



# Cosmic Rays Primary Energy estimation using ML and combined reconstruction

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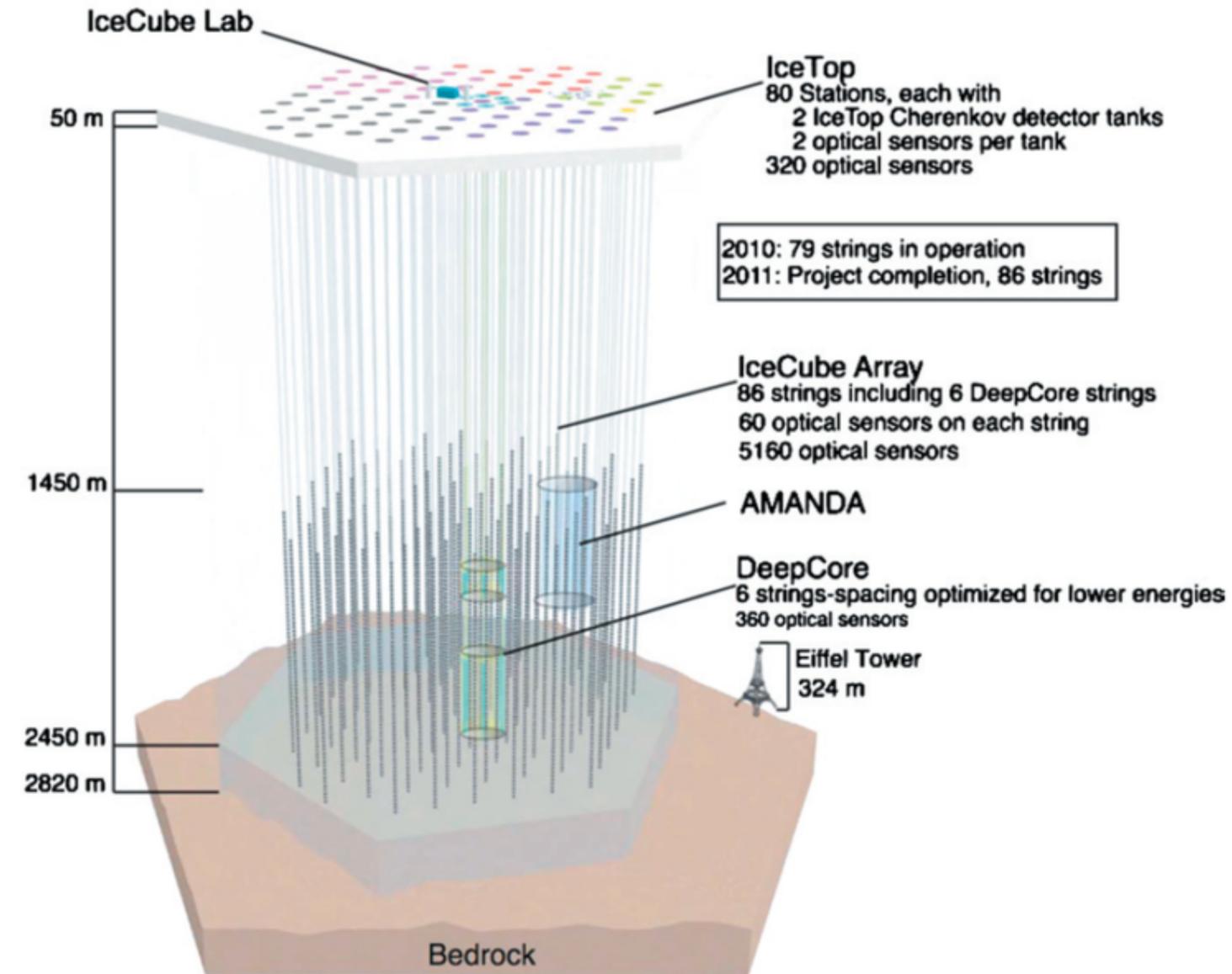
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# Overview

- Introduction and Motivation
- General description of the reconstruction
- Energy estimation method using Linear fit
- Energy estimation/prediction using Random Forest Regression
- Comparison between Linear Fit and Random Forest Regression performance
- Summary



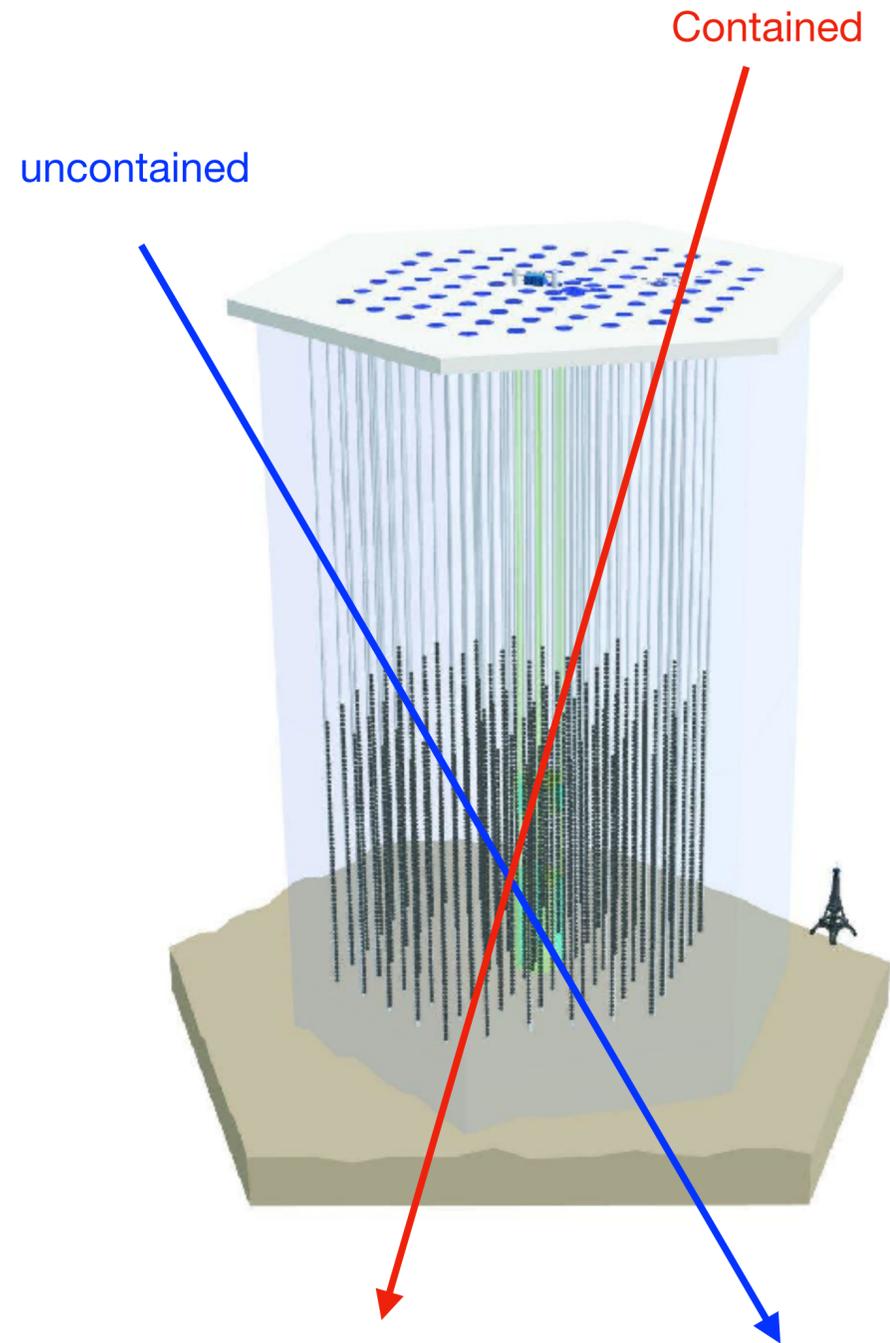
# Introduction



- A lot of techniques and parameters are available and can be combined to determine the primary energy and mass from air showers.



# Motivation



- There is no conventional energy estimation function (each analysis is unique; simulation, snowmodel, cuts, etc.).
- Using Random Forest Regression and a combined reconstruction to estimate cosmic rays' primary energy
- Using Monte Carlo events for proton, iron, helium and oxygen under two containment conditions (contained and uncontained).

## Goal

- Investigate a possible improvement for cosmic rays' primary energy estimation



# Reconstruction

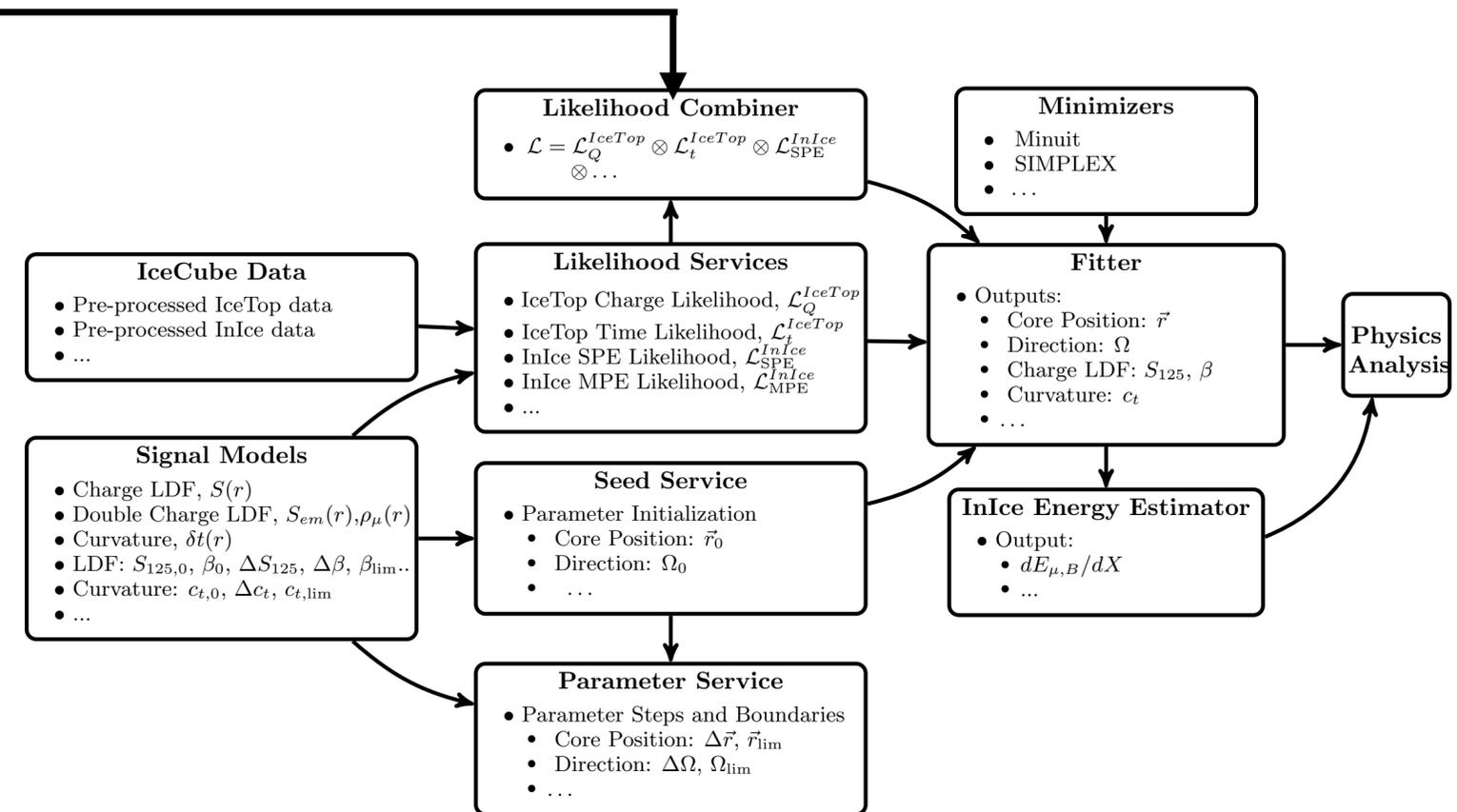
Events are reconstructed using a combined reconstruction (3D Reconstruction)

## Combined Reconstruction

- Combines the likelihoods of IceTop and InIce together for event reconstruction
- Timing Likelihood: Implementation of a **flexible curvature** and **new timing fluctuation**

## Events

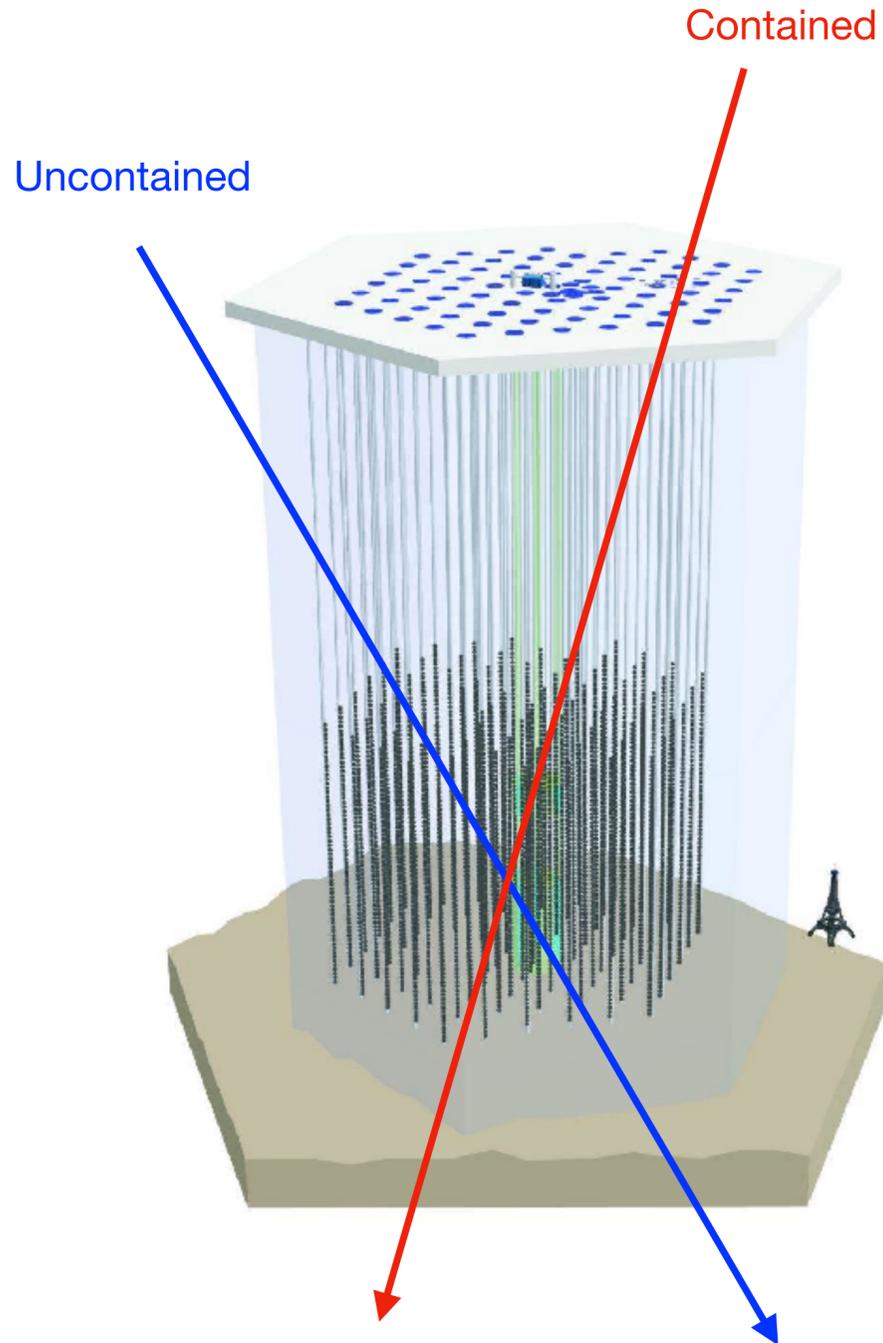
- Monte Carlo events for proton, helium, oxygen, and iron primaries (IC86-2012).



<https://wiki.icecube.wisc.edu/index.php/RockBottom>

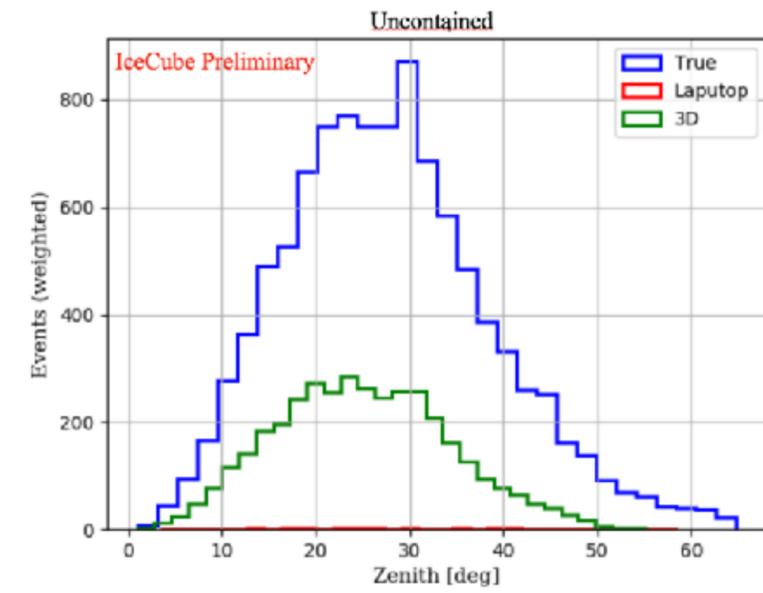
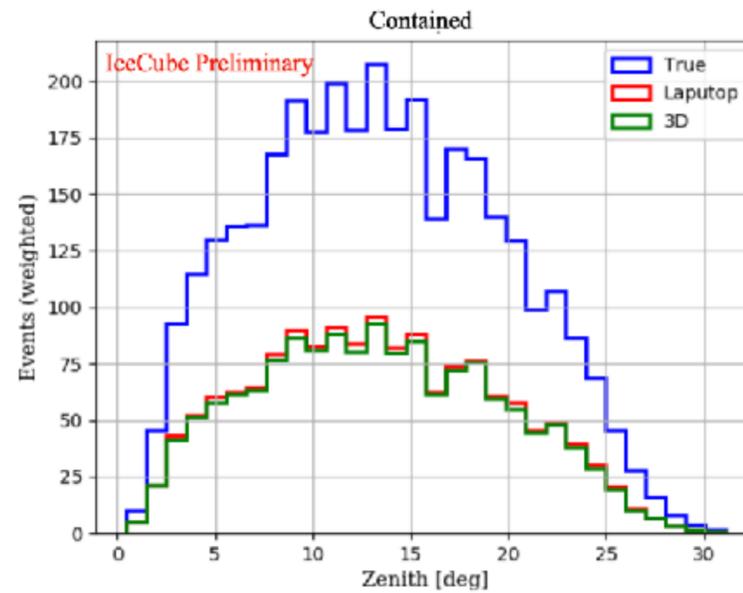
# Energy estimation method using Linear fit

Proton	Iron
Oxygen	Helium

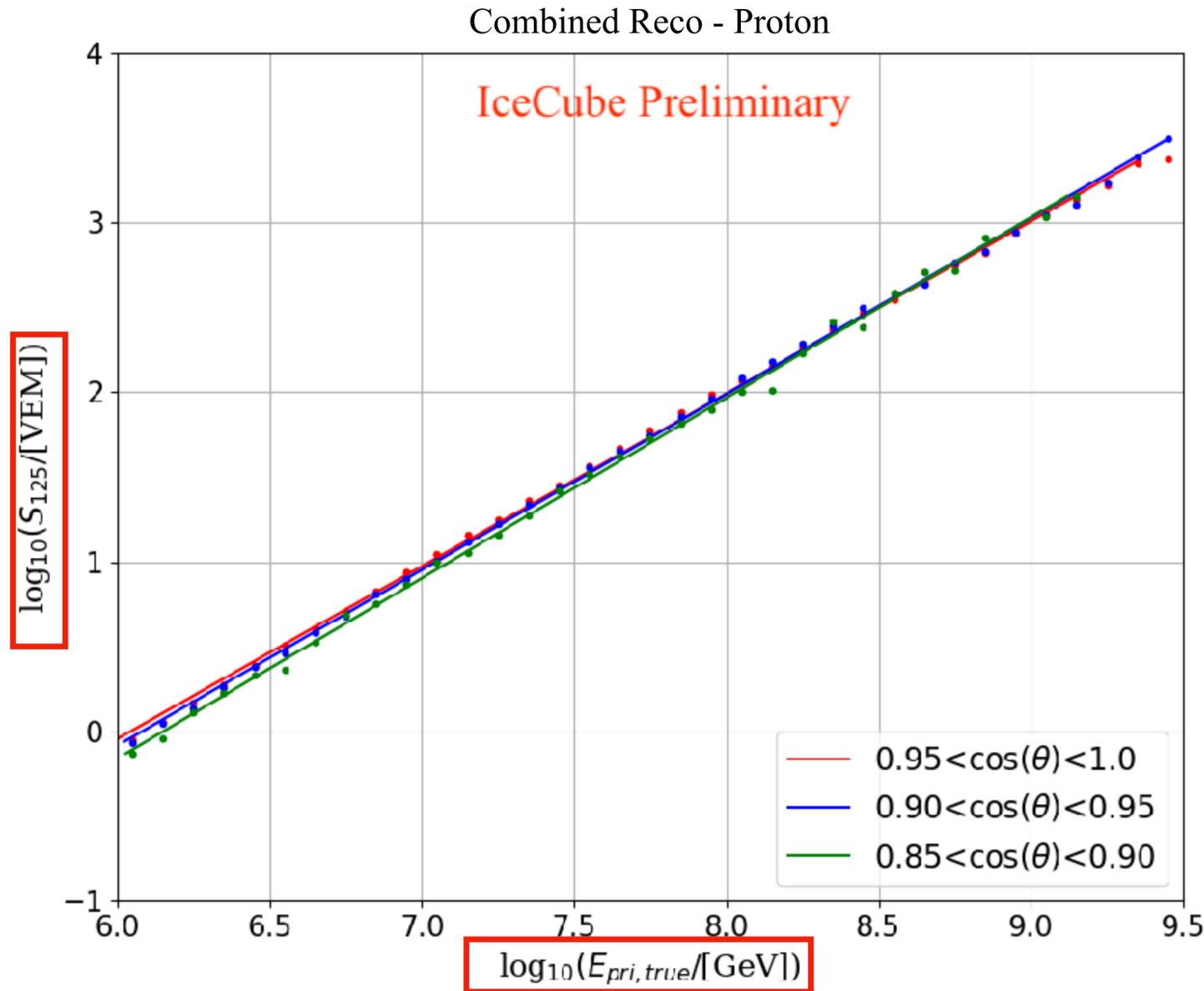


Linear Fit method:

- Analyze proton, helium, oxygen, and iron primaries separately.
- For each primaries split events in contained and uncontained events
- Considering different zenith ranges



# Energy estimation method using Linear fit

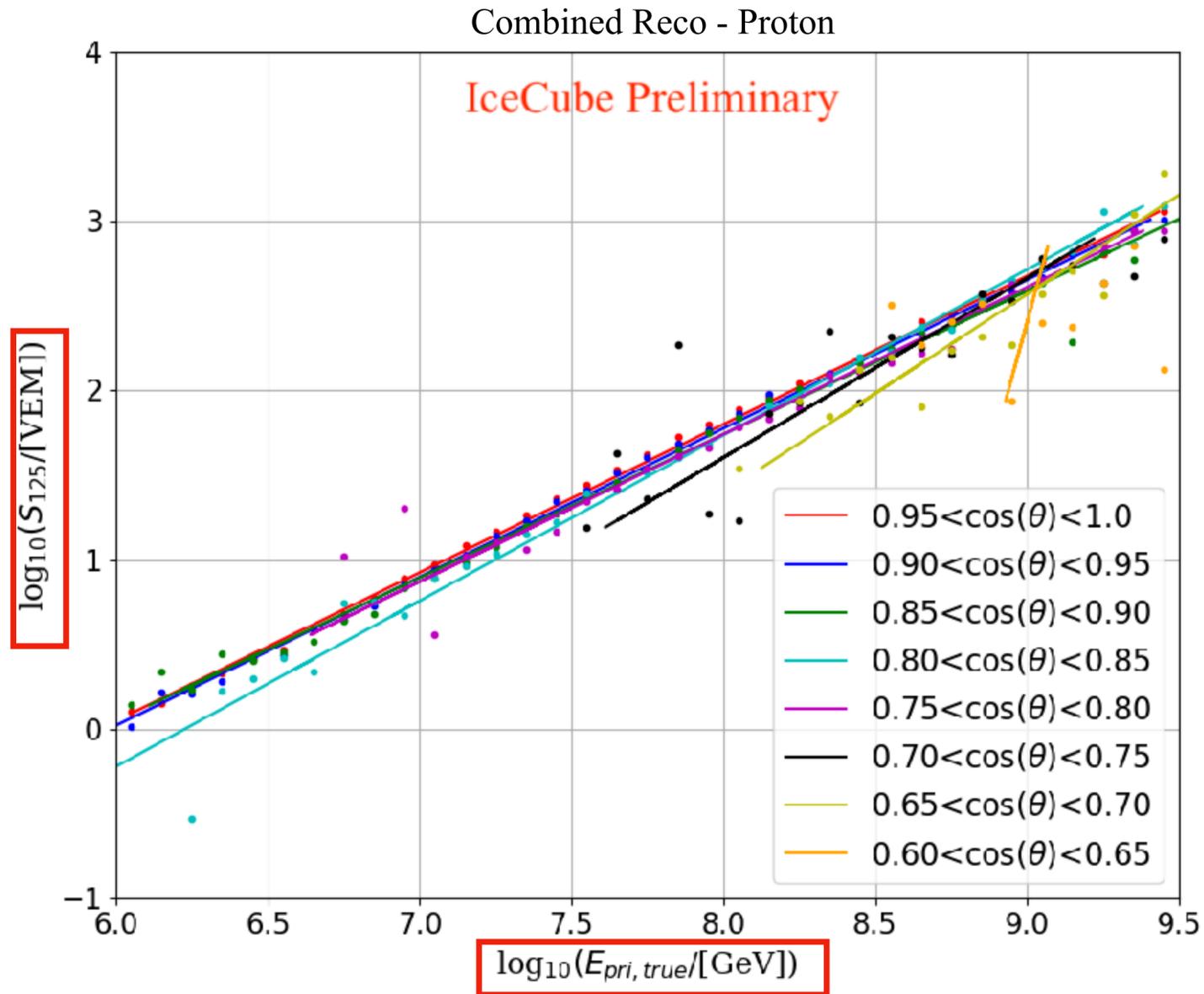


$$\log_{10}(E[\text{GeV}]) = p_0 + p_1 \log_{10}(S_{125}[\text{VEM}])$$

Combined Reco - Contained Events		
Zenith	$p_0$	$p_1$
$0.95 < \cos(\theta) < 1.0$	6.0446	0.9824
$0.90 < \cos(\theta) < 0.95$	6.0822	0.9639
$0.85 < \cos(\theta) < 0.90$	6.1517	0.9399

Note: Calculation for Helium, Oxygen and Iron at backup

# Energy estimation method using Linear fit

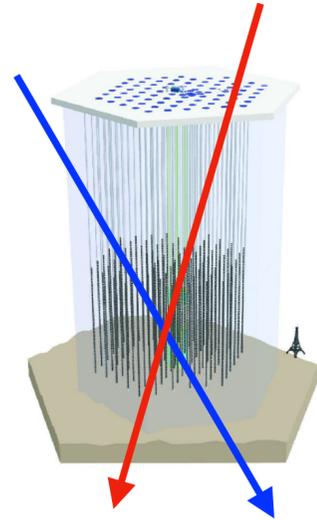
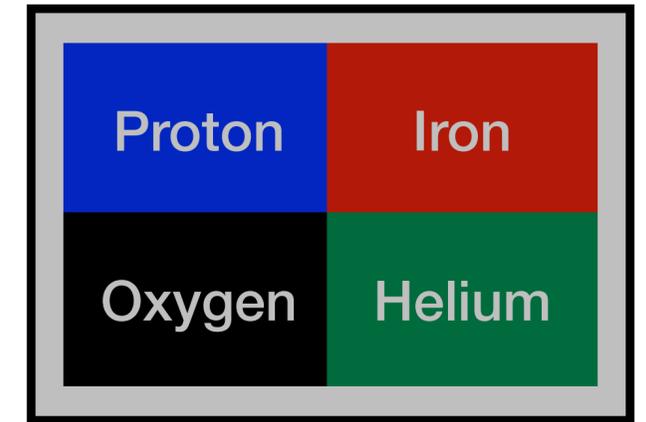


$$\log_{10}(E[GeV]) = p_0 + p_1 \log_{10}(S_{125}[VEM])$$

Combiend Reco - Uncontained Events		
Zenith	$p_0$	$p_1$
0.95 < $\cos(\theta)$ < 1.0	5.9447	1.1413
0.90 < $\cos(\theta)$ < 0.95	5.9767	1.1390
0.85 < $\cos(\theta)$ < 0.90	5.9451	1.1796
0.80 < $\cos(\theta)$ < 0.85	6.2266	1.0214
0.75 < $\cos(\theta)$ < 0.80	5.9997	1.1487
0.70 < $\cos(\theta)$ < 0.75	6.4873	0.9432
0.65 < $\cos(\theta)$ < 0.70	6.8099	0.8525
0.60 < $\cos(\theta)$ < 0.65	8.6340	0.1522

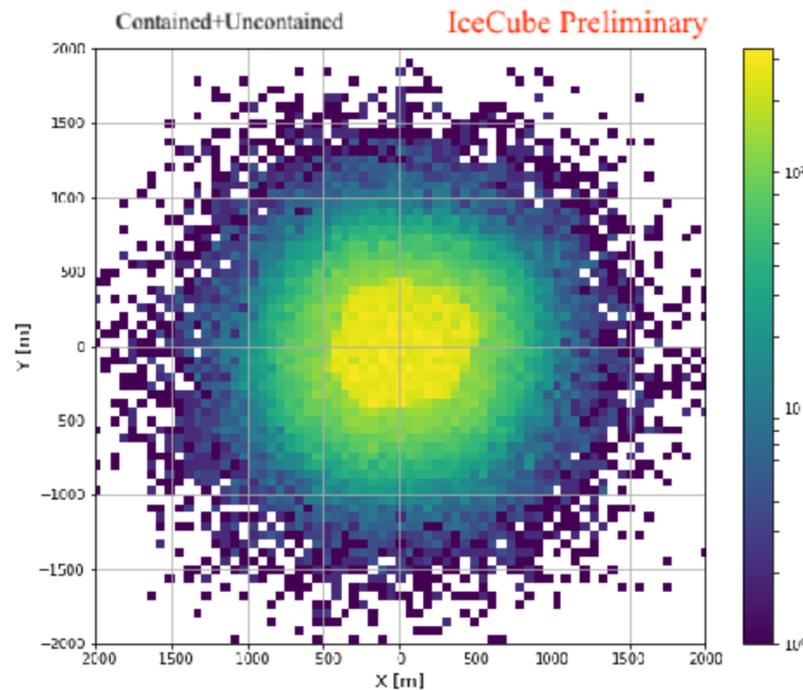
Note: Calculation for Helium, Oxygen and Iron at backup

# Energy estimation/prediction using Random Forest Regression



Random Forest Regression prediction:

- Consider proton, helium, oxygen and iron primaries together!!.
- Consider contained and uncontained events together!!.
- Zenith dependence as one feature parameter for training.
- Give the possibility to consider InIce feature parameters.



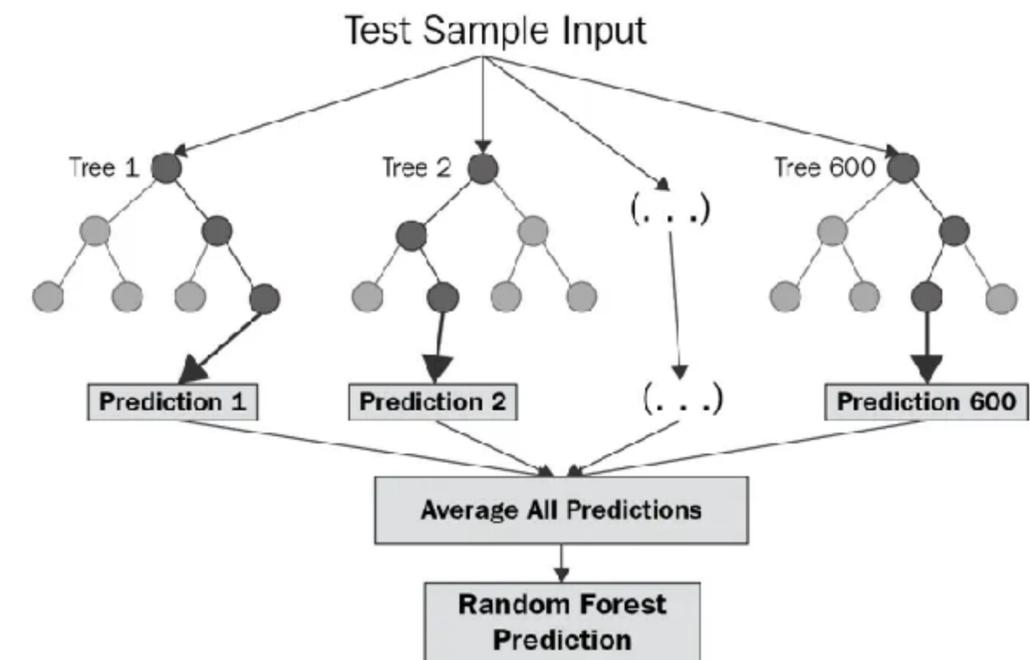
# Energy estimation/prediction using Random Forest Regression

## Events Selection

- Monte Carlo events for proton, iron, helium and oxygen (IC86-2012)
- Selection Criteria:
  - Contained: Core location inside of IceTop Array and InIce muon track
  - Uncontained: Core location outside IceTop Array and InIce muon track
- Requiring a successful reconstruction

## Machine Learning

- Random Forest Regression (open-source Python package Scikit-Learn).



- $R^2$  regression score function.

# Energy estimation/prediction using Random Forest Regression

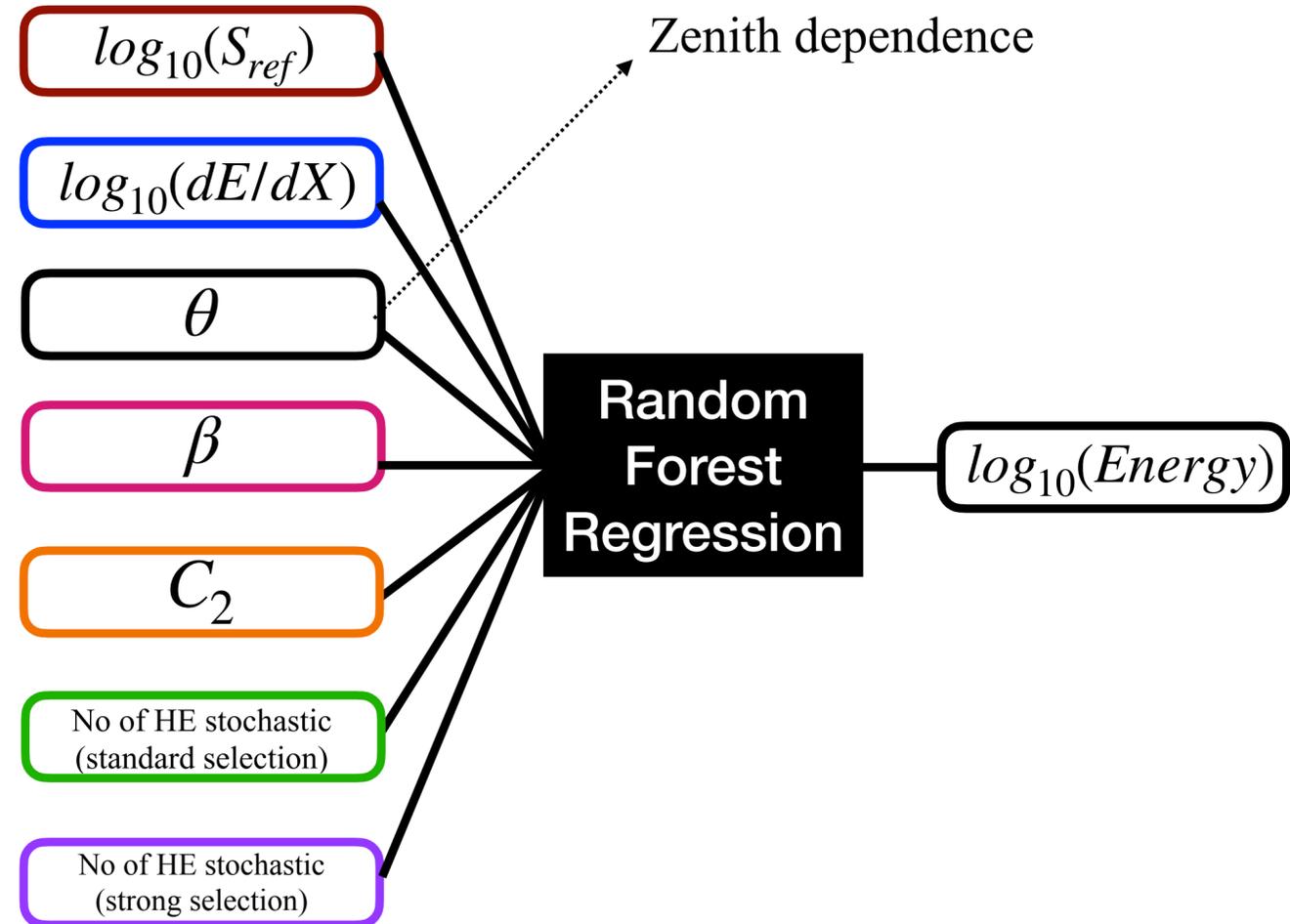
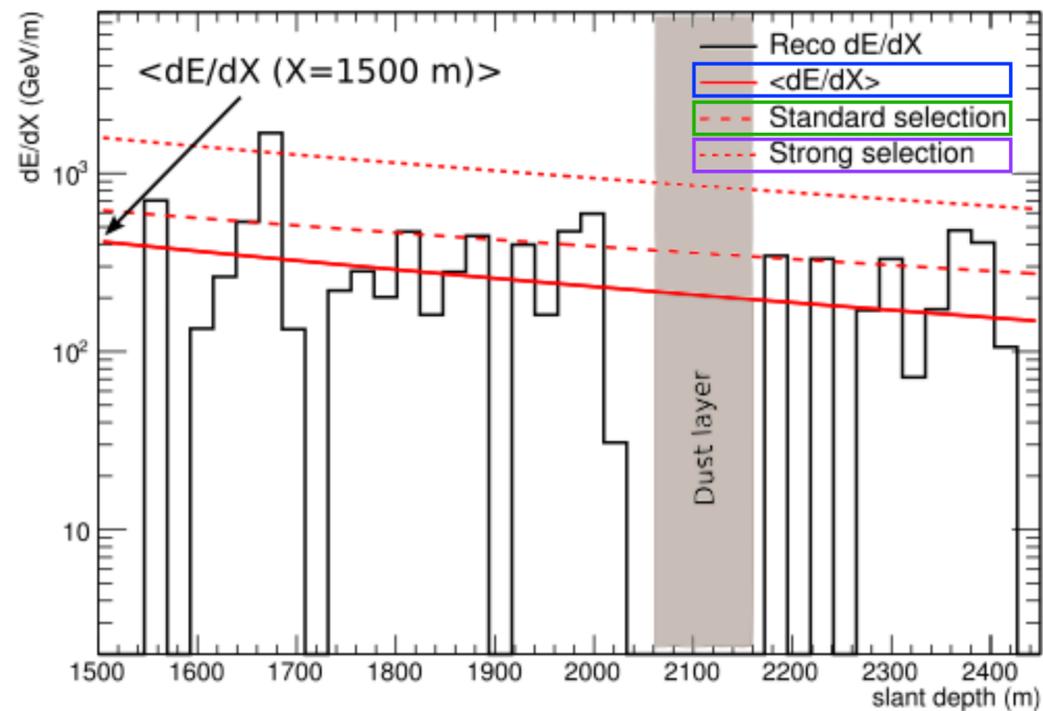
**LDF**

$$S(r) = S_{ref} \left( \frac{R}{R_{ref}} \right)^{-\beta - \kappa \log_{10}(R/R_{ref})}$$

**Time Residuals**

$$\Delta t(R) = C_2 R^2 + C_1 \left( 1 - \exp\left(-\frac{R^2}{2\sigma^2}\right) \right)$$

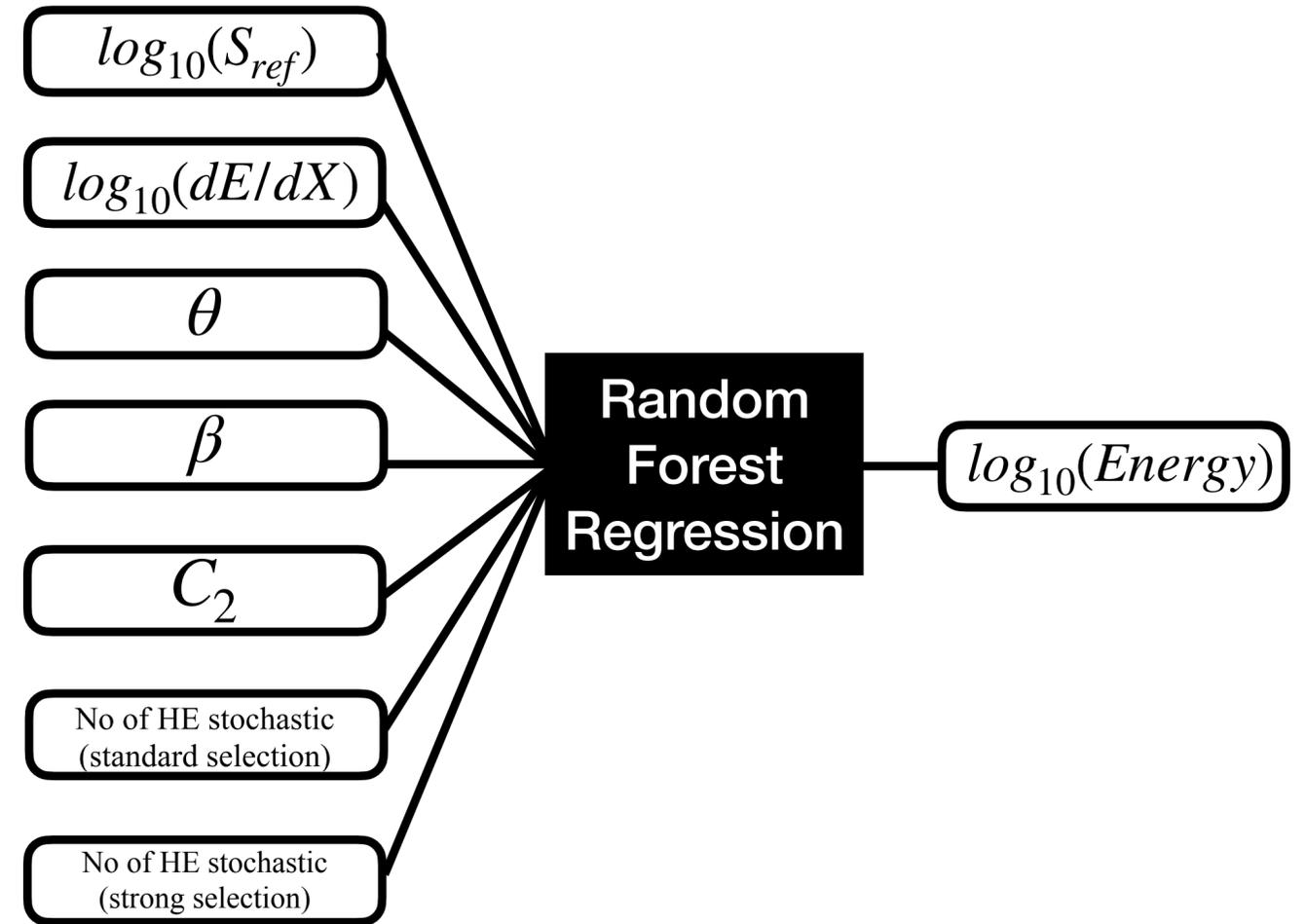
<https://arxiv.org/pdf/1906.04317.pdf>



# Energy estimation/prediction using Random Forest Regression

The training and testing dataset has a total 176070 events (proton, iron, helium and oxygen).

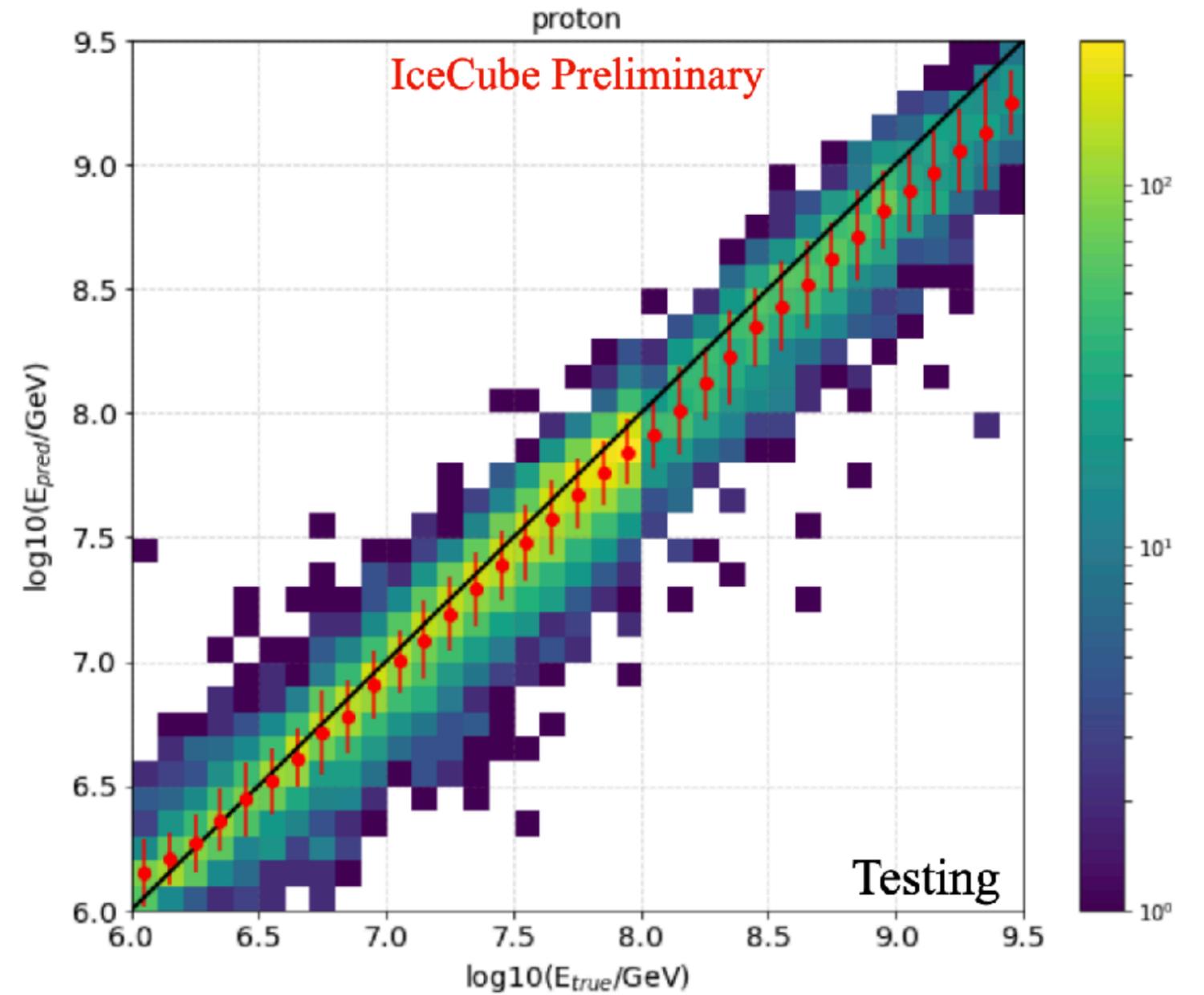
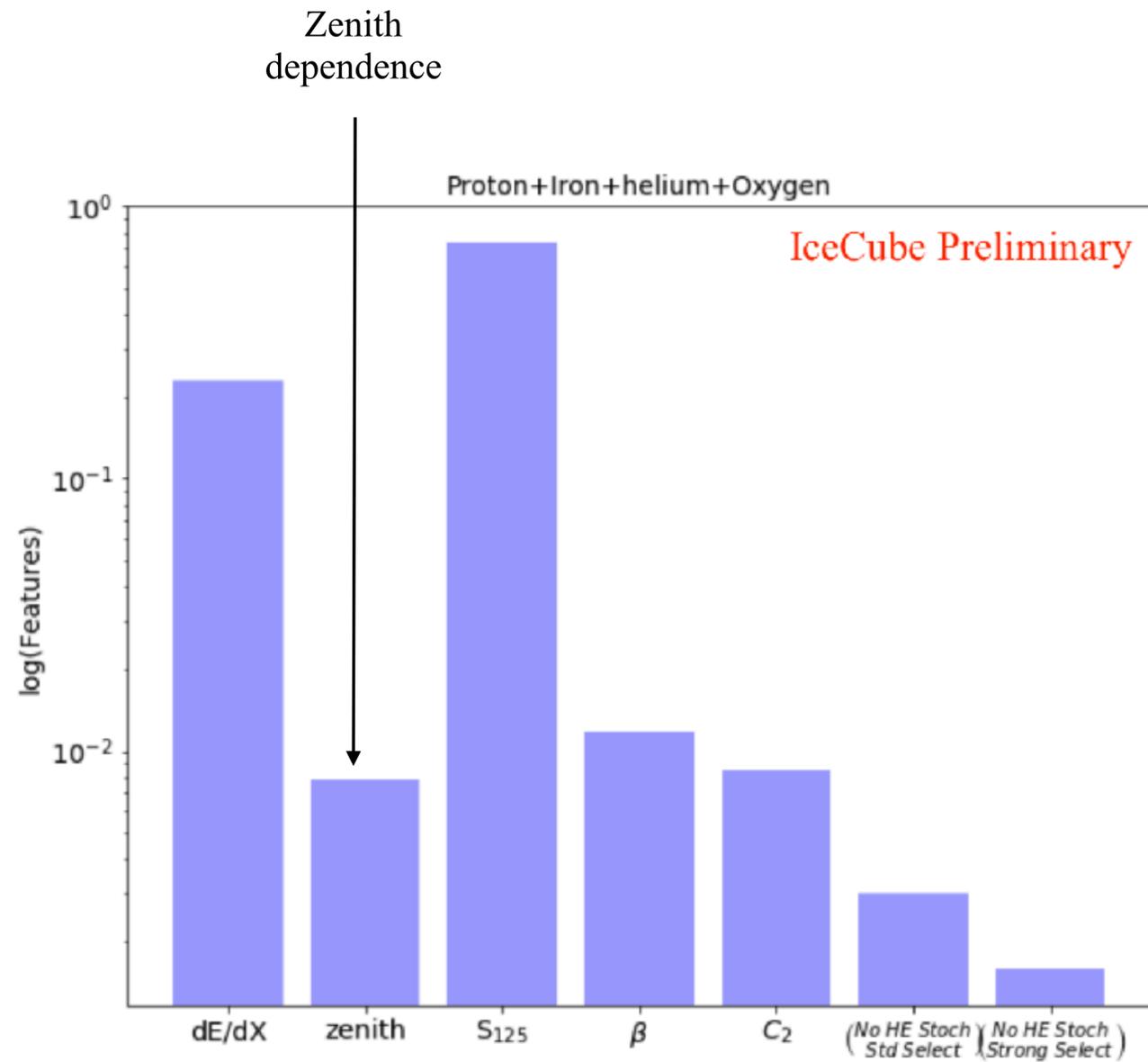
- 75% for Training
- 25% for Testing



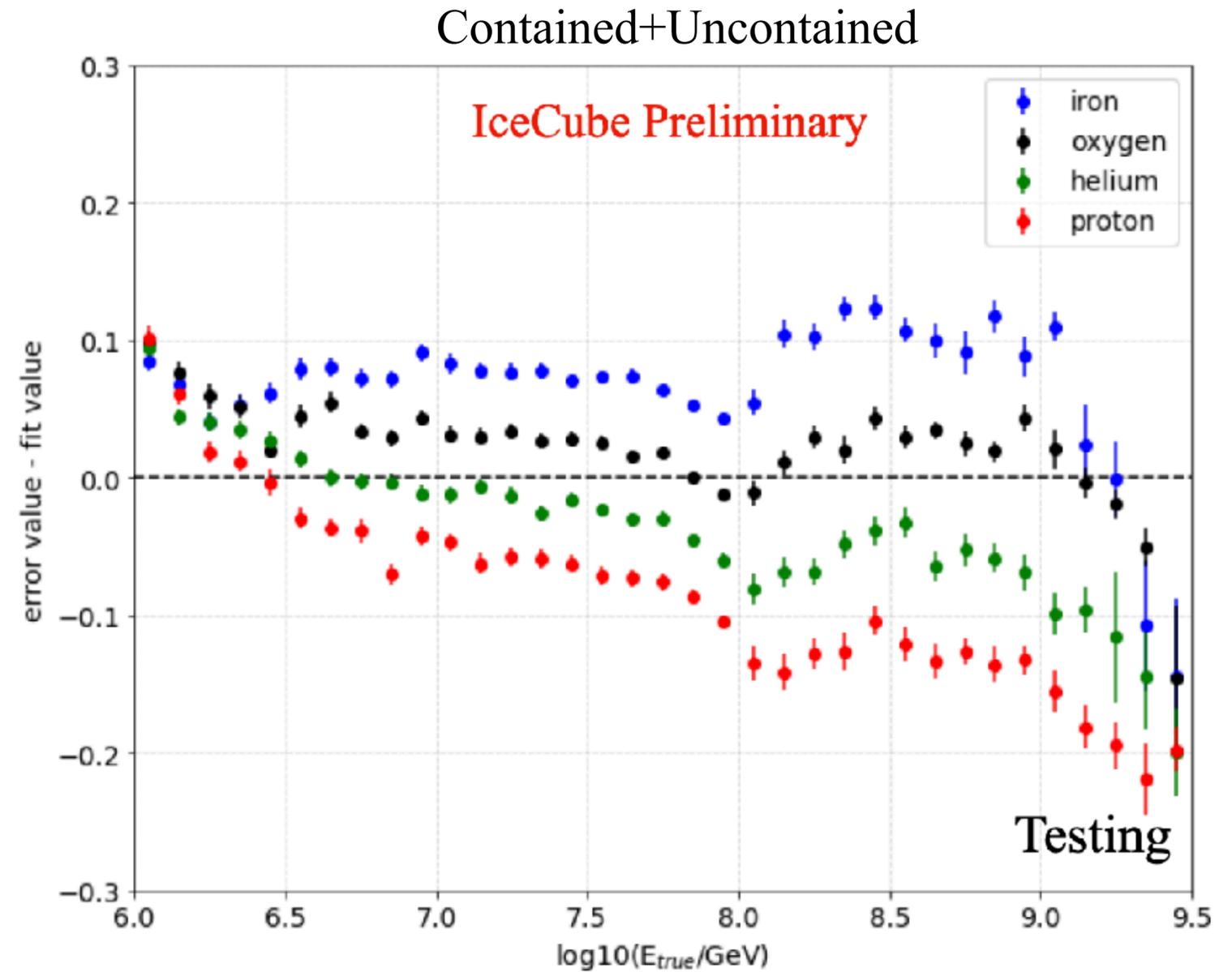
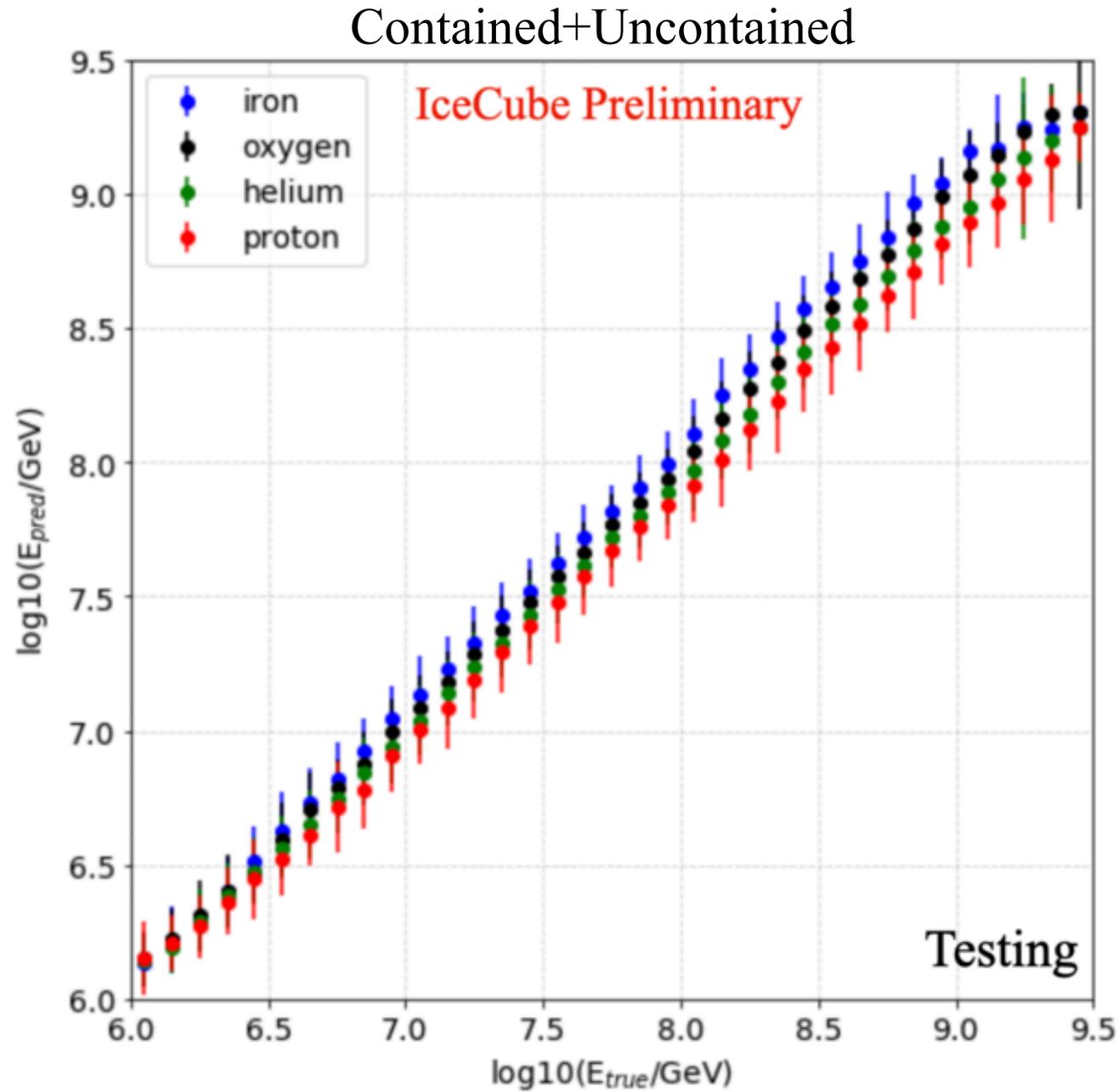
Regression Score	
Training	99.48%
Testing	96.37%



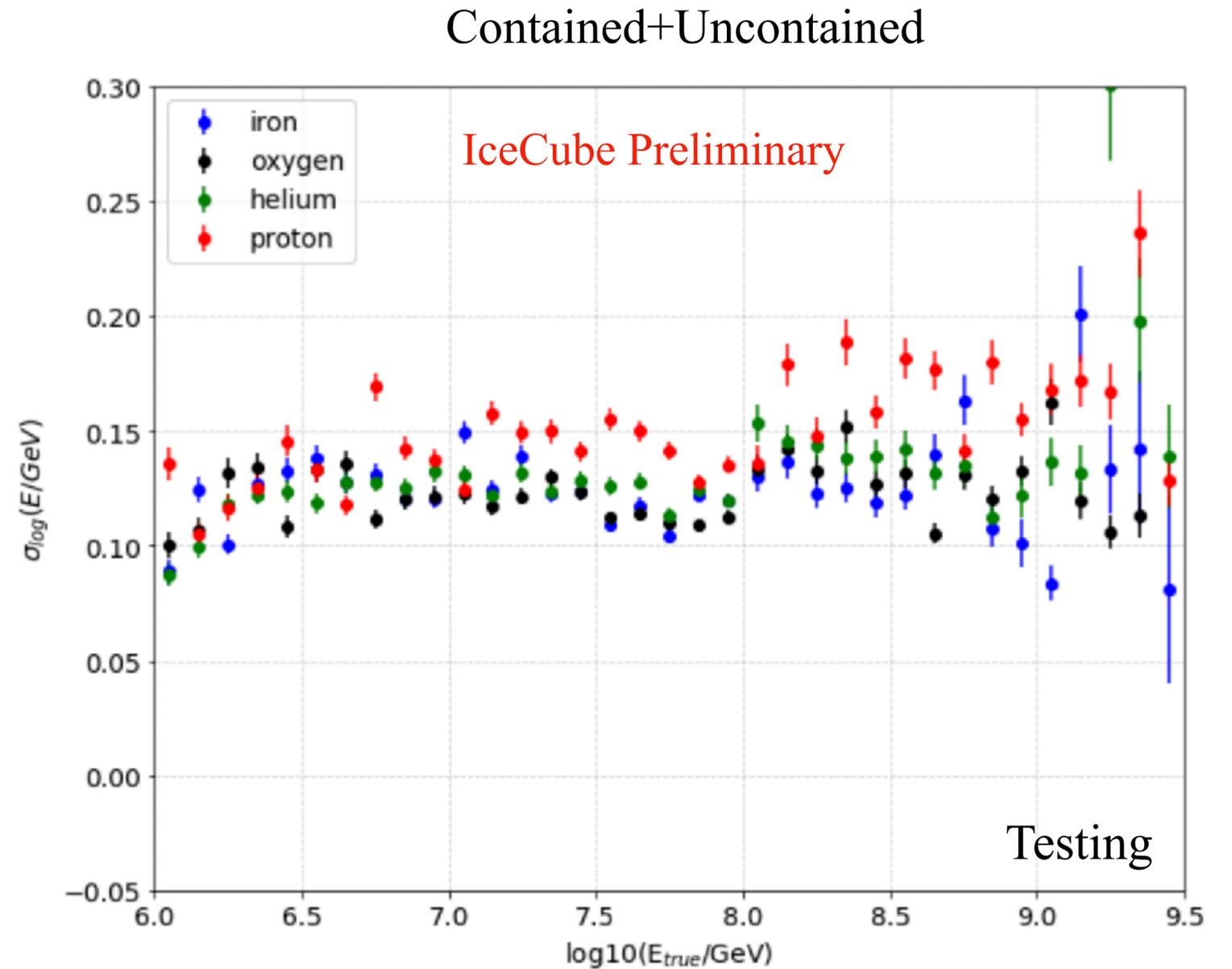
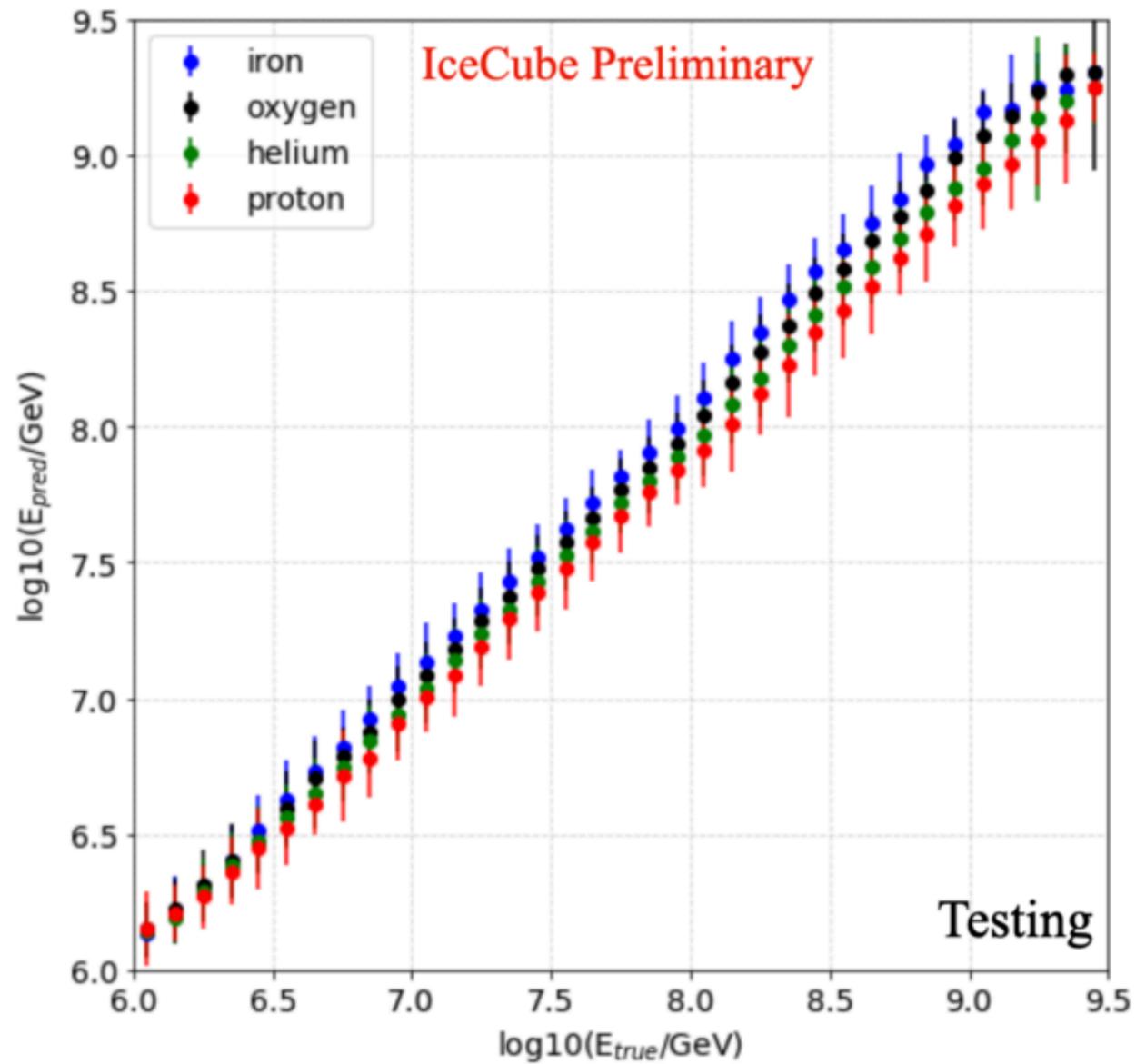
# Energy estimation/prediction using Random Forest Regression



# Energy estimation/prediction using Random Forest Regression

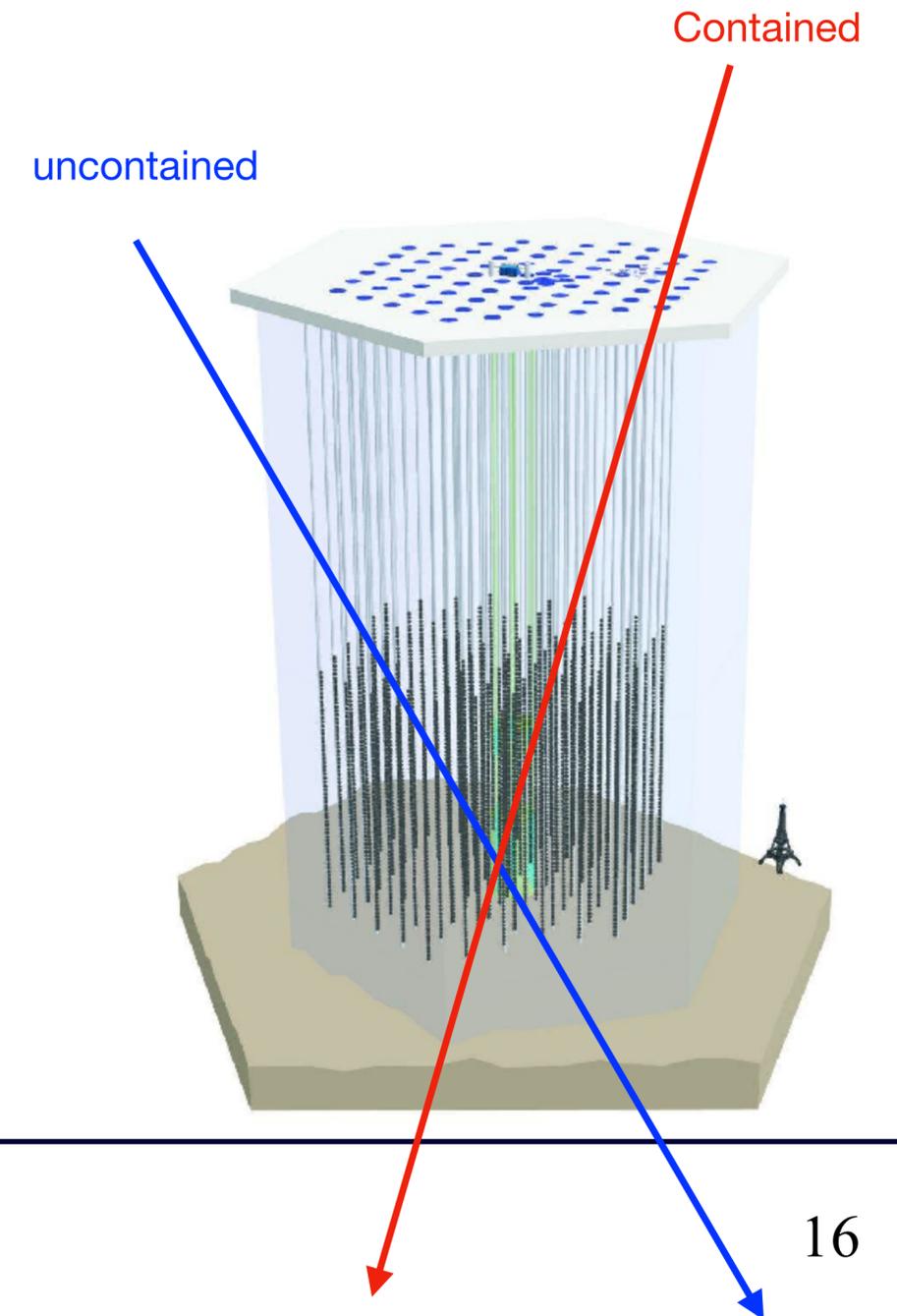


# Energy estimation/prediction using Random Forest Regression

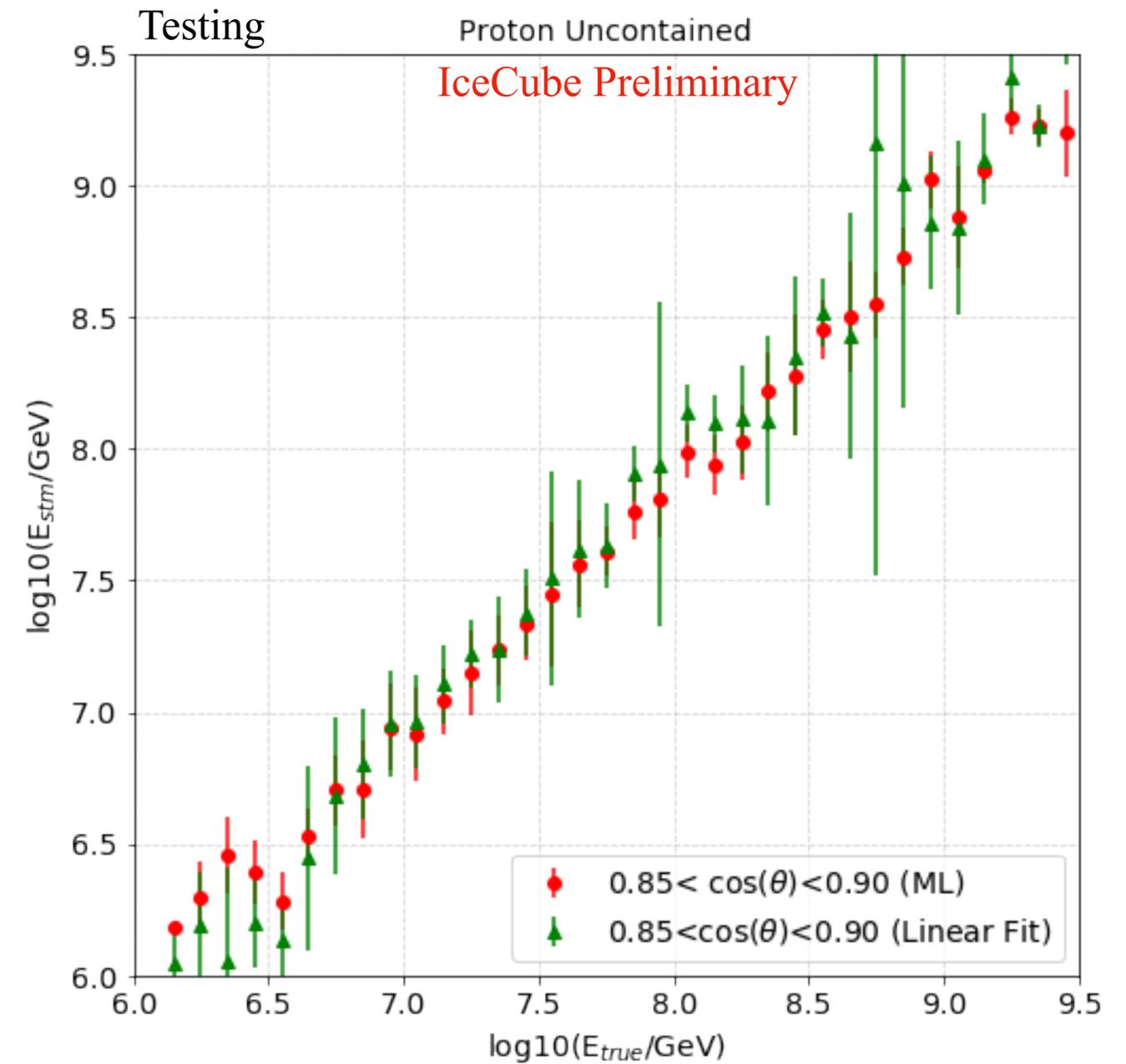
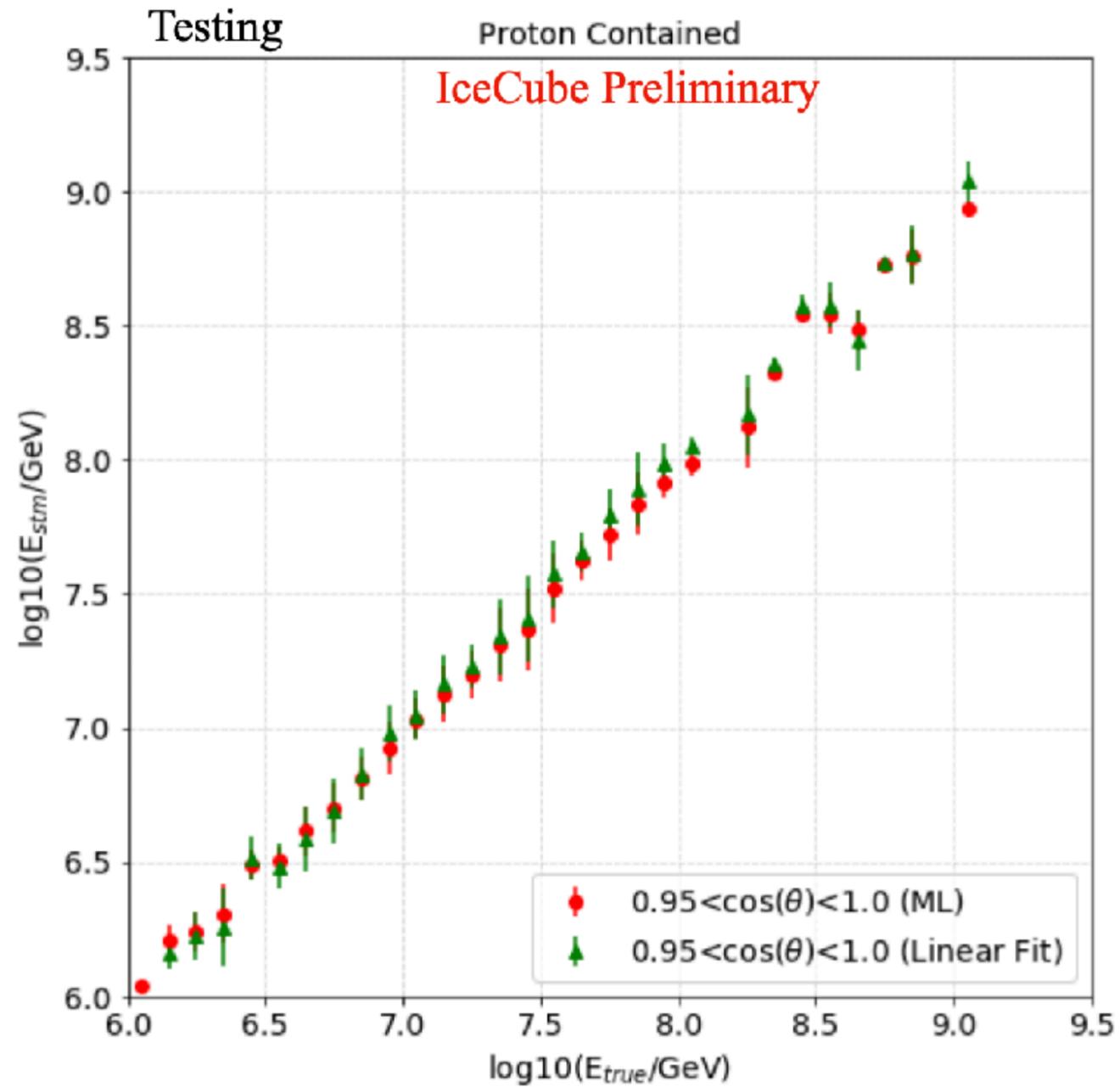


# Comparison between Linear Fit and Random Forest Regression performance

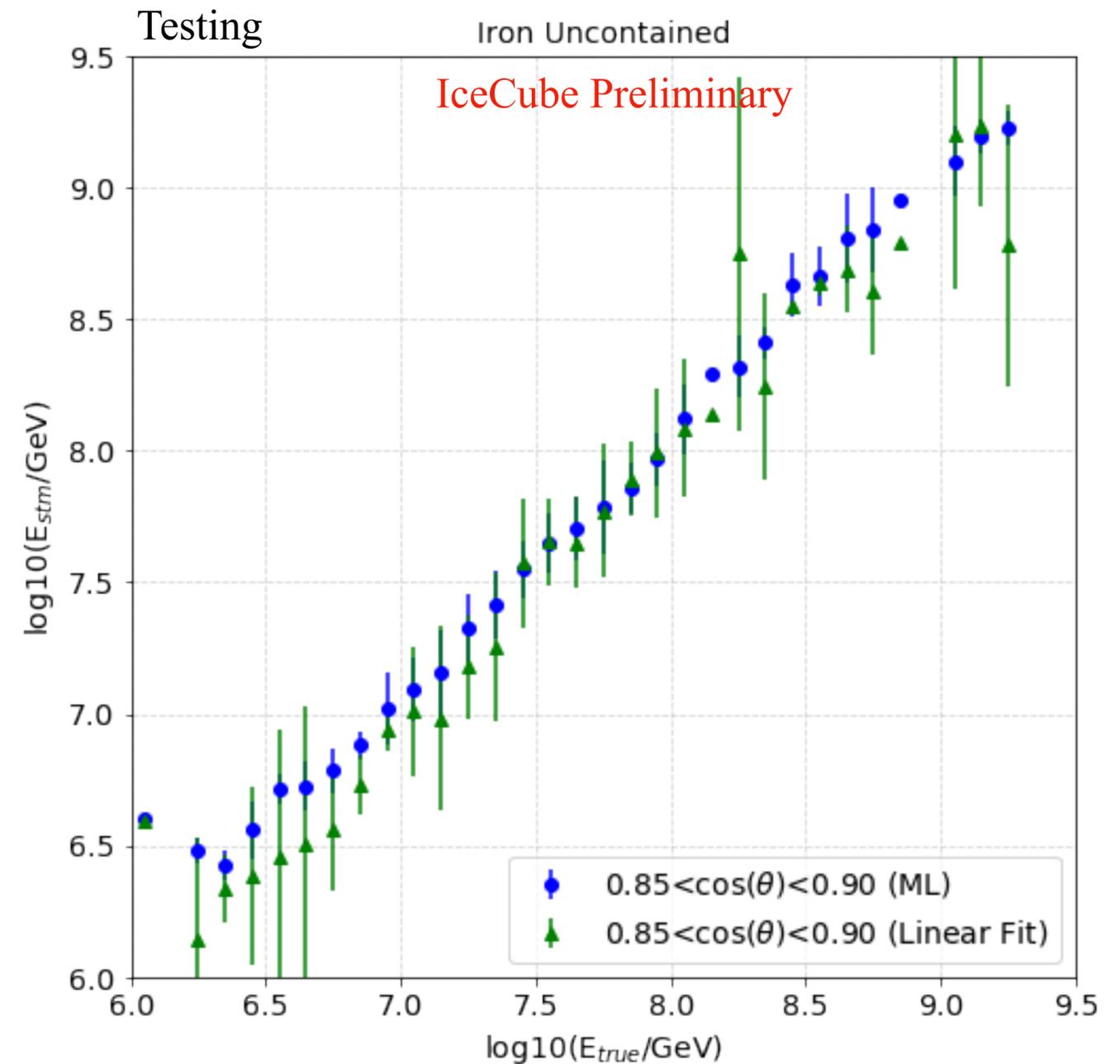
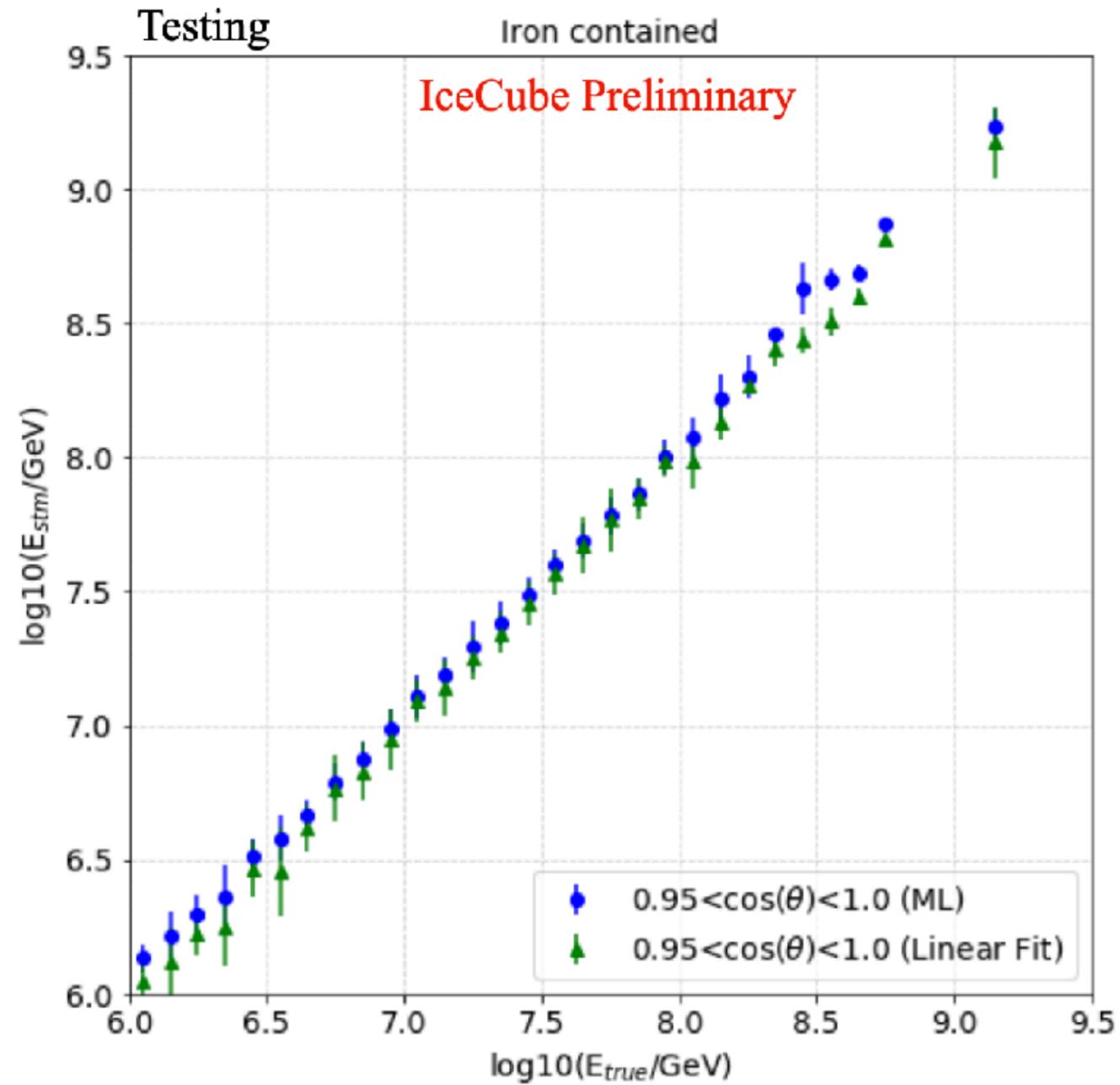
- Preliminary comparison considering proton and iron events (contained and uncontained)
- Specific energy ranges:
  - Contained:  $0.95 < \cos(\theta) < 1.0$
  - Uncontained:  $0.85 < \cos(\theta) < 0.90$



# Comparison between Linear Fit and Random Forest Regression performance



# Comparison between Linear Fit and Random Forest Regression performance



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# Summary

- In this work we implemented a combined reconstruction considering contained and uncontained events for proton, iron, helium and oxygen for IceTop and IceCube.
- Two methods for primary energy estimation were implemented. ML performs a comparable results related with contained events. While for uncontained events ML approach offers a better performance.



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# Backup



# Flexible Curvature

## Conventional

$$\Delta t(R) = C_2 R^2 + C_1 \left(1 - \exp\left(-\frac{R^2}{2\sigma^2}\right)\right)$$

Fix parameter

## New Flexible Curvature

$$\Delta t(R) = C_2 R^2 + C_1 \left(1 - \exp\left(-\frac{R^2}{2\sigma^2}\right)\right)$$

$(10^{-6}, 10^{-2}) \quad [ns \cdot m^{-2}]$

# New Timing Fluctuation

## Conventional

$$\sigma_t(R) = a + bR^2$$

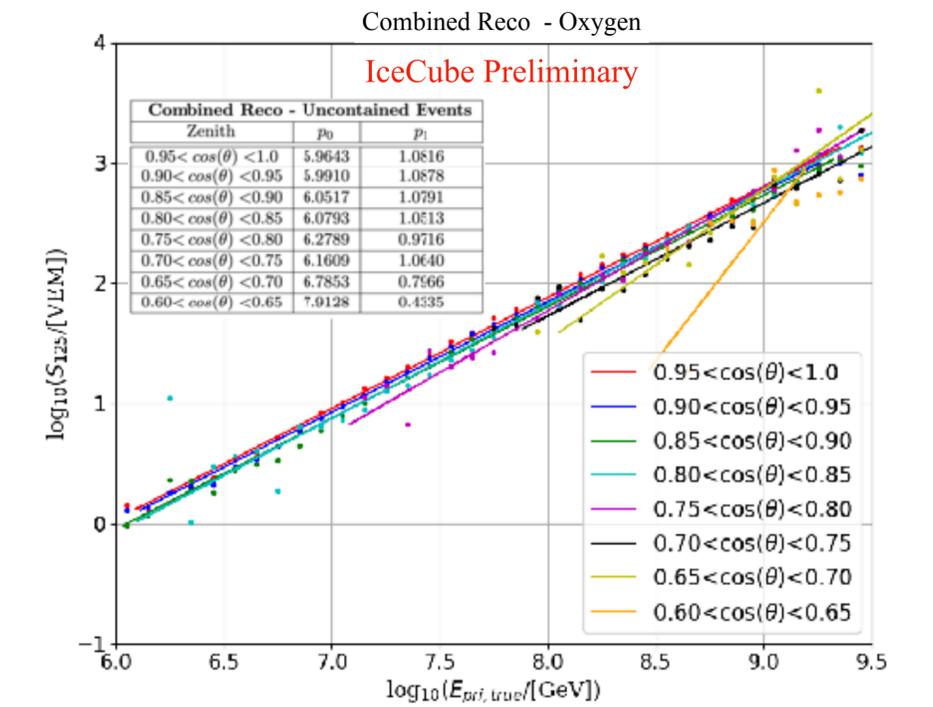
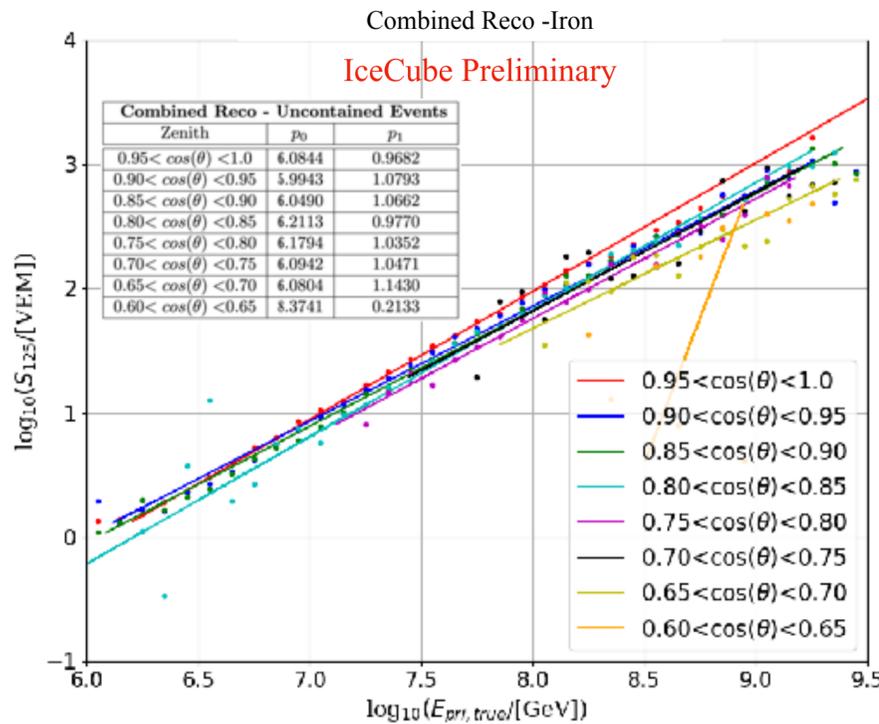
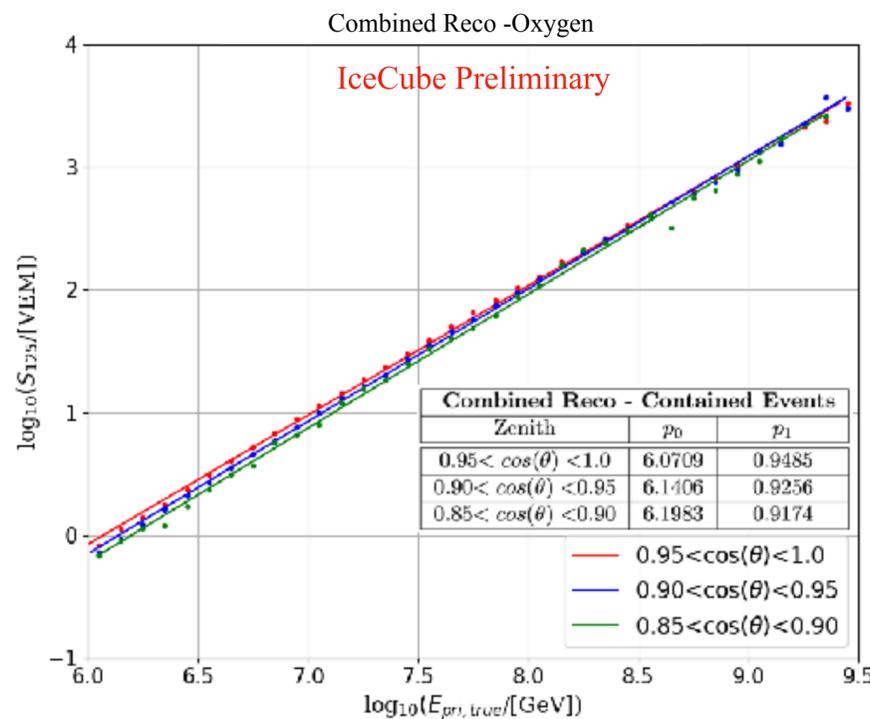
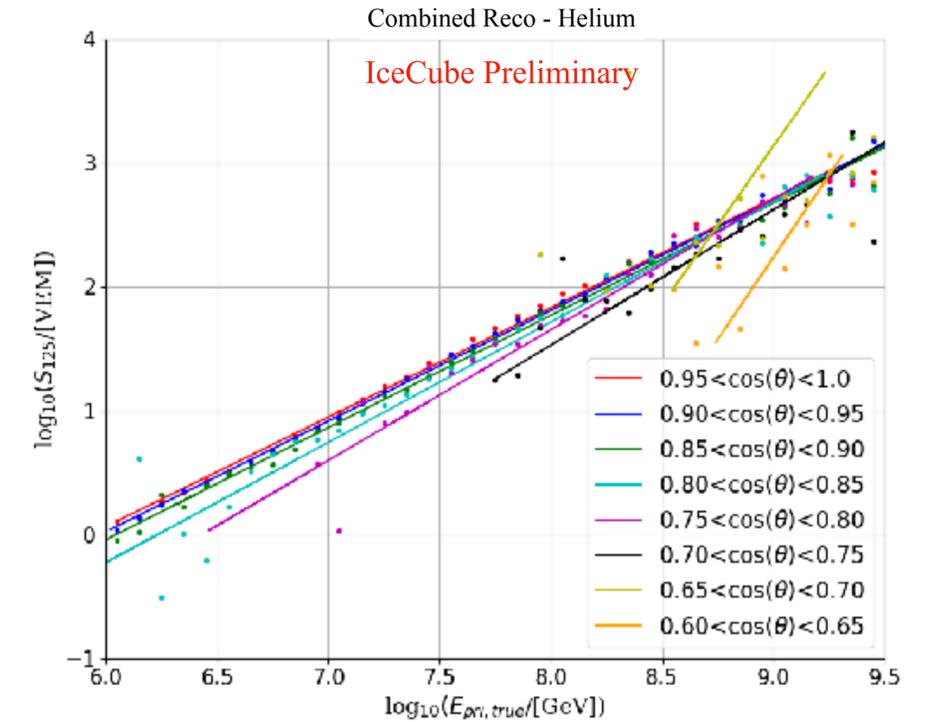
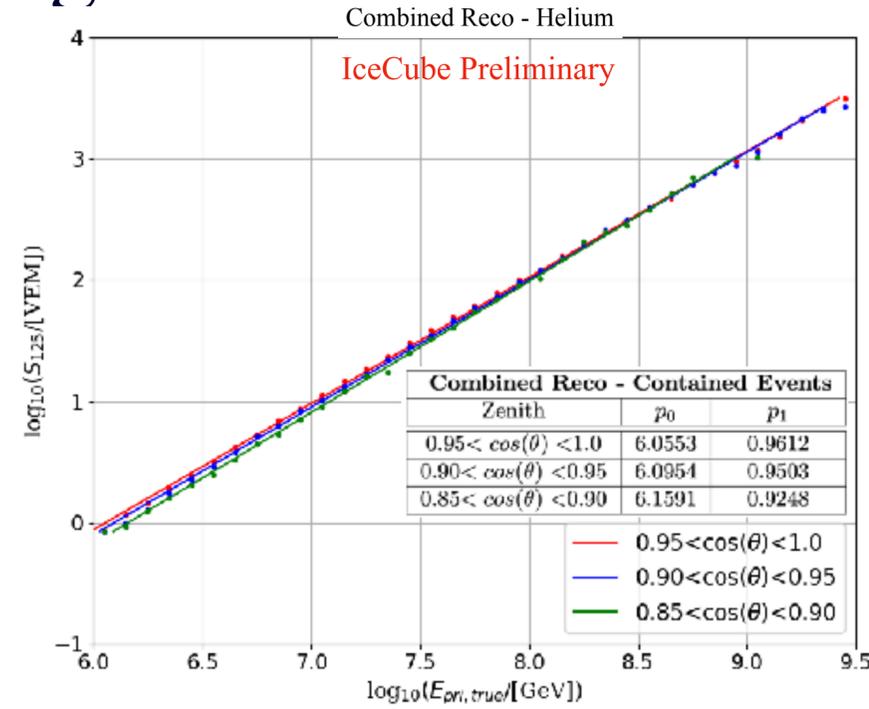
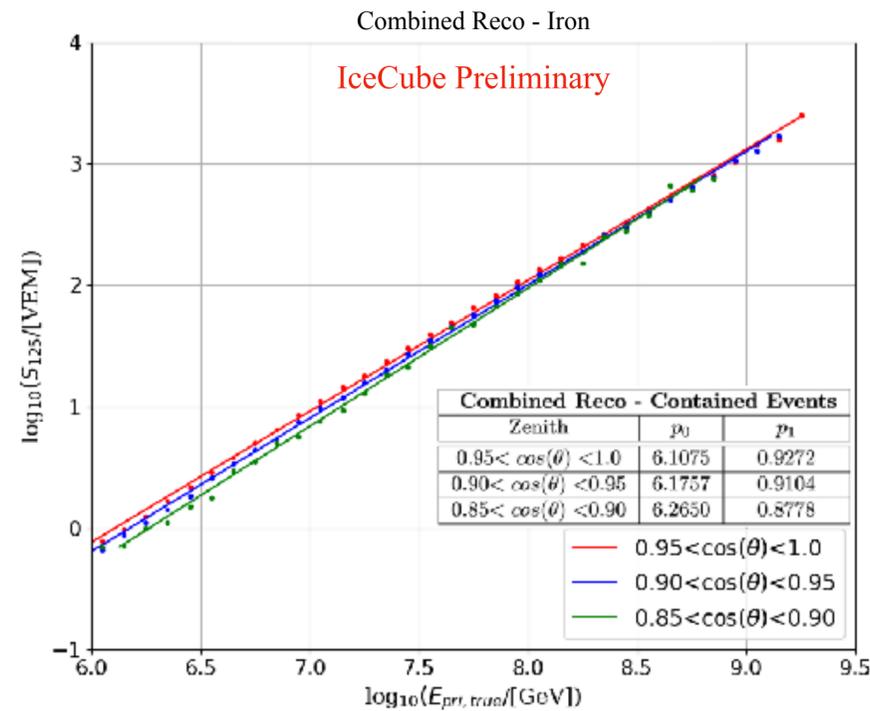
## New Timing fluctuation

$$\sigma_{ti} = C \frac{\sqrt{\sum_{j=1}^2 (t_{ij} - (\frac{t_{i1} + t_{i2}}{2}))^2}}{(\sum_{j=1}^2 Q_{ij})^a} + b$$

Not.	Value	Units
a	1.00	
b	1.22	ns
C	4	VEM

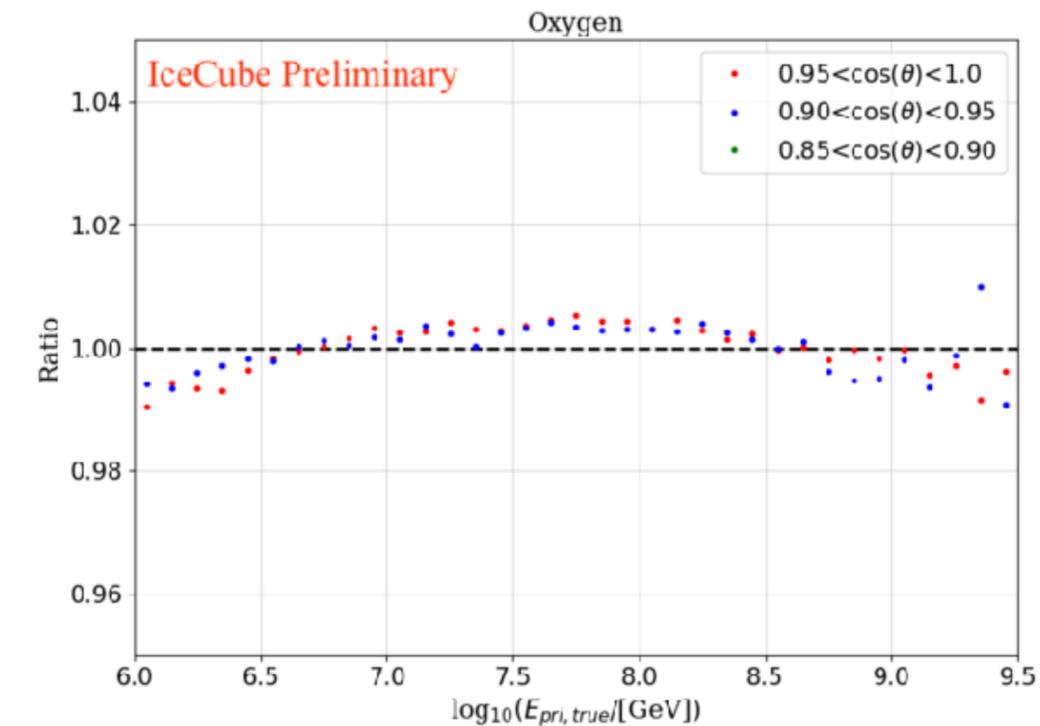
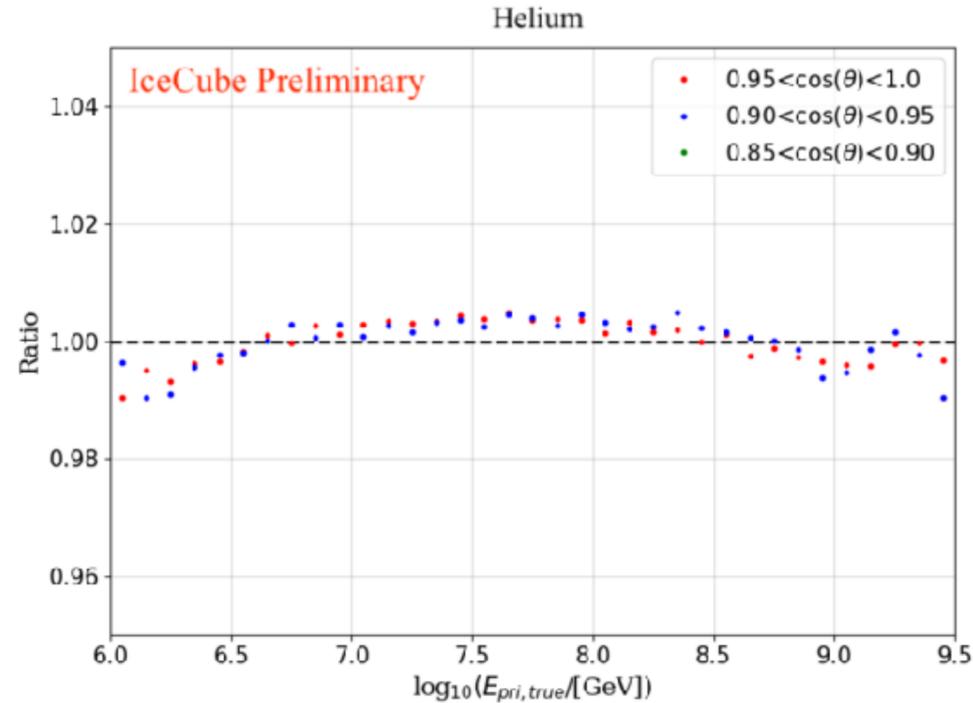
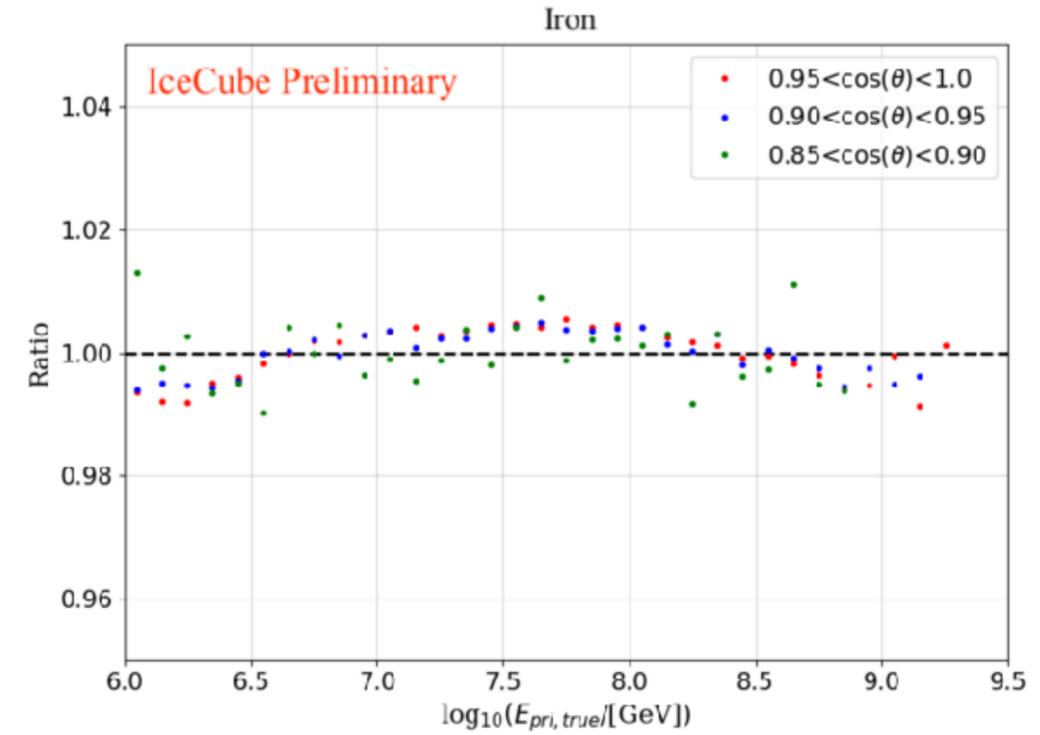
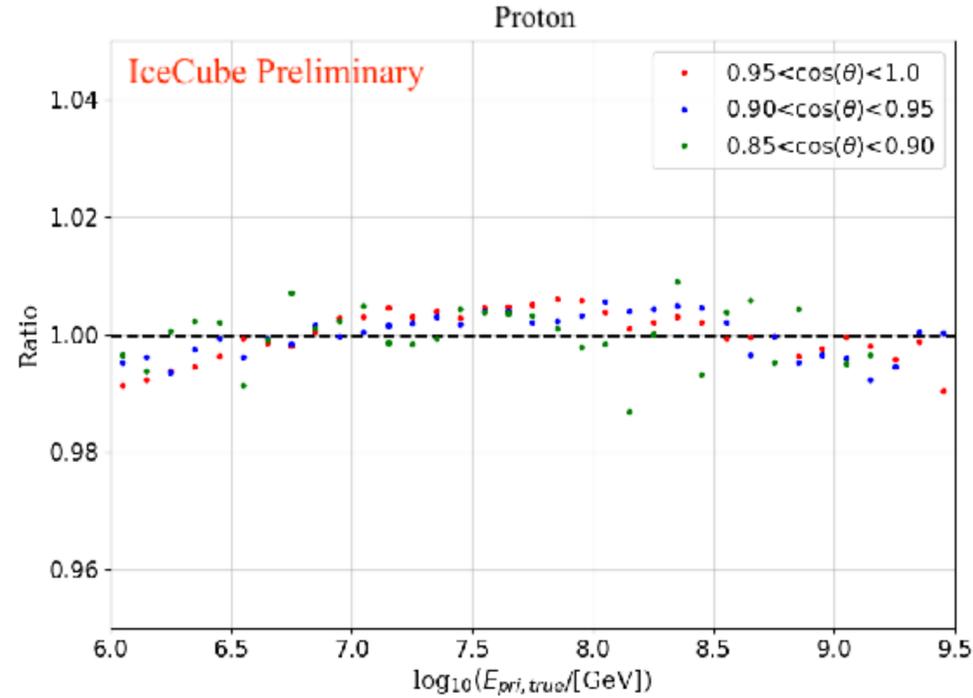


# Energy estimation method using Linear fit



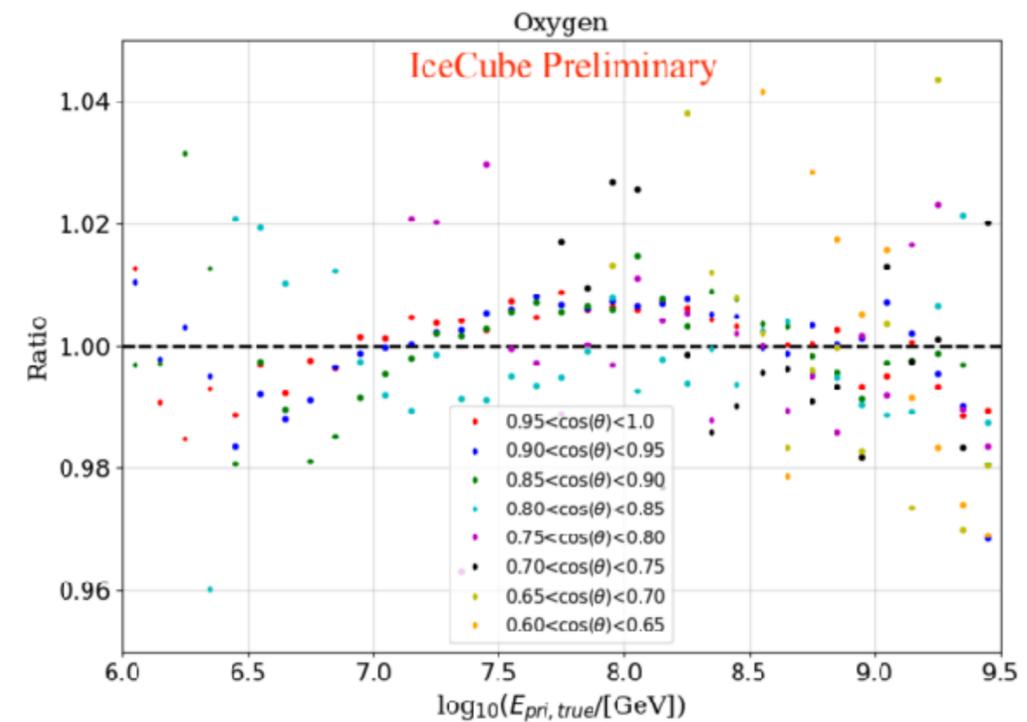
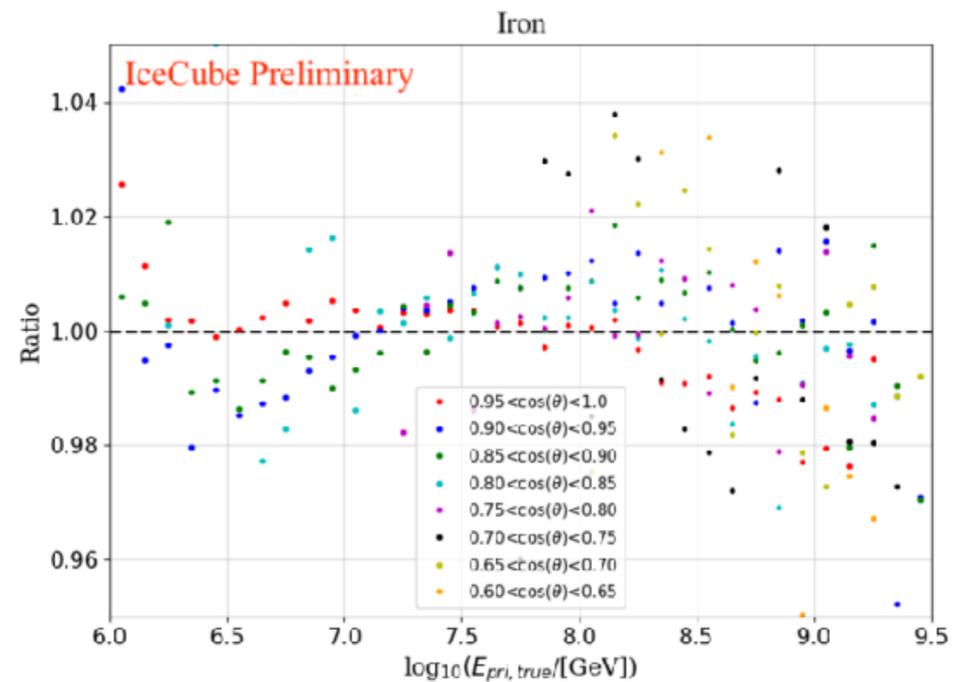
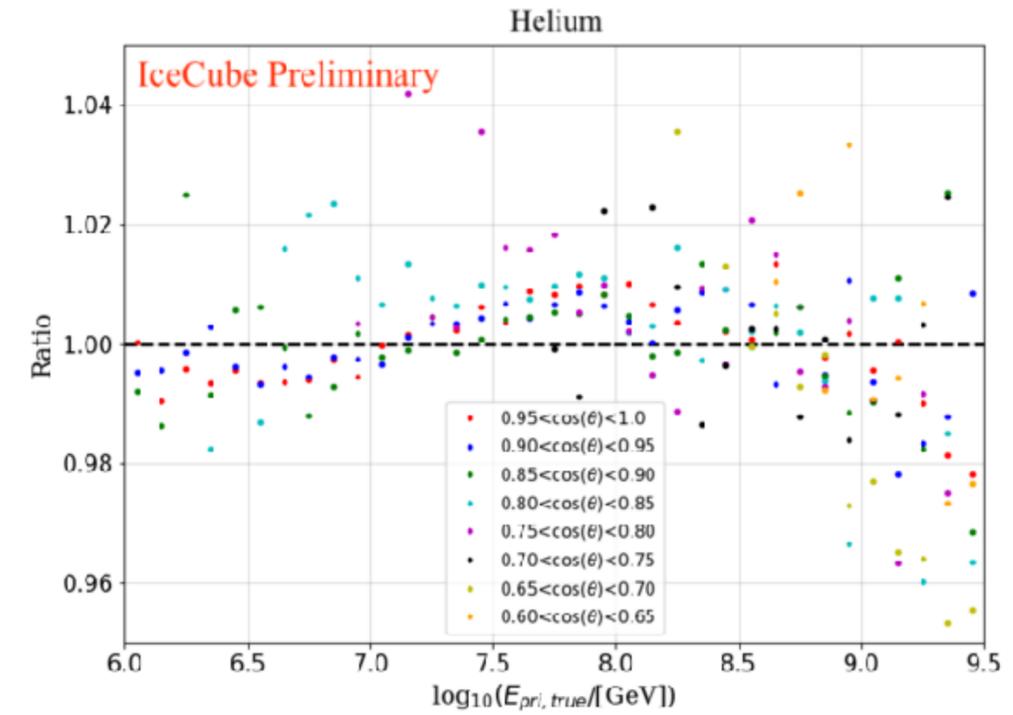
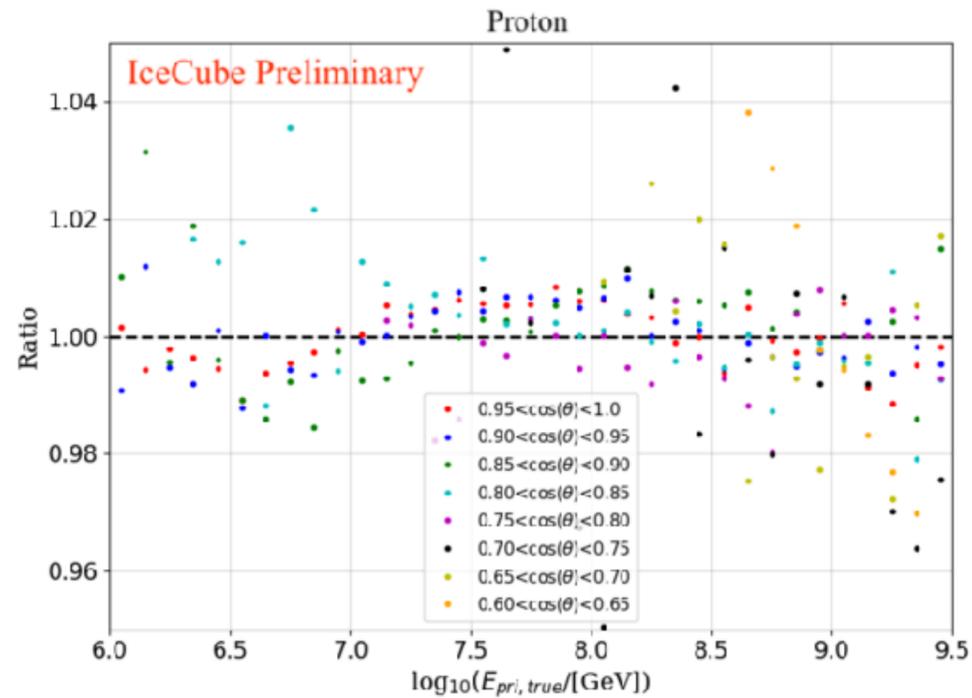
# Energy estimation method using Linear fit

Contained  
Events



# Energy estimation method using Linear fit

Uncontained  
Events



# Energy estimation/prediction using Random Forest Regression

