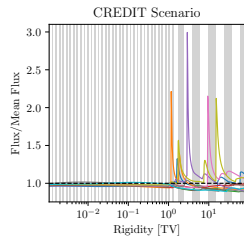
Stall, Loo, Mertsch, arXiv:2409.11012

$E_{\max,b}$ unknown



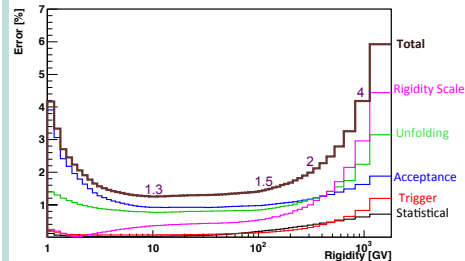
→ $E_{\max,b}$ varied in training

Finite bin widths



→ Integrate over bins

Systematic errors

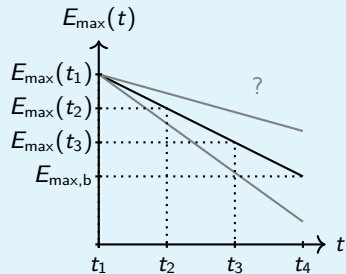


→ 1% uncorrelated systematic errors included Aguilar *et al.* (2015); Cavasonza *et al.* (2018)

The classification is very robust

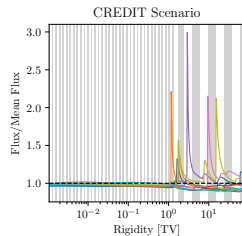
Stall, Loo, Mertsch, arXiv:2409.11012

$E_{\max,b}$ unknown



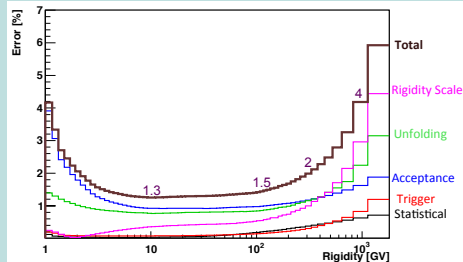
→ $E_{\max,b}$ varied in training

Finite bin widths



→ Integrate over bins

Systematic errors



→ 1% uncorrelated systematic errors included Aguilar *et al.* (2015); Cavasonza *et al.* (2018)

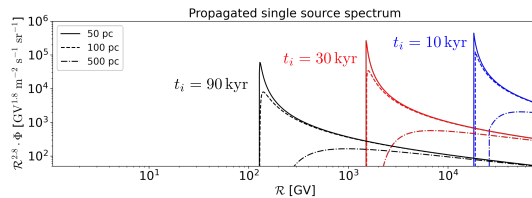
Accuracy virtually unchanged

The results are going to be interesting either way

Classifier finds ...

1. CREDIT scenario

→ Investigate sources



The results are going to be interesting either way

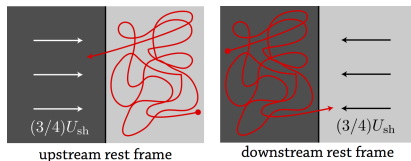
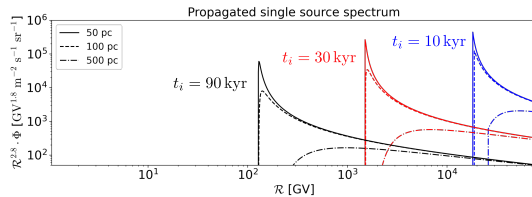
Classifier finds ...

1. CREDIT scenario

→ Investigate sources

2. Burst-like scenario ($E_{\max,b} \rightarrow \infty$)

→ Constraints on acceleration models



The results are going to be interesting either way

Classifier finds ...

1. CREDIT scenario

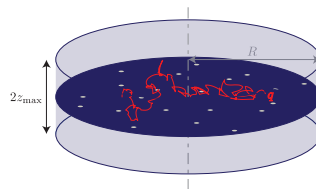
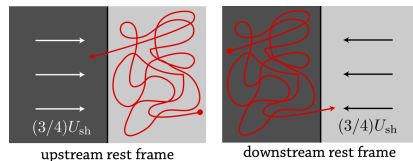
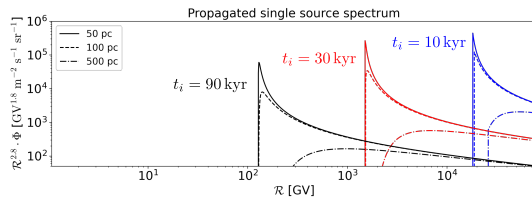
→ Investigate sources

2. Burst-like scenario ($E_{\max,b} \rightarrow \infty$)

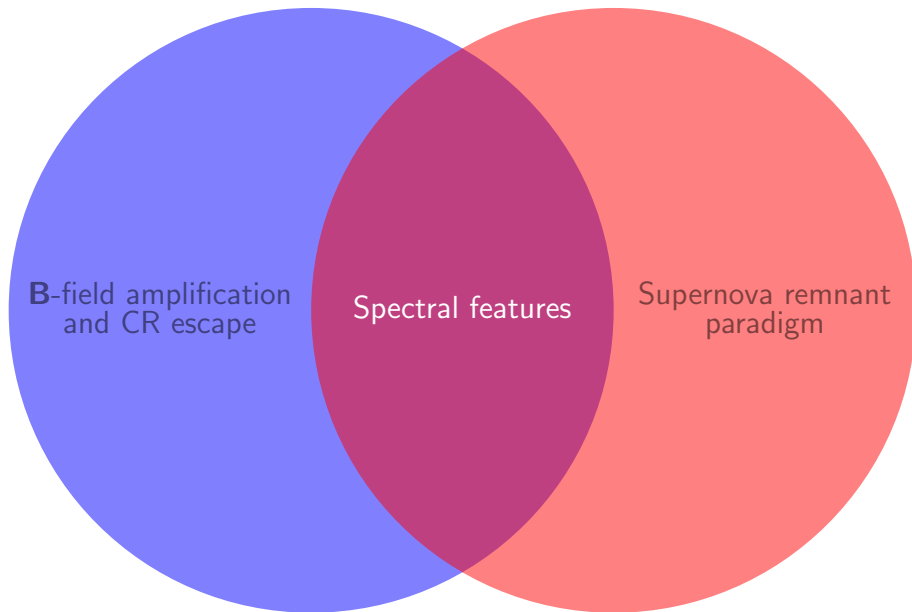
→ Constraints on acceleration models

3. Smooth scenario

→ Trouble for supernova remnant paradigm



Summary & Conclusion

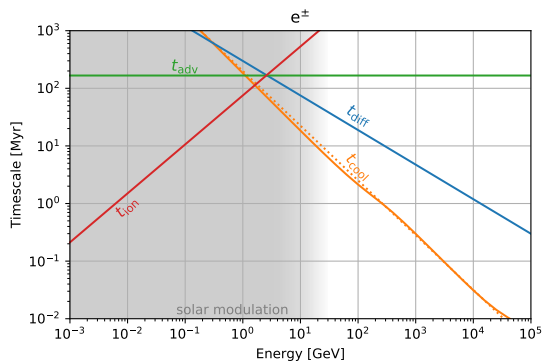




Backup

Time scales

Time scales:



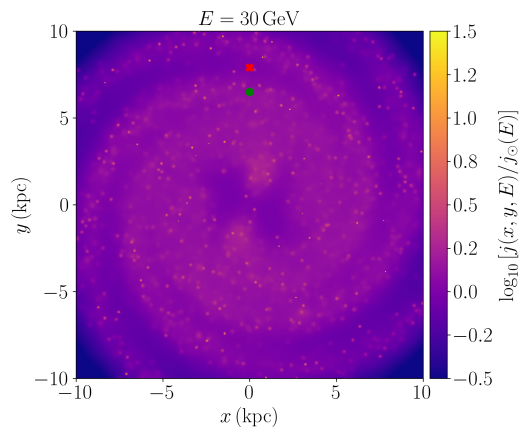
- $t_{\text{diff}} = \frac{z_{\text{max}}^2}{2\kappa}$ with $z_{\text{max}} = 5$ kpc, $\kappa(10 \text{ GV}) = 5 \times 10^{28} \text{ cm}^2 \text{ s}^{-1}$
- t_{cool} : KN cross-section with $\rho = \{0.26, 0.6, 0.6, 0.1\} \text{ eV cm}^{-3}$ for CMB, IR, opt, UV; $3 \mu\text{G}$ B-field
- t_{ion} : $n_{\text{H}} = 0.5 \text{ cm}^{-3}$ (WIM) and $n_{\text{H}} = 0.5 \text{ cm}^{-3}$ (WNM) and 100 pc wide gas disk

In a diffusion model with $E^{-\Gamma}$ sources in disk:

- $\phi(E) \propto E^{-\Gamma-\delta}$ if diffusion dominated
- $\phi(E) \propto E^{-\Gamma-(\delta+1)/2}$ if cooling dominated

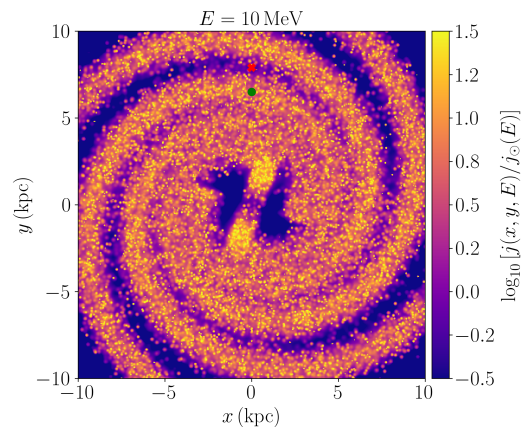
GeV vs MeV

Phan, Schulze, Mertsch, Recchia, Gabici (2023)



(diffusion-loss length) \gg (average source separation)

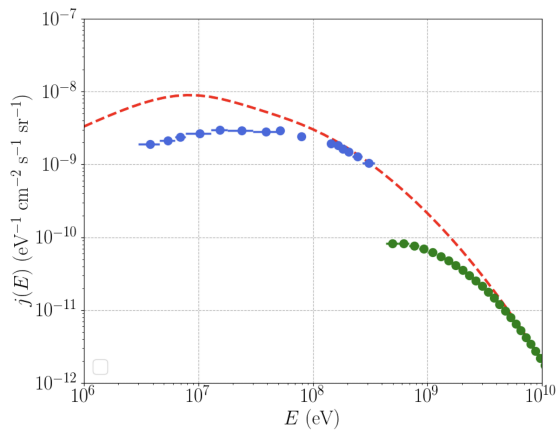
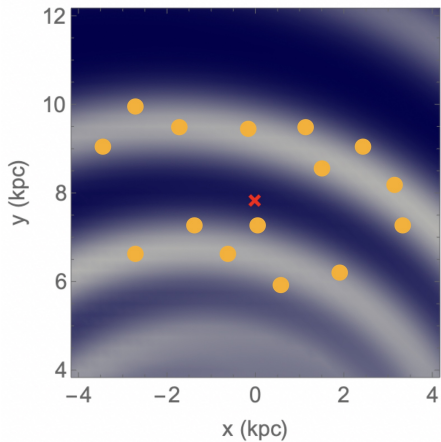
\Rightarrow little fluctuation
 \Rightarrow smooth approximation is good



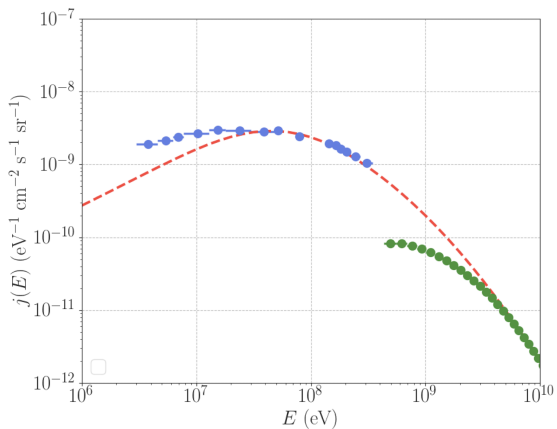
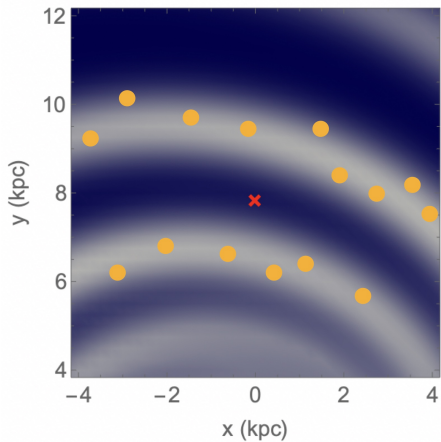
(diffusion-loss length) \ll (average source separation)

\Rightarrow sizeable fluctuations
 \Rightarrow smooth approximation is bad

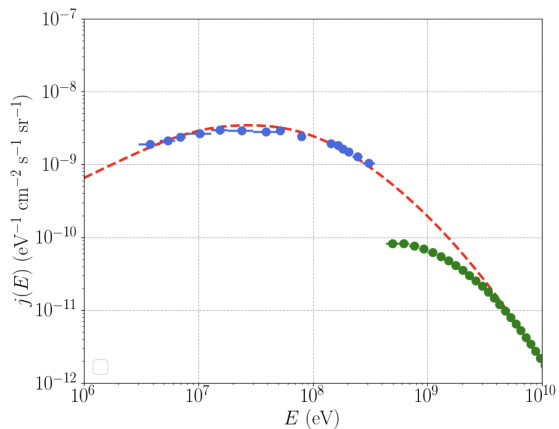
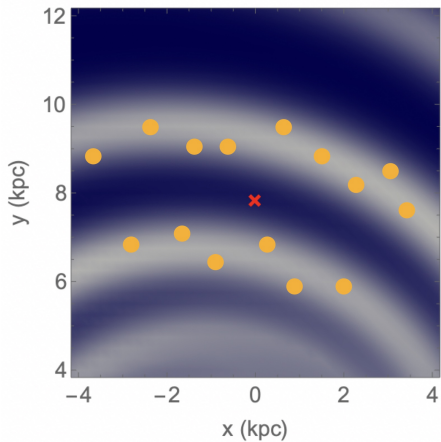
Importance of nearby sources



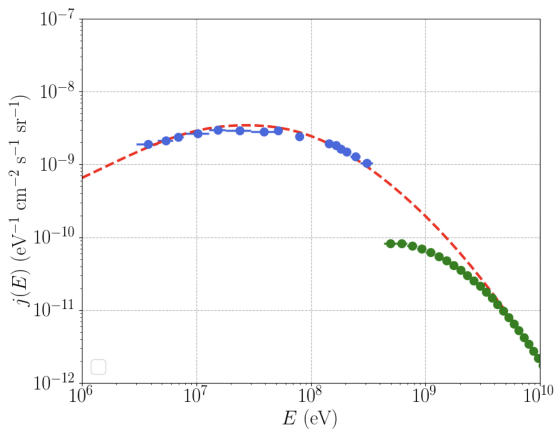
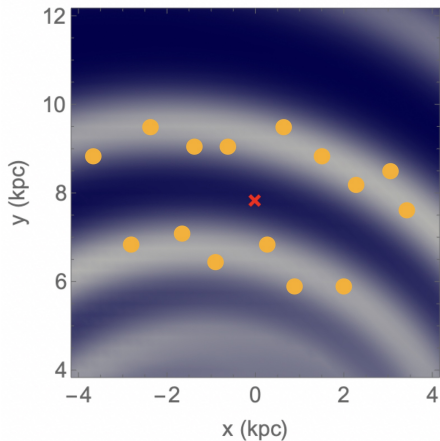
Importance of nearby sources



Importance of nearby sources



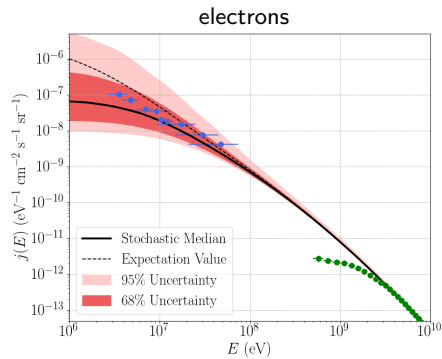
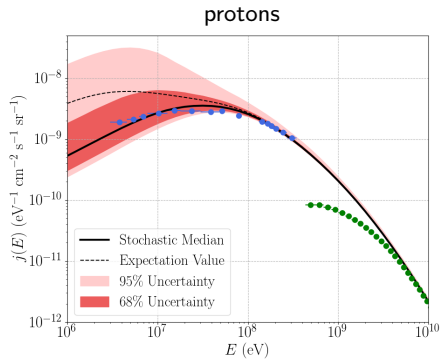
Importance of nearby sources



Cosmic ray flux is a stochastic quantity

Results: protons & electrons

Phan, Schulze, Mertsch, Recchia, Gabici (2021)



- Voyager 1 data inside uncertainty band

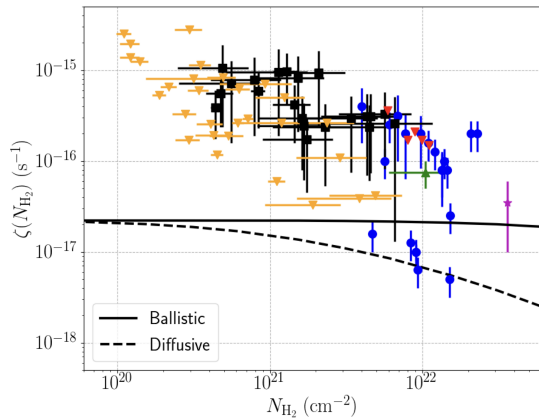
→ Source discreteness effects important

Result # 1

→ No need for unmotivated break in source spectrum!

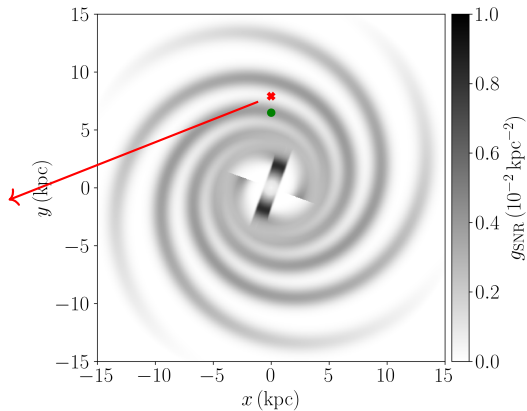
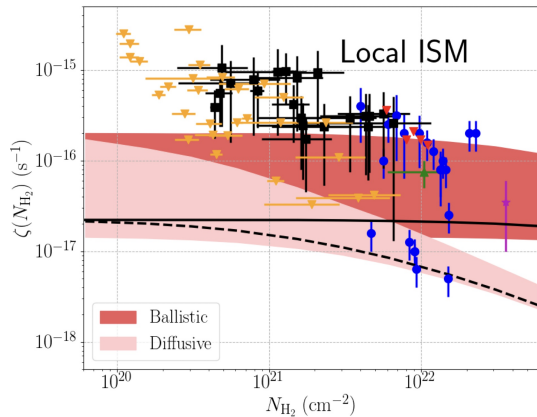
The ionisation puzzle

Phan, Schulze, Mertsch, Recchia, Gabici (2023)



The ionisation puzzle

Phan, Schulze, Mertsch, Recchia, Gabici (2023)

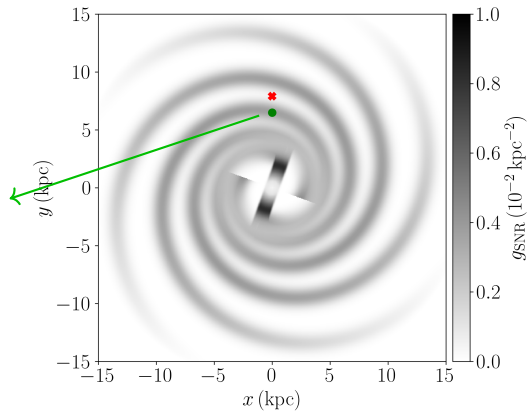
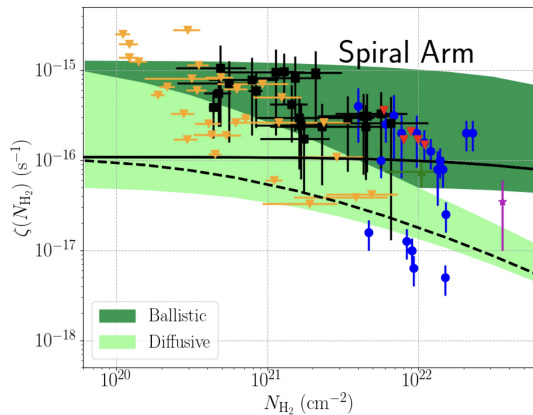


Result # 2

- Local ISM: improvement, but still too low

The ionisation puzzle

Phan, Schulze, Mertsch, Recchia, Gabici (2023)



Result # 2

- Local ISM: improvement, but still too low
- Spiral Arm: systematic shift up