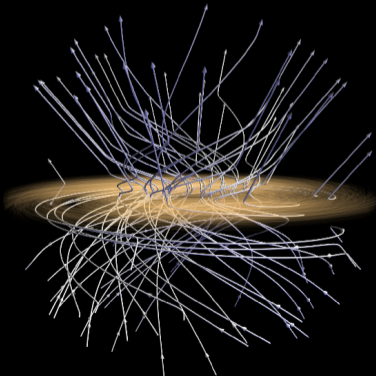
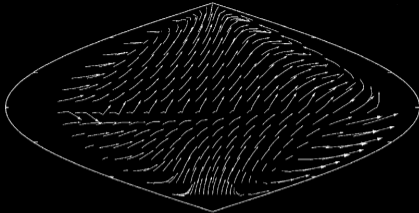


New Models of the Magnetic Field of the Galaxy

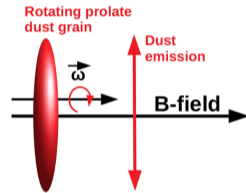
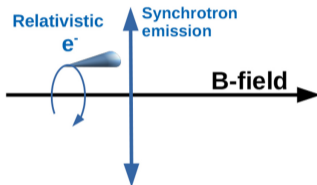
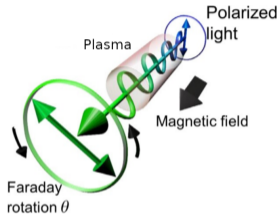
M. Unger (KIT) in collaboration with G.R. Farrar (NYU)



Modeling of the Coherent Galactic Magnetic Field (GMF)

Aim: Describe large-scale structure of GMF with simple parametric forms

Observables:



adapted from Hasegawa+13 and Pelgrims+18

Popular GMF Models:

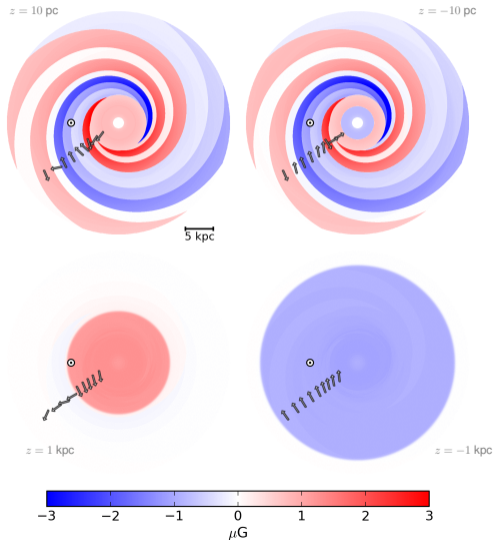
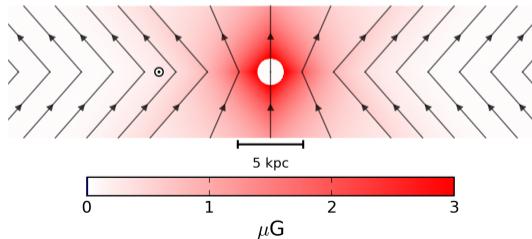
	S97	Jaffe10*	PT11	JF12	Planck16	TF17**
parameter fit	X	✓	✓	✓	X	✓
extragalactic RMs	X	✓	✓	✓	X	✓
polarized synchrotron	X	✓	X	✓	✓	X
polarized dust	X	X	X	X	✓	X
$\nabla \mathbf{B} = 0$	X	X	X	✓	X	✓

Jansson&Farrar Magnetic Field Model (JF12)

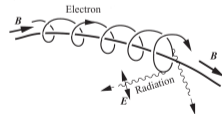
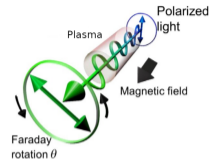
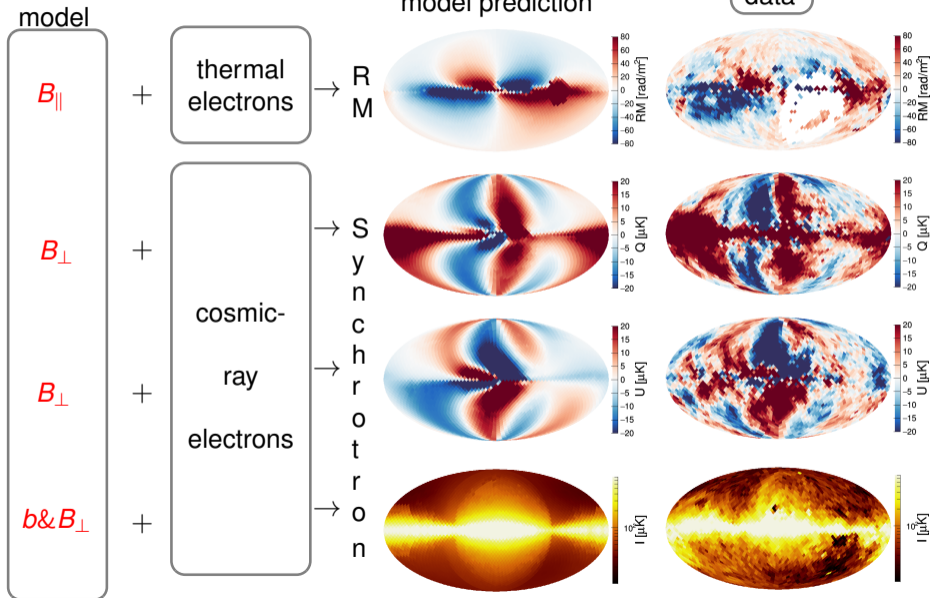
R. Jansson & G.F. Farrar, ApJ 757 (2012) 14

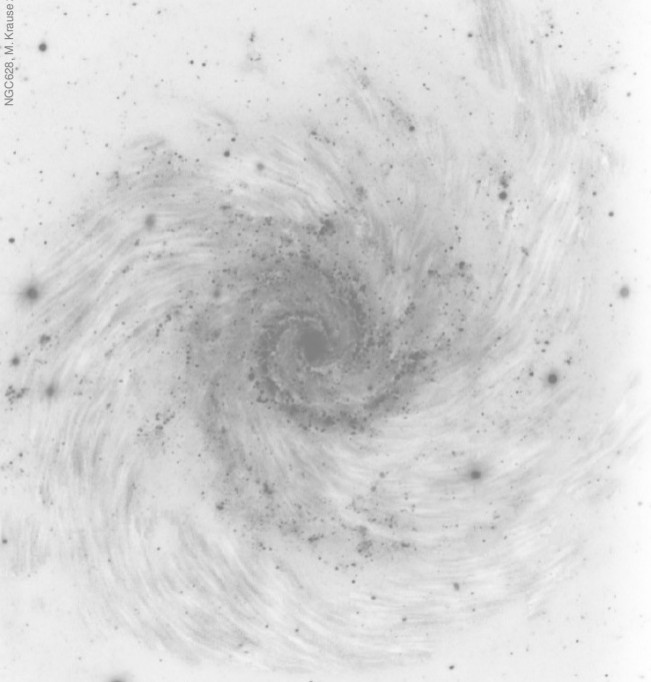
three divergence-free components:

- disk field, ($h \lesssim 0.4$ kpc)
- toroidal halo field ($h_{\text{scale}} \sim 5.3$ kpc)
- “X-field” (halo)
- 21 parameters adjusted to 6605 data points



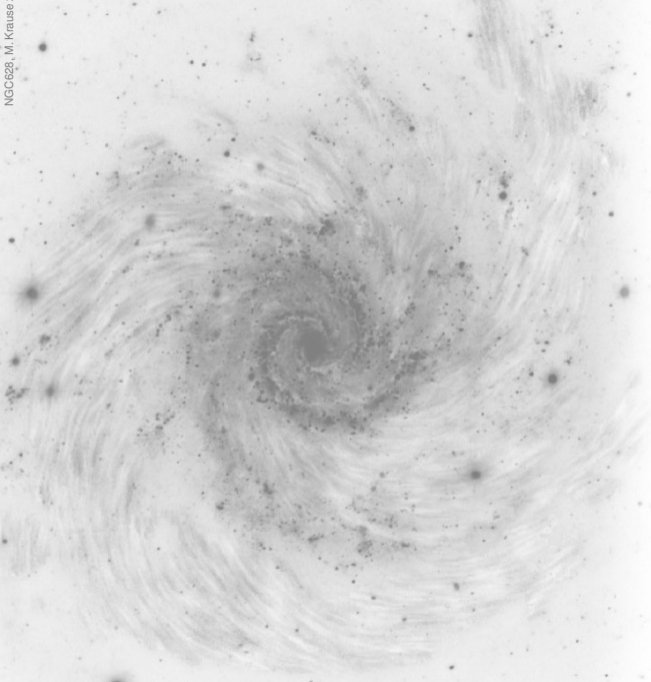
Model Optimization





Outline

- **RM and Synchrotron Data**
- **Thermal Electrons**
- **Cosmic-Ray Electrons**
- **Parametric GMF Models**
- **Results**

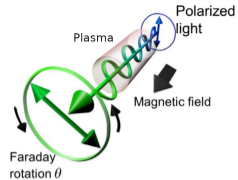
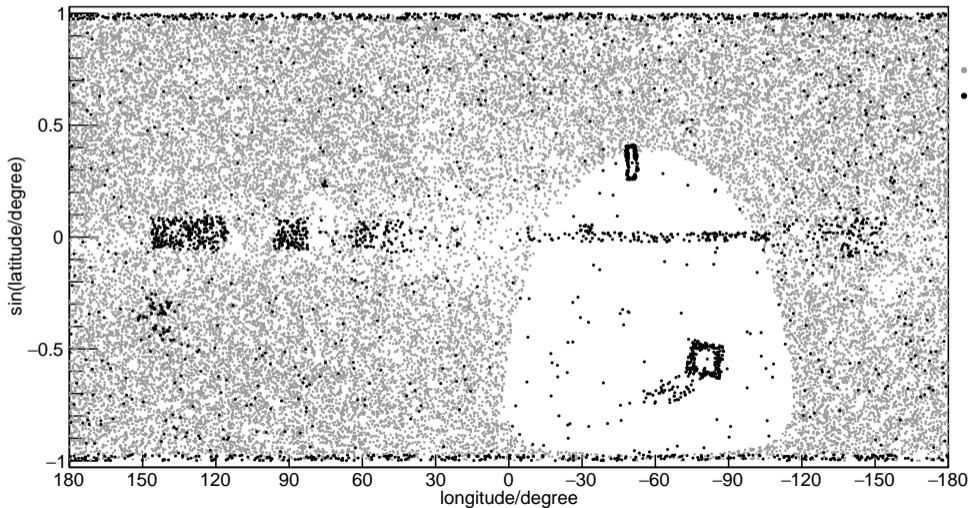


Outline

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Extragalactic Rotation Measures used for JF12

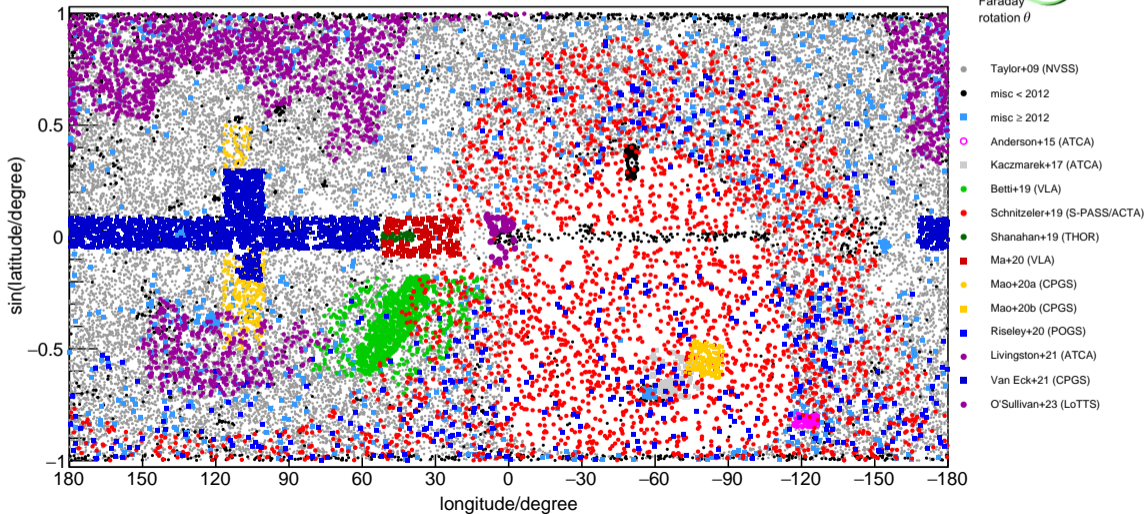
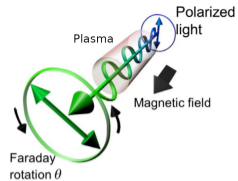
$$\theta = \theta_0 + \text{RM} \lambda^2$$



- Taylor+09 (NVSS)
- misc < 2012

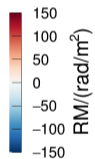
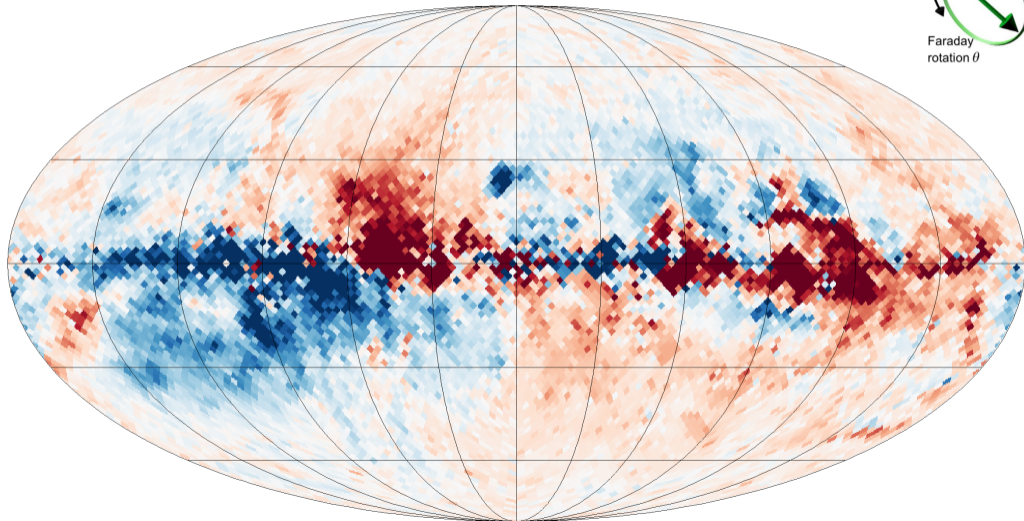
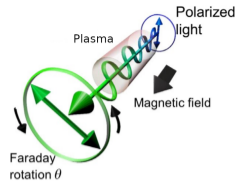
Extragalactic Rotation Measures 2023

$$\theta = \theta_0 + \text{RM} \lambda^2$$



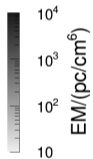
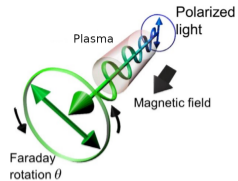
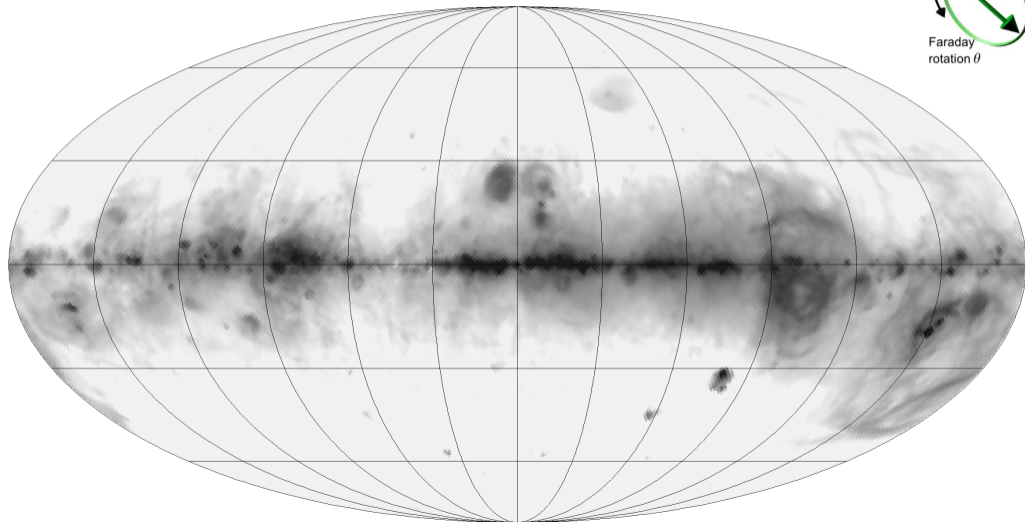
2023 RM Sky

$$RM \propto \int_{\text{source}}^{\text{observer}} B_{\parallel}(l) n_e(l) dl$$



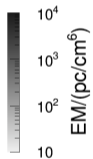
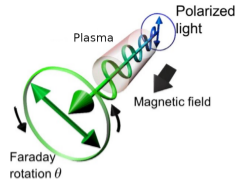
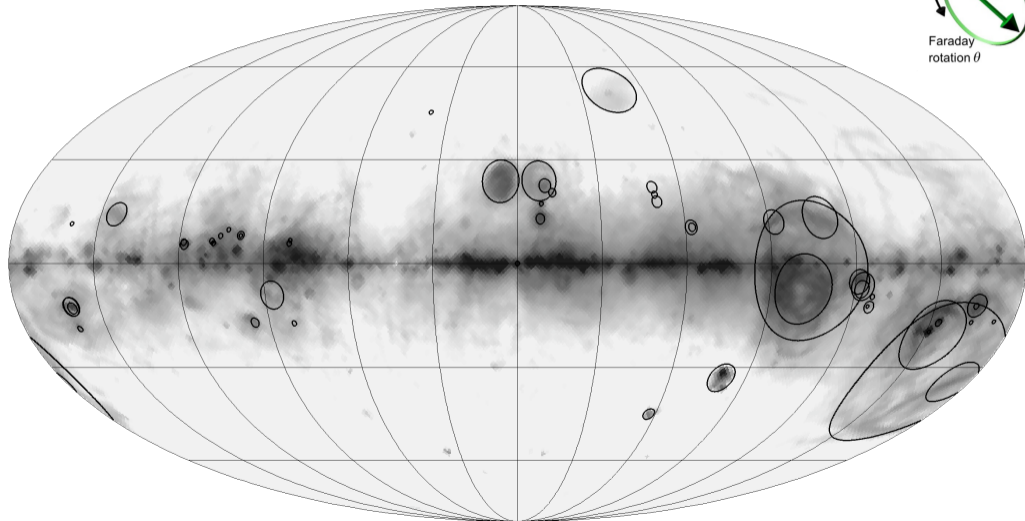
Foreground: HII Regions

$$EM \propto \int_{\text{source}}^{\text{observer}} n_e(l)^2 dl$$

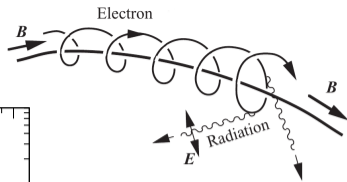
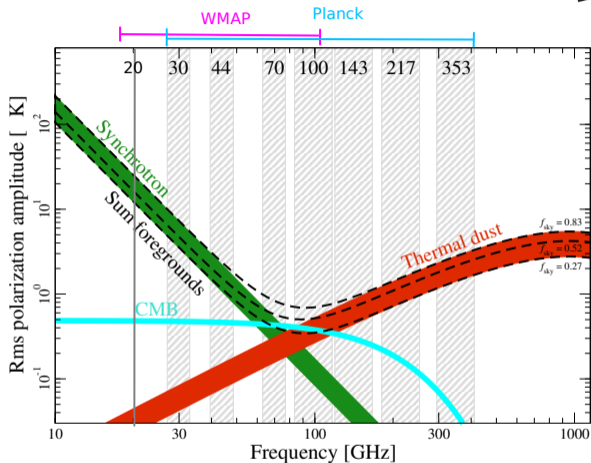


Foreground: HII Regions

$$EM \propto \int_{\text{source}}^{\text{observer}} n_e(l)^2 dl$$



Polarized Synchrotron Emission



- antenna temperature: $T_{\text{syn}} \propto \nu^{-(p+3)/2} \equiv \nu^{\beta_S}$
- electron spectral index p : ~ 2 at source, ~ 3 after cooling
- $\beta_S \sim -3 \rightarrow T_{\text{syn}}(20 \text{ Hz})/T_{\text{syn}}(30 \text{ Hz}) \approx 3.4$

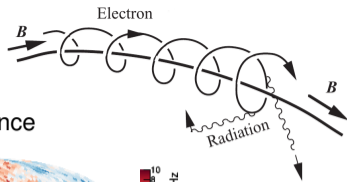
Polarized Synchrotron Emission



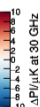
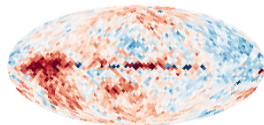
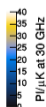
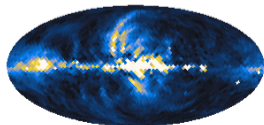
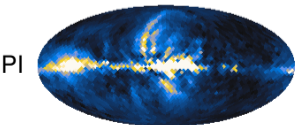
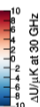
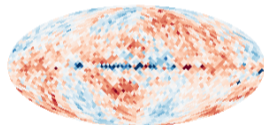
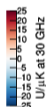
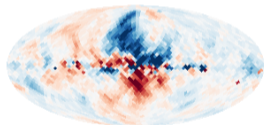
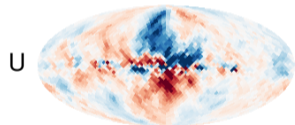
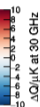
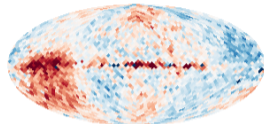
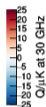
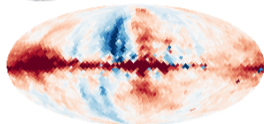
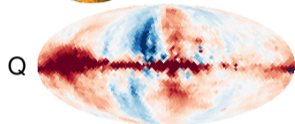
WMAP9



Planck R3.00

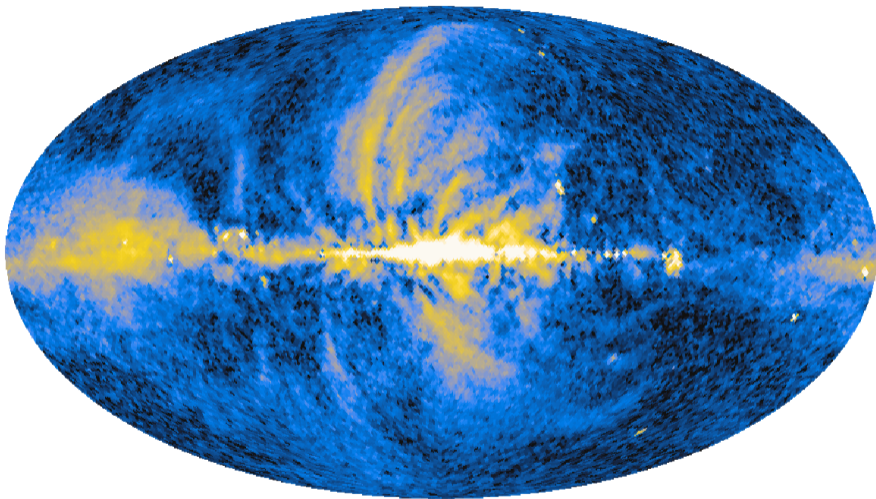
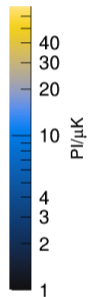
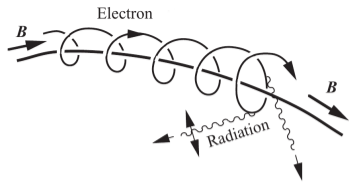


difference

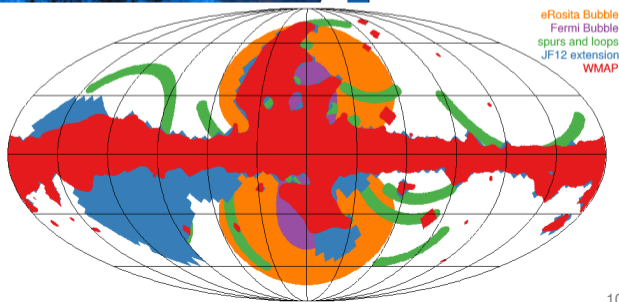
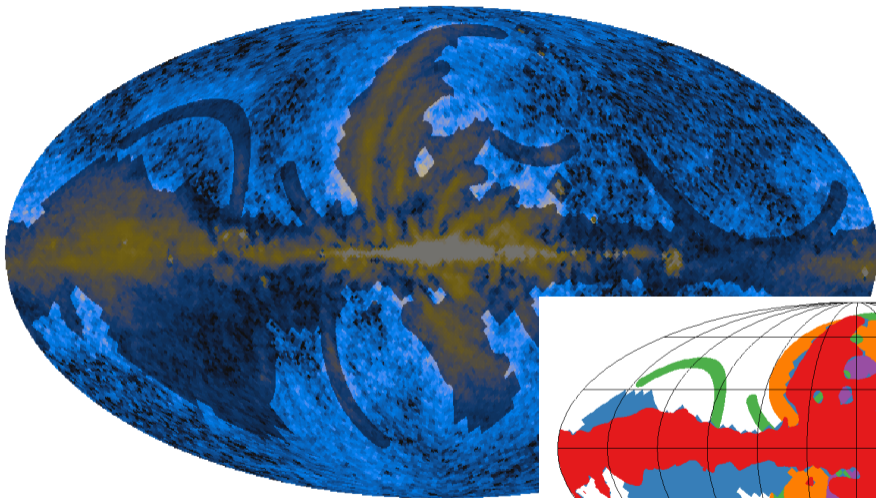
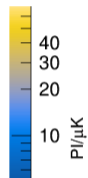
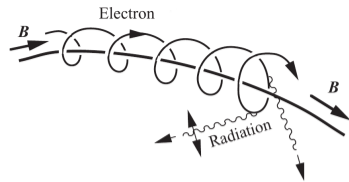


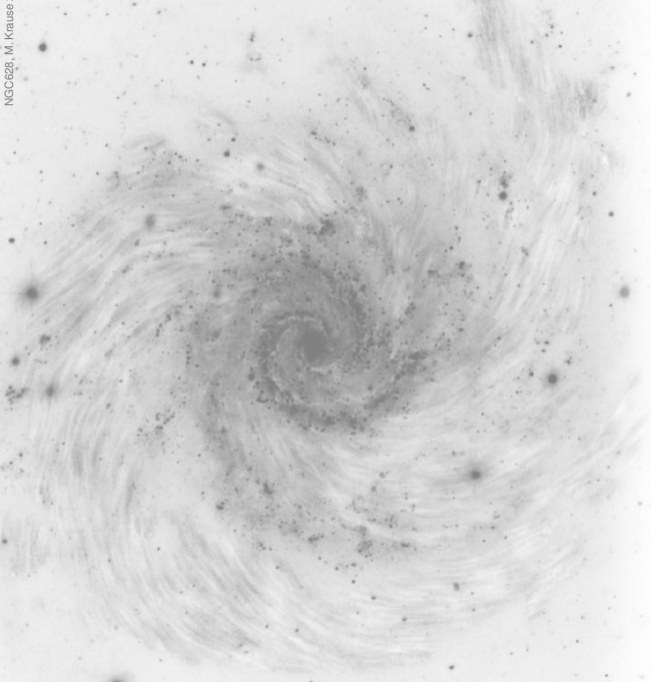
calibration uncertainty? cosmic-ray spectral index?

Combined WMAP-Planck Polarized Emission



Combined WMAP-Planck Polarized Emission



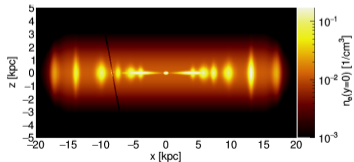
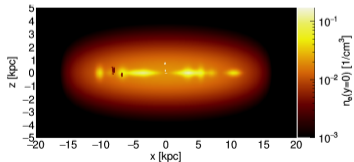
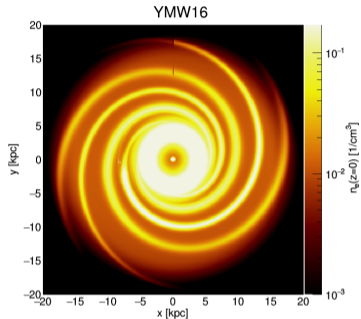
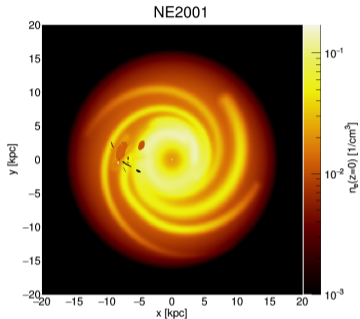
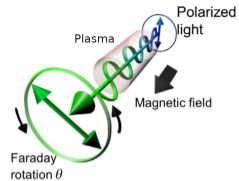


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Thermal Electron Models

$$DM \propto \int_{\text{source}}^{\text{observer}} n_e(l) dl$$



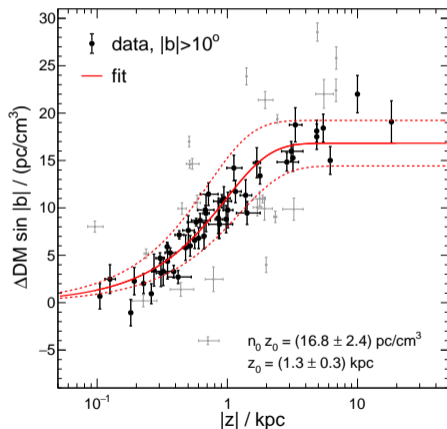
112 pulsar DMs

189 pulsar DMs

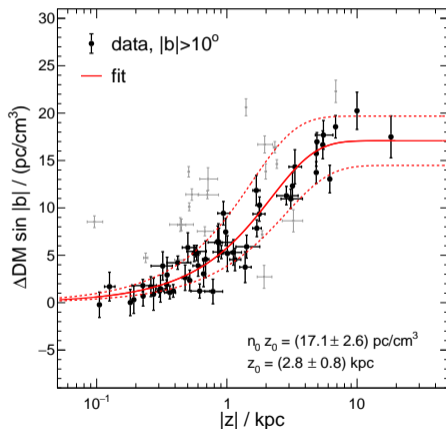
Thermal Electron Halo

reasonably well-constrained from DMs of pulsars in globular clusters

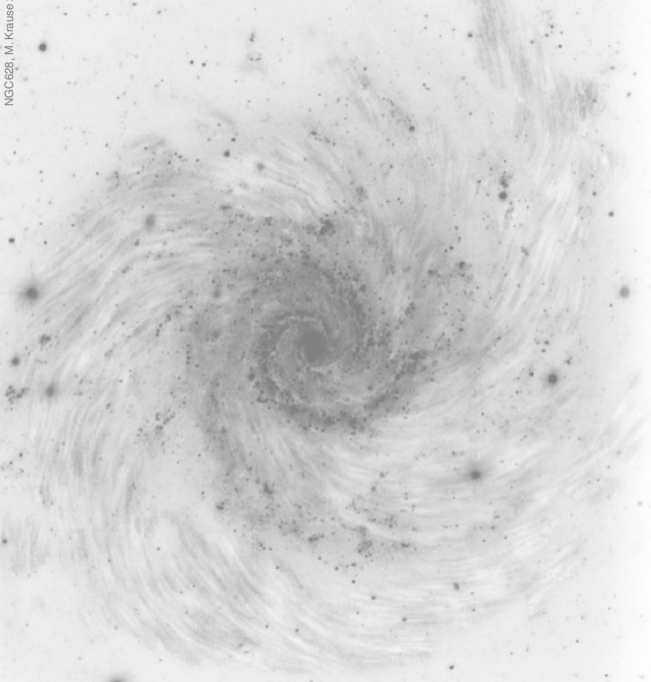
YMW16



NE2001



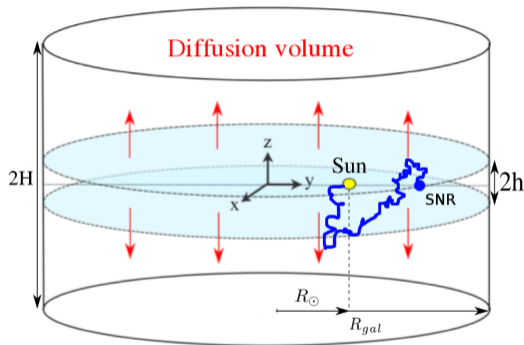
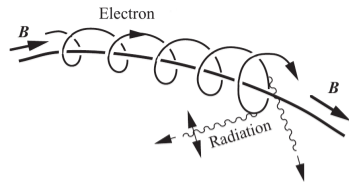
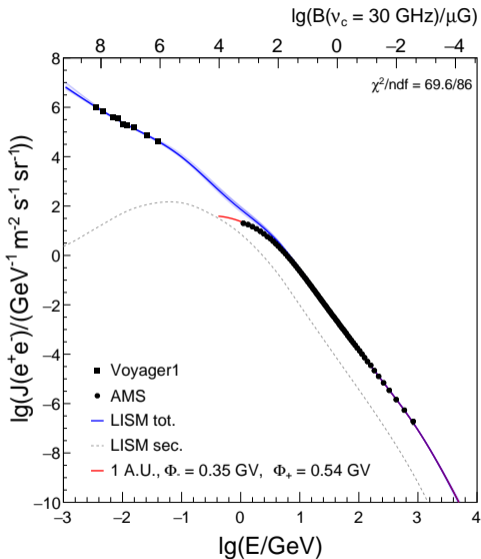
ΔDM : data-model residual without exponential halo (preliminary)



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Cosmic-Ray Electron Model

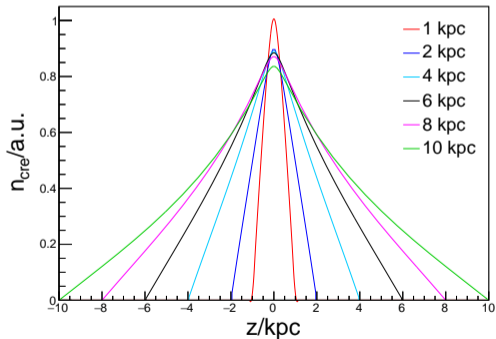


homogenous and isotropic diffusion $D_0 \propto R^\delta$ (rigidity R)

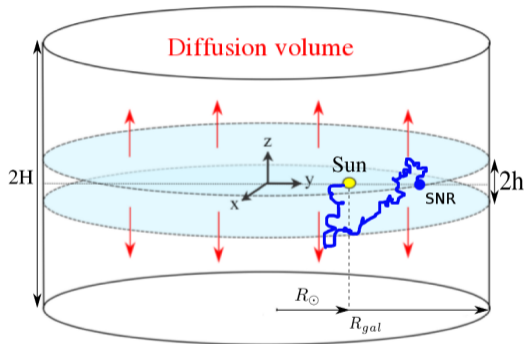
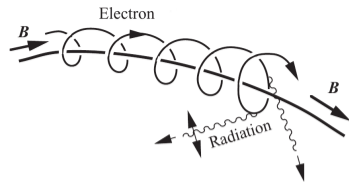
Cosmic-Ray Electron Model

- $D_0/H = \text{const}$ from B/C
- halo half-height H currently not well constrained Weinrich+20, Evoli+20, Maurin+22

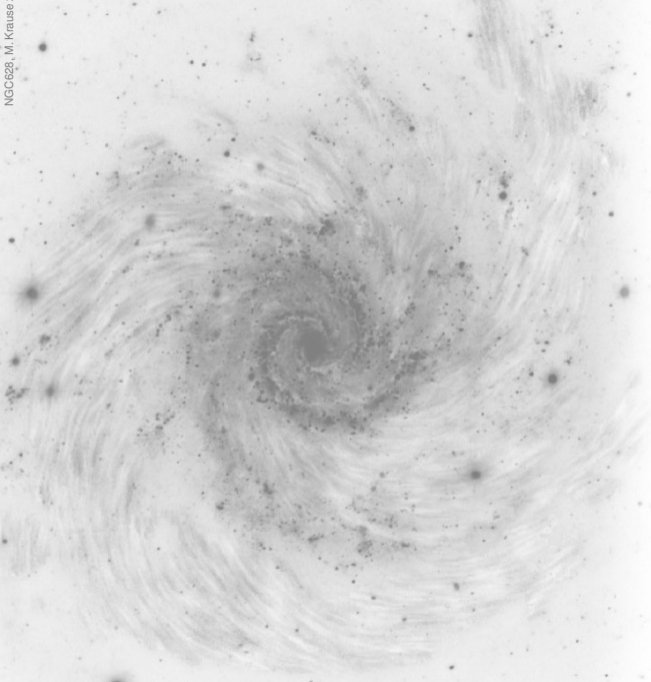
→ large uncertainty in vertical n_{cre} profile!



example: $r = 5\text{kpc}$, $E = 10\text{GeV}$



homogenous and isotropic diffusion $D_0 \propto R^\delta$ (rigidity R)

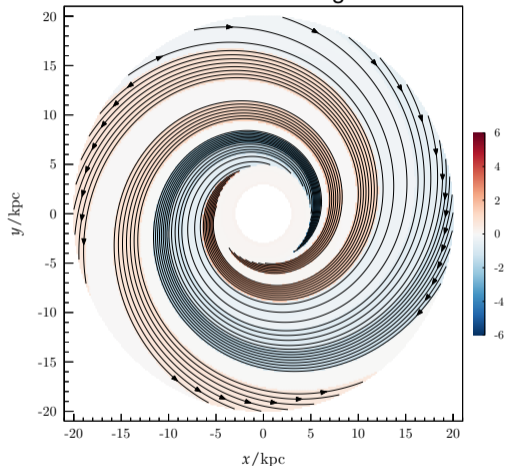


Outline

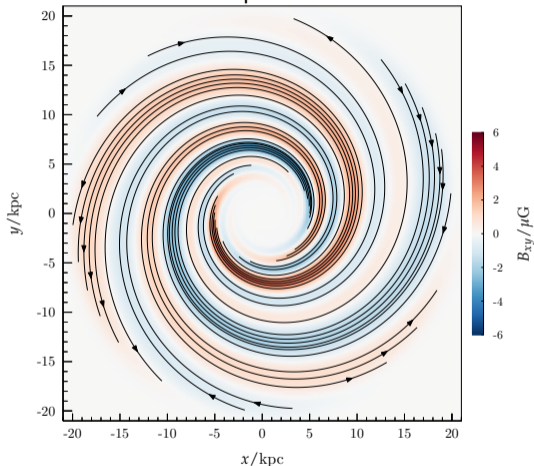
- RM and Synchrotron Data
- Thermal Electrons
- Cosmic-Ray Electrons
- **Parametric GMF Models**
- Results

GMF Model Improvements – Disk Field

JF12: Brown+07 “wedge”-model:



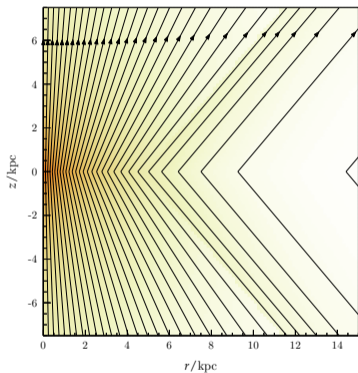
smooth spiral disk field:



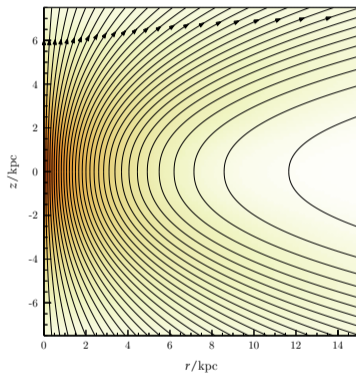
- divergence-free Fourier-expansion of $B_\phi(r)$ at reference radius
- avoids sharp radial discontinuities of JF12
- free pitch angle and “magnetic arms” (number of Fourier modes)

GMF Model Improvements – Halo X-Field

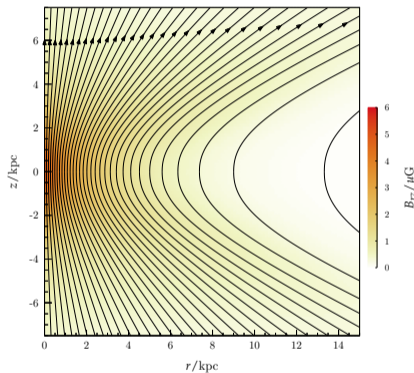
JF12



Ferriere&Terral14



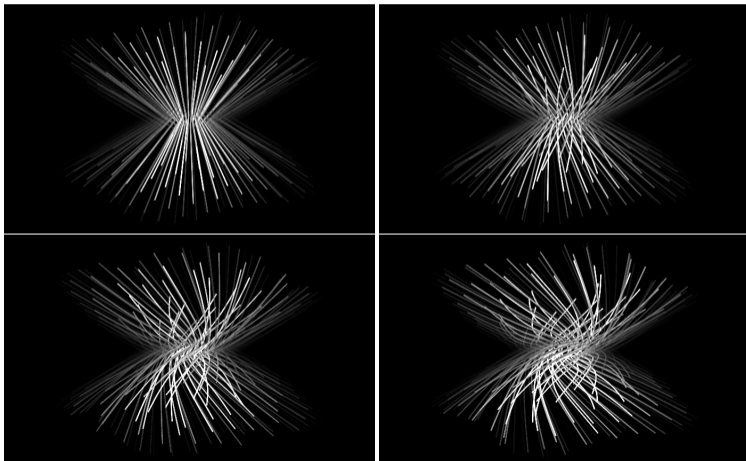
UF23



- fix JF12 discontinuities at $z = 0$ and transition to $\theta_X = 49^\circ$

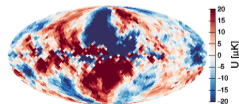
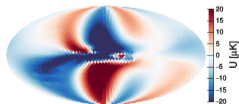
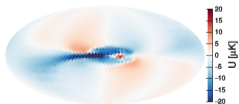
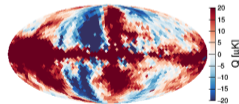
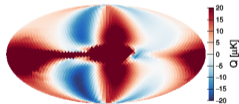
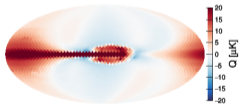
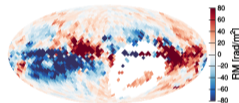
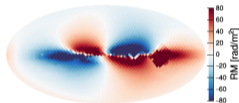
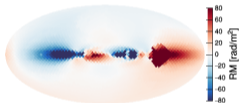
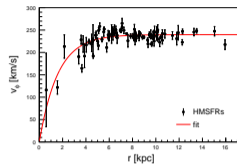
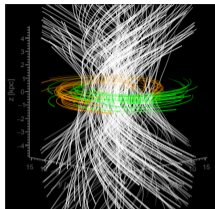
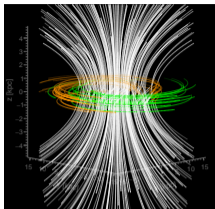
GMF Model Improvements – Halo Field

- evolve X-field via ideal induction equation $\partial_t \mathbf{B} = \nabla \times (\mathbf{v}_{\text{rot}} \times \mathbf{B})$
- radial and vertical shear of Galactic rotation generates toroidal field



- no separate X- and toroidal halo needed!

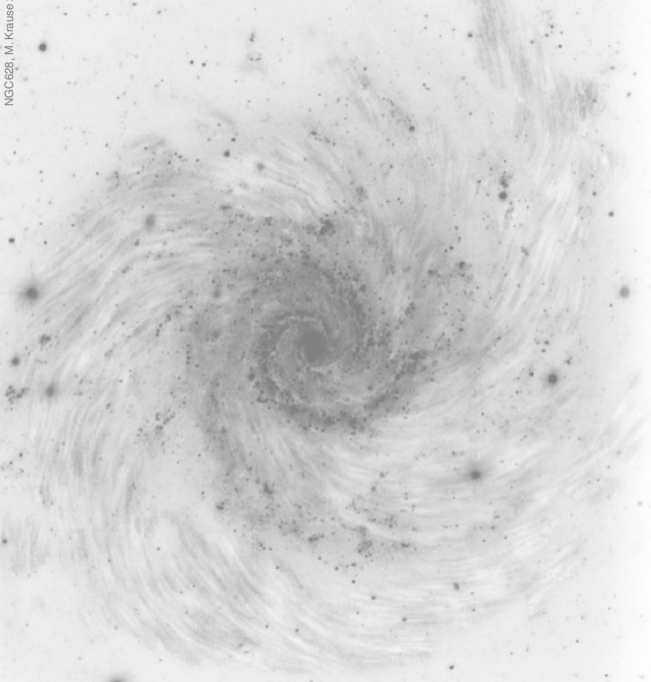
“Twisted X-field”



(a) $t = 0$ Myr

(b) $t = 70$ Myr

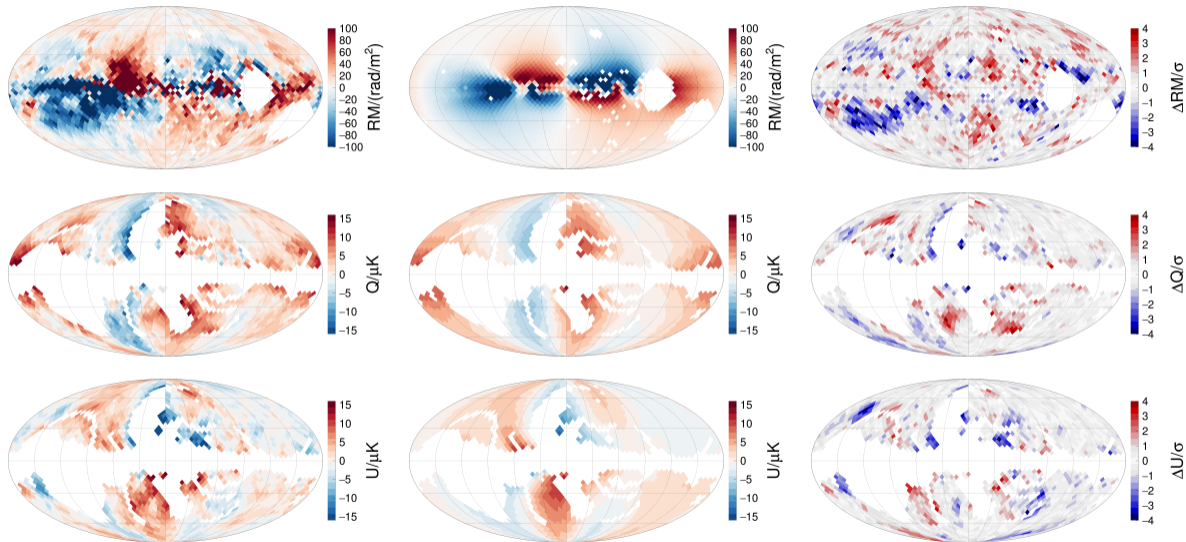
(c) data



Outline

- RM and Synchrotron Data
- Thermal Electrons
- Cosmic-Ray Electrons
- Parametric GMF Models
- **Results**

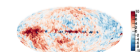
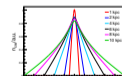
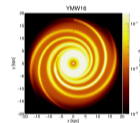
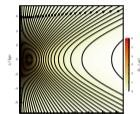
Fit of RM/Q/U ($\chi^2/\text{ndf} = 7759/6500 = 1.19$)



model describes large-scale features of 6520 data points with only 20 parameters!

UF23 Model Variations

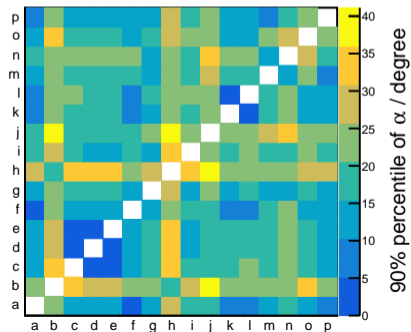
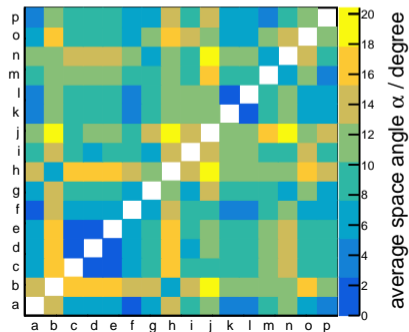
id	disk	halo		n_e model	κ	h_{cre} (kpc)	QU	χ^2/ndf
		toroidal	poloidal					
Parametric models								
a	UF	JFsym	UF	logistic	YMW16	0	(W+P)/2	7923 / 6500 = 1.22
b	UF	twist	UF	logistic	YMW16	0	(W+P)/2	8324 / 6504 = 1.28
c	UF	JFsym	UF	gauss	YMW16	0	(W+P)/2	8298 / 6500 = 1.28
d	UF	JFsym	UF	sech2	YMW16	0	(W+P)/2	8381 / 6500 = 1.29
e	UF	JFsym	UF	expo	YMW16	0	(W+P)/2	8431 / 6500 = 1.30
f	UF	JFsym	FTc	logistic	YMW16	0	(W+P)/2	7926 / 6500 = 1.22
Thermal electrons								
g	UF	JFsym	UF	logistic	NE2001	0	(W+P)/2	7759 / 6500 = 1.19
h	UF	twist	UF	logistic	NE2001	0	(W+P)/2	8180 / 6504 = 1.26
i	UF	JFsym	UF	gauss	NE2001	0	(W+P)/2	8079 / 6500 = 1.24
j	UF	JFsym	UF	logistic	YMW16	-0.4	(W+P)/2	7905 / 6500 = 1.22
Cosmic-ray electrons								
k	UF	JFsym	UF	logistic	YMW16	0	(W+P)/2	7940 / 6500 = 1.22
l	UF	JFsym	UF	logistic	YMW16	0	(W+P)/2	7939 / 6500 = 1.22
Synchrotron Map								
m	UF	JFsym	UF	logistic	YMW16	0	CG23	9758 / 6500 = 1.50
n	UF	JFsym	UF	logistic	NE2001	0	CG23	9551 / 6500 = 1.47
o	UF	JFsym	UF	logistic	YMW16	0	P	11013 / 6500 = 1.69
p	UF	JFsym	UF	logistic	YMW16	0	W	8845 / 6500 = 1.36



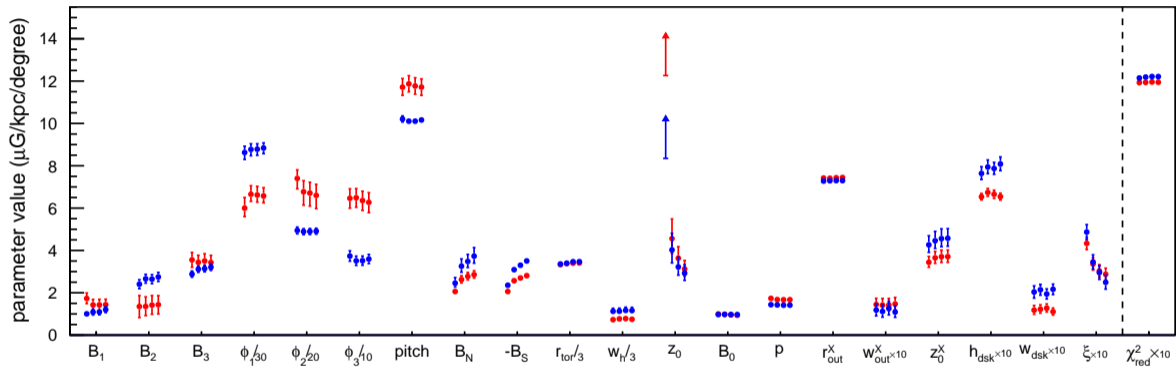
UF23 Model Ensemble

id	name	disk	halo		n_e model	κ	h_{cre} (kpc)	QU	χ^2/ndf	
			toroidal	poloidal						
1	base	UF	JFsym	UF	logistic	YMW16	0	6	(W+P)/2	1.22
2	xr	UF	JFsym	UF	expo	YMW16	0	6	(W+P)/2	1.30
3	ne	UF	JFsym	UF	logistic	NE2001	0	6	(W+P)/2	1.19
4	κ	UF	JFsym	UF	logistic	YMW16	-0.4	6	(W+P)/2	1.22
5	twist	UF	twist	UF	logistic	NE2001	0	6	(W+P)/2	1.26
6	cre	UF	JFsym	UF	logistic	YMW16	0	10	(W+P)/2	1.22
7	syn	UF	JFsym	UF	logistic	YMW16	0	6	CG23	1.50

deflection angle differences at 10 EV:



Example: Thermal and Cosmic-Ray Models

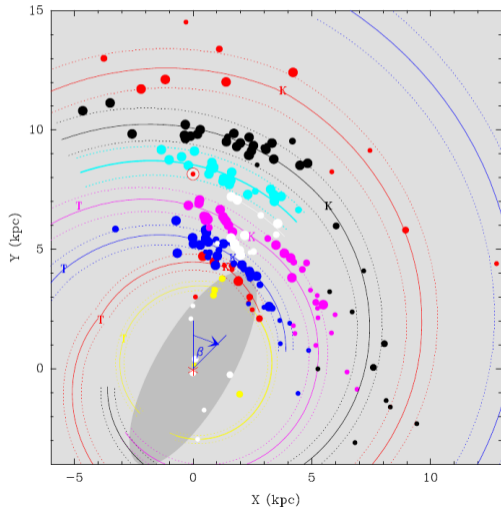


NE2001, YMW16, left to right $h_{\text{cre}} = 4, 6, 8, 10$ kpc

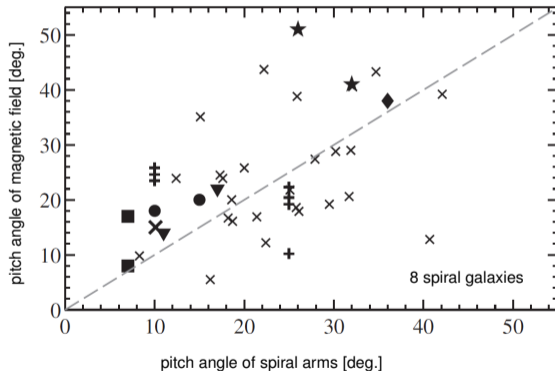
Magnetic Pitch Angle

- fitted magnetic pitch angle in disk $(11 \pm 1)^\circ$ (error dominated by n_e)
- pitch angle of local arm $(11.4 \pm 1.9)^\circ$ (fit of HMSFR with parallaxes)

Reid+ApJ19



van Eck+ApJ15



The RM-PI Puzzle

Longstanding Problem:

derived field $\hat{B}(\text{RM}) < \hat{B}(\text{PI})$

Proposed Solutions:

- $n_{\text{cre}} - B$ correlations: $\hat{B}(\text{PI}) > B_{\text{true}}$
 → not observed in MHD simulations ($l < l_{\text{outer}}$) Seta+18
- anisotropic (“striated”) random fields: $\hat{B}(\text{PI}) > B_{\text{true}}$

prescription:

$$B = (1 + \xi)B_0 \quad \text{Jansson\&Farrar ApJ12}$$

(striation enhances PI but not RM!)

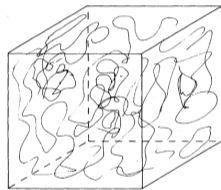
- $n_e - B$ anti-correlation: $\hat{B}(\text{RM}) < B_{\text{true}}$

prescription:

$$\text{RM} = \text{RM}_0 \left(1 + \frac{2}{3} \kappa \frac{\langle b^2 \rangle}{B^2 + \langle b^2 \rangle} \right) \quad \text{Beck+A\&A03}$$

(anti-correlation diminishes RM)

Laing MNRAS80



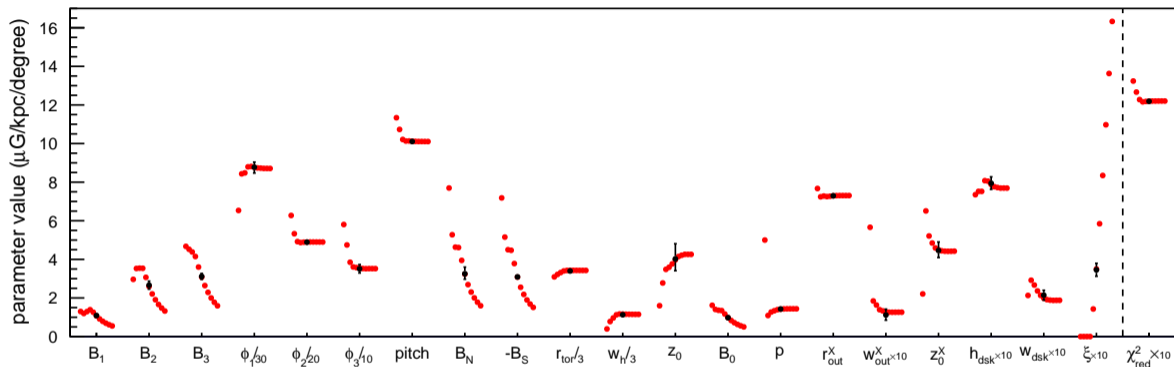
(a)
Before Compression



(b)
After Compression



The RM-PI Puzzle

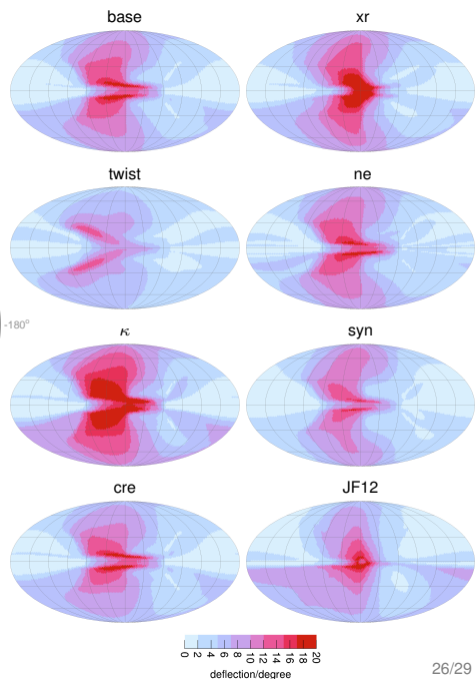
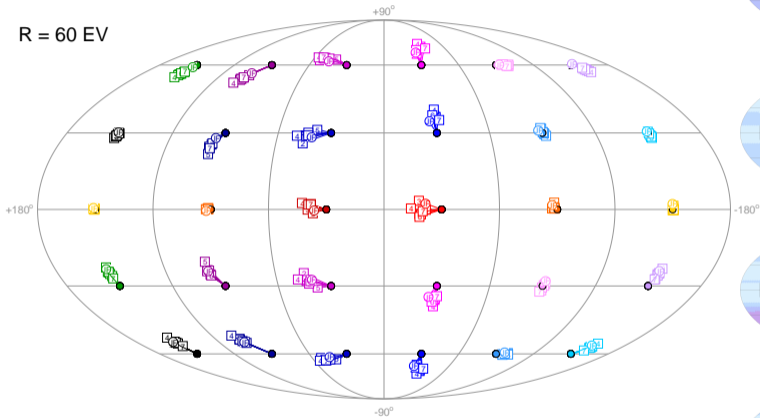


left to right: $\kappa = -1 \dots +1$, black point is $\kappa = 0$

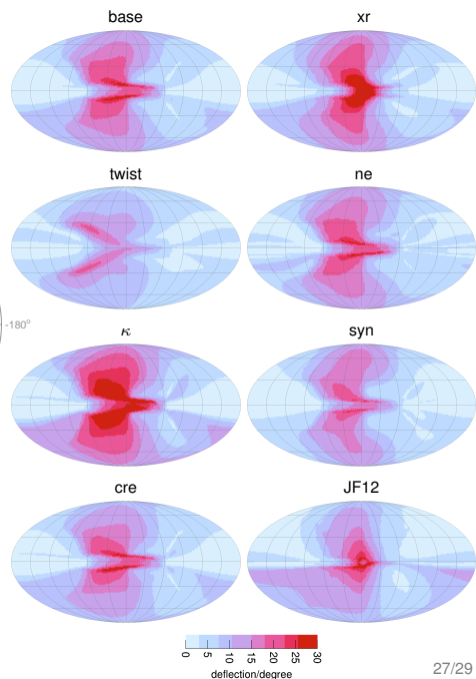
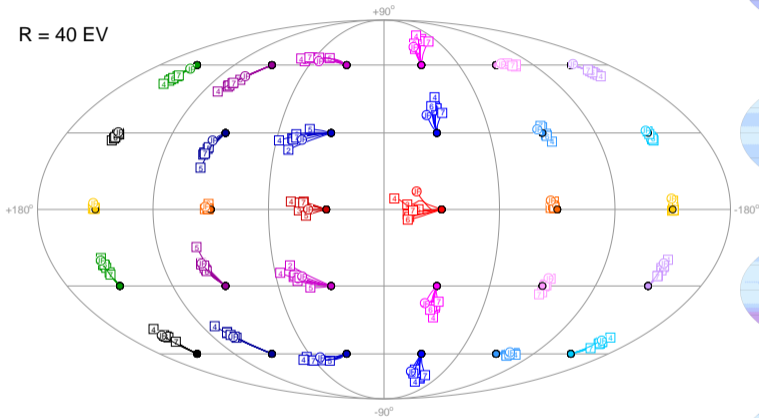
- no stration needed at $\kappa \sim -0.4$
- χ^2 minimum at $\kappa = -0.4$ ($\Delta\chi^2 = -23$ wrt. $\kappa = 0$)

Cosmic-Ray Deflections, R=60 EV

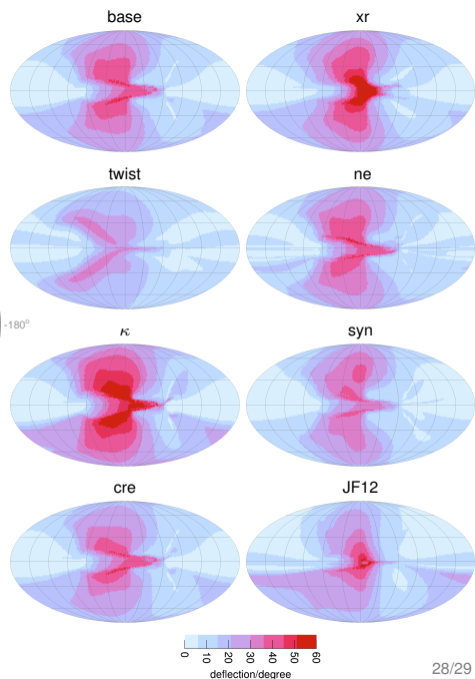
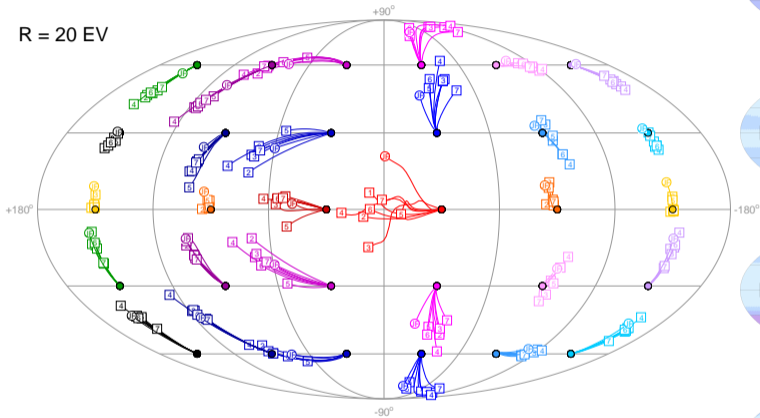
R = 60 EV



Cosmic-Ray Deflections, R=40 EV



Cosmic-Ray Deflections, R=20 EV



Summary

Major Overhaul of JF12 GMF Model

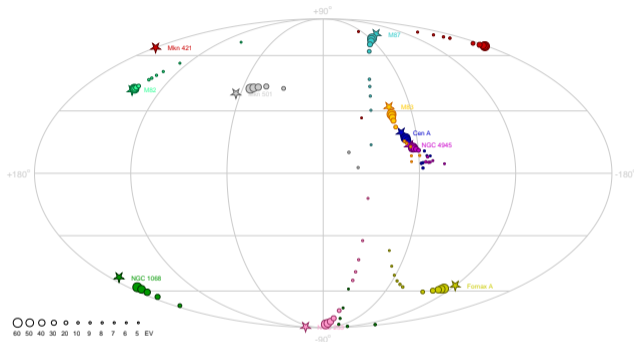
- new RM data
- new synchrotron sky maps
- improved auxiliary models (n_e and n_{cre})
- smooth disk-field
- unified halo model

Main Results:

- JF12 dipolar X-field robust ⚡ **dynamo?**
- magnetic pitch \sim spiral pitch ⚡ **coherent?**
- $n_e - B$ anti-corr. is alternative to striation
→ **larger B estimates**
- GMF model ensemble
→ **cosmic-ray deflection uncertainties**

Outlook

Apply to CR Analysis



Incorporate New Data (existing and future)
pulsar RMs, low-frequency QU, I_{syn} + variances,
dust pol. tomography, ...

Foreground Modelling

local bubble, loops and spurs.